1	Kinetic study of 1-butanol dehydration to
2	di-n-butyl ether over Amberlyst 70
3	M. A. Pérez-Maciá, R. Bringué, M. Iborra, J. Tejero and F. Cunill
4	Department of Chemical Engineering, University of Barcelona, C/Martí i Franquès, 1,
5	08028 – Barcelona
6	
7	
8	Abstract
9	Kinetics of the catalytic dehydration of 1-butanol to di-n-butyl ether (DNBE) over
10	Amberlyst-70 was investigated. Experiments were performed in liquid phase at 4 MPa and
11	413-463 K. Three elementary reaction mechanisms were considered: a Langmuir-Hinselwood-
12	Hougen-Watson (LHHW) formulation; an Eley-Rideal (ER) formulation in which DNBE
13	remains adsorbed; an ER formulation in which water remains adsorbed.
14	Two kinetic models explain satisfactorily the dehydration of 1-butanol to DNBE: a LHHW
15	formalism in which the surface reaction between two adjacent adsorbed molecules of 1-butanol
16	is the rate limiting step (RLS) and where the adsorption of water is negligible, and a mechanism
17	in which the RLS is the desorption of water being the adsorption of DNBE negligible. In both
18	models the strong inhibiting effect of water was successfully taken into account by means of a
19	correction factor derived from a Freundlich adsorption isotherm. Both models present similar
20	values of apparent activation energies (122±2 kJ/mol).
21	Topical area: Reaction Engineering, Kinetics and Catalysis
22	Key words: di-n-butyl ether, 1-butanol, Amberlyst 70, kinetics, water inhibiting effect.
23	

1 Introduction

2 Environmental regulations imposed over the past decades concerning diesel quality and 3 vehicles emission have led to an active search for more efficient and cleaner fuels. In this 4 search, di-n-butyl ether (DNBE) has been identified as an important candidate biofuel which can be produced from lignocellulosic biomass.^{1,2} Besides the significant advantages of using 5 lignocellulosic biomass as raw material (residues from agriculture, energy crops and forest 6 7 refuse are produced in abundance and worldwide and they have no direct competition with food, 8 thus being an attractive, inexpensive, renewable resource for the production of next generation 9 of biofuels), DNBE presents excellent properties to be blended with diesel fuel³: it has a 10 particularly high cetane number (100) indicating short ignition delay times which at the end 11 translates into relatively longer combustion process and thus less unburned hydrocarbons; its 12 moderate boiling point (415.6 K) allows facile vaporization of the fuel after engine injection 13 while minimizing the volatile organic compounds emissions during storage, transport and refueling; finally, its volumetric energy content is comparable to that of petroleum fuels 14 15 providing satisfactory engine power without modification of existing diesel engines.

Biobutanol can be produced from biomass either by fermentation or by thermochemical 16 routes.^{4,5} Currently, biobutanol is being produced on industrial scale through the ABE 17 18 fermentation process in which biomass fermentation by microorganisms of the genus Clostridium gives place to 1-butanol along with acetone and ethanol.⁶ Subsequently, DNBE can 19 be obtained by dehydration of 1-butanol over acid catalysts.^{7,8} In a previous work⁹ it was 20 21 showed that acidic ion-exchange resins were excellent catalysts for the selective dehydration of 1-butanol to di-n-butyl ether in liquid phase. Among the ion exchangers tested, Amberlyst 70 22 23 was selected as the most appropriate resin for industrial use due to its thermal stability (up to 24 463 K), its high selectivity to DNBE and its suitable activity.

In order to design and model an heterogeneous catalyzed process obtaining a reliable reaction rate expression is essential. From the few kinetic studies on 1-butanol dehydration, the majority have been carried out at experimental conditions in which butenes (resulting from 1-butanol intramolecular dehydration) are the main products.¹⁰ Olaofe and Yue¹⁰ studied the

1 kinetics of 1-butanol dehydration over three types of zeolites in gas phase in the temperature 2 range 473 – 573 K and 1-butanol pressures up to 60 kPa. At these conditions the main products 3 were both butenes and DNBE. For the dehydration of 1-butanol to di-n-butyl ether they 4 considered a power law kinetic model as well as three Hougen-Watson type kinetic expressions 5 assuming the surface reaction as the rate controlling step and that the adsorption of water and ether was negligible against the adsorption of 1-butanol. They concluded that empirical power 6 7 functions rate expressions satisfactorily correlated the reaction rate data of the dehydration of 8 1-butanol to DNBE and found an activation energy of 54 - 142 kJ/mol (depending on the used zeolite). Krampera and Beránek¹¹ studied the kinetics of individual reactions for the dehydration 9 10 of 1-butanol over alumina in gas phase at 433 K. For di-n-butyl ether formation they proposed a 11 LHHW mechanism where the irreversible surface reaction of two adsorbed molecules of 12 1-butanol was the rate limiting step and assuming the adsorption of water and ether negligible against the adsorption of 1-butanol. Sow et al.¹² studied the kinetics of 1-butanol dehydration to 13 DNBE in liquid phase (at 433, 453 and 473 K under autogenerated pressure) over three 14 15 sulfonated mesoporous silica and organosilica catalyst and a Y-zeolite. In their study they only considered a kinetic rate expression based on a mechanism where one molecule of 1-butanol 16 17 adsorbs on an active site, the irreversible surface reaction being the rate limiting step and 18 assuming the adsorption of alcohol and ether to be negligible against the adsorption of water, $r = k \cdot [DNBE] / (1 + K_{H,O}[H_2O])$. The values of the activation energies that they obtained ranged 19 20 between 95 - 97 kJ/mol.

 $20 \quad \text{between } 95 - 97 \text{ kJ/mol.}$

The main goal of this study was to perform a comprehensive kinetic analysis of DNBE
synthesis on the acidic resin Amberlyst 70 in the liquid phase at the temperature range of 413 –
473 K. Particular emphasis was placed on high water contents given its inhibitory effect.¹³⁻¹⁶

24

25 Experimental

26 Material

1 1-butanol (≥ 99.4 w/w % pure; ≤ 0.1 w/w % butyl ether; ≤ 0.1 w/w % water) and DNBE (≥
 2 99.0 w/w % pure; ≤ 0.05 w/w % water) supplied by Acros Organics were used without further
 3 purification. Deionised water (resistivity 18.2 mΩ·cm) obtained in our laboratory and N₂ (≥
 4 99.995 w/w %) supplied by Abelló Linde were also used.

The macroreticular thermostable resin Amberlyst-70 supplied by Rohm and Haas was used as the catalyst. Amberlyst-70 is a low cross-linked chlorinated and sulfonated copolymer of styrene-divinylbenzene (S-DVB), stable up to 463 K. Its acid capacity, determined following the procedure described by Fisher and Kunin¹⁷, was found to be 2.65 mol H⁺/kg. Table 1 gathers the main properties of Amberlyst 70.

10

11 Apparatus and analysis

Experiments were carried out in a 100 cm³ 316 stainless steel autoclave (Autoclave
 Engineers, M010SS, maximum temperature: 505 K; pressure range: 0 – 15 MPa).

The system was equipped with a pneumatic injection system to load the catalyst, a magnetic drive stirrer and a 400 W electrical furnace for heating. Temperature and stirring speed were measured by a thermocouple located inside the reactor and by a tachometer. Both operation variables were controlled to ± 1 K and ± 1 rpm respectively by an electronic control unit. One of the outlets of the reactor was connected directly to a liquid sampling valve, which injected 0.2 mm³ of pressurized liquid into a gas-liquid chromatograph equipped with a TCD detector (Agilent Technologies, 7820A). Analysis procedure is described in detail elsewhere.⁹

21

22 Procedure

Wet resin (as provided by the supplier) was dried at room temperature for 24 h prior to mechanical sieving. Afterwards, resin samples with bead size between 0.40 - 0.63 mm were dried at 383 K in an atmospheric oven during 3 h and then under vacuum (1 kPa) for 15 h. A previous work showed that after this drying treatment the residual water content of the resin was <3% (w/w).¹⁸ 70 mL of 1-butanol, or 1-butanol/water, or 1-butanol/DNBE were charged in the reactor and heated to the working temperature. The pressure was kept at 4 MPa with N₂ to ensure that the reaction medium was in liquid phase over the whole temperature range and the
stirring speed was set at the corresponding value (300-700 rpm). Once the corresponding
working temperature was reached (413-163K), the dried catalyst was injected by means of
pneumatic transport considering this time as the starting point of reaction. Liquid composition
was analyzed hourly during 7 h.

Reaction rates of DNBE formation were obtained from the function of the DNBE moles
produced vs. time (Equation 1). A rational function was used to describe the relationship
between n_{DNBE} and t.

9
$$r_{\text{DNBE}}(t) = \frac{l}{W_{\text{cat}}} \left(\frac{\text{dn}_{\text{DNBE}}}{\text{dt}} \right) \left[\frac{\text{mol}}{\text{h} \cdot \text{kg}_{\text{cat}}} \right]$$
 (1)

Measured reaction rate were accurate within \pm 5%

10

11

12 **Results and Discussion**

13 Preliminary experiments

14 In order to check that the overall observed reaction rates were not influenced by mass 15 transfer limitations or solid distribution effects, a set of preliminary experiments was conducted by changing the resin particle size, stirring speed and the catalyst loading of the reactor. Since 16 17 external mass transfer depends both on particle size and stirring speed, instead of three series of experiments in which, one by one, the effect of particle size, stirring speed and catalyst loading 18 was tested, a factorial design of experiments¹⁹ was carried out, since it allows to study the 19 simultaneous effect of the three factors (stirring speed, N; catalyst particle size, dp; mass of 20 21 loaded catalyst, W_{cat}). Each factor was studied at two levels, i.e. following a 2³ factorial design. 22 Taking into account the operation conditions in which the dehydration reactions of 1-pentanol and 1-octanol to linear ether over Amberlyst 70 were not influenced by mass transfer 23 limitations^{20,21}, the following range for the three factors was selected: (catalyst mass: 0.5-2 g; 24 25 stirring speed: 300-700 rpm; catalyst particle size: 0.4-0.8 mm). Table 2 shows the experimental matrix for the 2³ factorial design. Some of the eight formulations (denoted with an *) were 26 replicated and four additional runs (last 4 rows) were carried out at the central point of the 27

design (500 rpm, 1g of catalyst with particle size between 0.4-0.63 mm). The last column in
Table 2 shows the initial rate of DNBE formation obtained for each run. The order in which the
runs were carried out was randomized to avoid systematic errors. All tests were performed at 4
MPa and at the highest temperature of the range explored, which corresponds to the catalyst
maximum operating temperature (463 K).

As can be seen in Table 2, reaction rates measured in all the experiments are quite close;
most of them can be taken as the same within the limits of the experimental error. In order to
examine statistically the influence of the studied factors on the reaction rate, a linear regression
model (Equation 2) which considered as regressor variables the main effects (N, d_p, W_{cat}) as
well as the interaction effects (N·d_p; N·W_{cat}; d_p·W_{cat}; N·d_p·W_{cat}) was fitted to data of Table 2 by
the least squares method.

$$r^{0} = 150.93 + 1.235 \cdot (N) + 2.445 \cdot (W_{cat}) - 4.051 \cdot (d_{p}) - 0.472 \cdot (N \cdot W_{cat}) - 0.341 \cdot (N \cdot d_{p}) - 0.341 \cdot (N \cdot d_$$

13
$$2.271 \cdot (W_{cat} \cdot d_p) - 0.677 \cdot (N \cdot W_{cat} \cdot d_p)$$

12

To evaluate whether Equation 2 represented the experimental data satisfactorily from a statistical standpoint, a *Test for the lack of fit*²² was performed. By computing the variance due to pure error (s_{PE}^2) and the variance due to the lack of fit (s_{LOF}^2) it was possible to compare the test statistic $F_0 = s_{LOF}^2/s_{PE}^2 = 0.868$ with the critical value of the $F_{distribution} = 4.737$ to ascertain if both variances were statistically different. It can be seen that $F_0 < F_{distribution}$ for a probability of 0.95. Thus, Equation 2 represents satisfactorily reaction rate data.

(2)

To determine whether the regressor variables contributed significantly to the model a Test 20 for significance of regression²² was performed. The test procedure involves computing the 21 statistic F_0 as the ratio between the variance due to the regression, s_R^2 , and the variance due to 22 the experimental error, $s_{\scriptscriptstyle E}^2$, and compare this value with the critical value of the $F_{\scriptscriptstyle distribution}.$ From 23 the results of the test for significance it can be concluded that $F_0 = 2.608 < F_{distribution} = 3.293$ (for 24 25 a probability of 0.95). Thus, none of the regressor variables contributed significantly to Equation 2. As a result, reaction rate values can be considered the same in the whole range of 26 operation variables checked (N = 300 - 700 rpm, $d_p = 0.4 - 0.8$ mm and $W_{cat} = 0.5 - 2$ g). 27

1 Therefore, to carry out the kinetic experiments the following operation conditions were 2 selected: N = 500 rpm, $W_{cat} = 1$ g of Amberlyst-70 and $d_p = 0.4 - 0.63$ mm. 3 4 Modeling of kinetic data 5 The reaction rate models considered in this work are based on the Langmuir-Hinshelwood-Hougen-Watson (LHHW) and the Eley Rideal (ER) formalisms. These formalisms, as well as 6 7 the kinetic expressions derived from different rate limiting step (RLS) and quasi-steady states 8 assumptions are discussed next. 9 Mechanism 1: Langmuir-Hinshelwood-Hougen-Watson (LHHW) formalism. 10 In the LHHW mechanism two alcohol molecules, each one adsorbed on an adjacent active site, react to yield the ether. The elementary steps for this model are shown in the following 11 expressions, in which σ represents an active site and BuOH σ , DNBE σ and H₂O σ correspond, 12 13 respectively, to 1-butanol, di-n-butyl ether and water chemisorbed on an only active site. $BuOH + \sigma \xrightarrow{K_{BuOH}} BuOH\sigma$ 14 2 BuOH σ + n(σ) $\xleftarrow{K_s}$ DNBE σ + H₂O σ + n(σ) 15 $DNBE\sigma \xrightarrow{1/K_{DNBE}} DNBE + \sigma$ 16 $H_2O\sigma \xrightarrow{1/K_{H_2O}} H_2O + \sigma$ 17 18 Mechanism 2: Eley Rideal formalism where DNBE remains adsorbed (ER_{DNBE}) The ER formalism assumes that only one of the two reacting molecules of 1-butanol 19 adsorbs on the surface and reacts with other one directly from the bulk yielding DNBE and 20 water. The formed DNBE molecule remains adsorbed on the surface while water is immediately 21 22 released into solution: $BuOH + \sigma \xrightarrow{K_{BuOH}} BuOH\sigma$ 23 BuOH + BuOH σ + n(σ) $\xleftarrow{K_s}$ DNBE σ + H₂O + n(σ) 24 $DNBE\sigma \xrightarrow{1/K_{DNBE}} DNBE + \sigma$ 25

26

1 Mechanism 3: Eley Rideal formalism where water remains adsorbed (ER_{H2O})

As in mechanism 2, 1-butanol from solution reacts directly with 1-butanol adsorbed on the surface of the catalyst but, in this case, the ether is immediately released to the liquid phase and water remains adsorbed:

$$I + \sigma \xrightarrow{R_{BuOH}} BuOH\sigma$$

6 BuOH + BuOH σ + n(σ) $\xleftarrow{K_S}$ DNBE+ H₂O σ + n(σ)

7
$$H_2O\sigma \xleftarrow{I/K_{H_2O}} H_2O + \sigma$$

8 In the three mechanisms it was taken into account the possibility that *n* additional active
9 sites (with *n* = 0, 1 or 2) could participate in the surface reaction.

10 Each of the elementary steps that take part in the reaction mechanisms just described can 11 be considered as the rate limiting step. If the chemical reaction rate on the surface is considered 12 the RLS, it is assumed that adsorption of species is maintained in a quasi-equilibrium state all 13 the time. On the contrary, if the RLS is considered to be the adsorption of the reactant or the 14 desorption of a product, it is assumed that the chemical reaction between adsorbed species is in 15 quasi-equilibrium. Table 3 gathers the kinetic models derived from the three reaction 16 mechanisms depending on the elementary step that is considered as the RLS. \hat{k} is the forward rate constant for the surface reaction; k_i and K_i are, respectively, the adsorption rate constant and 17 18 the adsorption equilibrium constant of compound j; K_{eq} is the thermodynamic equilibrium constant which was experimentally determined in a previous work.²³ All the rate expressions of 19 20 Table 3 may be expressed as a combination of three terms, the kinetic, the driving potential and the adsorption term^{24,25}: 21

22
$$r_{\text{DNBE}} = \frac{\text{kinetic term} \cdot (\text{driving potential term})}{(\text{adsorption term})^{\text{m}}}$$
 (3)

When the surface reaction is considered the RLS, the kinetic term is the product of the surface reaction rate constant for the forward reaction and a power of the 1-butanol adsorption equilibrium constant which depends on the considered mechanism. If the adsorption of 1butanol or the desorption of one of the products is the RLS, the kinetic term is the rate constant of the rate limiting adsorption/desorption process. The driving potential term accounts, in all rate expressions, for how far the thermodynamic equilibrium is, and it must become zero when the equilibrium is reached. Finally, the adsorption term accounts for all the species that are adsorbed on surface sites. The exponent on the adsorption term for the cases where the surface reaction is considered the RLS is equal to the number of active sites participating in the surface reaction. When the adsorption/desorption of a single species is the RLS, the corresponding element in the adsorption term is modified according to the surface reaction involved.

8 Simplified kinetic models were derived from the general kinetic models of Table 3 by 9 assuming the amount of free active sites very low compared with the occupied ones (thus the 10 unity present in the adsorption term can be removed), and/or the adsorption of alcohol, ether 11 and/or water to be negligible. This way, 82 different kinetic models were obtained which have 12 been included in the Supplementary Data section.

All the models where fitted to reaction rate data by minimizing the sum of squared relative errors (SSRE, Equation 4) using the Levenberg-Marquardt algorithm^{26,27} which is implemented in Matlab. We consider the relative error to be a more meaningful measure^{28,29} than the sum of squared errors, SSE (SSE = $\sum (r_{exp} - r_{cal})^2$), given that the range of rate values is large ($r_{DNBE} \approx$ 2 - 135 mol/h·kg).

18
$$SSRE = \sum \left(\frac{r_{exp} - r_{cal}}{r_{exp}}\right)^2$$
(4)

19 The dependence of the kinetic parameters with the temperature was considered to follow 20 the Arrhenius law (Equation 5) for the rate constants (\hat{k} and k_j), and the Van't Hoff law 21 (Equation 6) for the adsorption equilibrium constants (K_j). Both expressions were 22 reparameterized in order to avoid strong binary correlation between parameters.³⁰ T_{ref} is defined 23 as the midpoint T value in the analyzed range of temperatures.

24
$$\hat{\mathbf{k}}_{,\mathbf{k}_{j}} = \mathbf{A} \exp\left[-\frac{\mathbf{E}_{A}}{\mathbf{R}}\left(\frac{1}{\mathbf{T}} - \frac{1}{\mathbf{T}_{ref}}\right)\right]$$
 (5)

1
$$K_{j} = \exp\left[\frac{\Delta S_{j}}{R} - \frac{\Delta H_{j}}{R}\left(\frac{1}{T} - \frac{1}{T_{ref}}\right)\right]$$
 (6)

2 The temperature dependence of the thermodynamic equilibrium constant was found to
3 be²³:

4 $K_{eq} = exp\left[\frac{37.0}{T} + 3.2\right]$ (7)

5 Whenever possible, rate and adsorption constants were grouped for mathematical fitting 6 purposes. Equations 8-11 show, by way of example, how the constants association was done for 7 the kinetic model LHHW-RLS2/1b (see Supplementary Data) which stemmed from the LHHW 8 formalism when the following assumptions were made: (1) the surface reaction was considered 9 the RLS; (2) the number of active center participating in the reaction was 3 and; (3) the amount 10 of free active sites was very low compared with the occupied ones.

11
$$r_{\text{DNBE}} = \frac{k^* \cdot \left(a_{\text{BuOH}}^2 - \frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}}}\right)}{\left(a_{\text{BuOH}} + K_1 \cdot a_{\text{DNBE}} + K_2 \cdot a_{\text{H}_2\text{O}}\right)^3}$$
(8)

12 With

13
$$k^* = \hat{k} \cdot \frac{K_{BuOH}^2}{K_{BuOH}^3} = \hat{k} \cdot K_{BuOH}^{-1}$$
 (9)

$$14 K_1 = \frac{K_{\text{DNBE}}}{K_{\text{BuOH}}} (10)$$

$$15 K_2 = \frac{K_{H_2O}}{K_{BuOH}} (11)$$

16

17 Experiments starting from pure 1-butanol

A series of experiments with pure 1-butanol was conducted in the temperature range 413 - 463 K. Each experiment was, at least, duplicated (being the relative error corresponding to DNBE formation rates lower than 5%). Figures 1a and b represent, respectively, 1-butanol conversion and selectivity to di-n-butyl ether as a function of the reaction time for all the temperatures tested. From Figure 1a it could be concluded that 1-butanol normalized conversion is strongly influenced by reaction temperature increasing from a value of 4% at 413 K to more than a tenfold (≈ 46%) at 463 K (after 7 h of experiment). However, it must be taken into account that the system is far away from the equilibrium position. In a previous work we found that the dehydration of 1-butanol to DNBE is a slightly exothermic reaction (almost athermic). Thus it is expected that, with time, the curves of conversion for all the tested temperatures tend to a very close value (not exactly the same value due to the existence of secondary reactions which are influenced by the temperature reaction).

8 Selectivity to DNBE also depends on the reaction temperature although in all cases was 9 higher than 90%. As it can be seen, after some time selectivity reaches a plateau. The time 10 needed to reach this plateau and the value to which the selectivity tends depends on the 11 operating temperature: a higher reaction temperature results in longer times to reach a constant 12 value (in experiments run at the higher temperatures, 443 - 463 K, selectivity was still moderately decreasing after 7 h) and lower selectivity to DNBE, other detected products being 13 butenes, 2-butanol and the branched ether 1-(1-methylpropoxy)butane (a detailed scheme of the 14 15 reaction network can be found elsewhere9). Nevertheless, for all the tested temperatures the catalyst is very selective to the linear ether. 16

Figure 1c shows the reaction rate of DNBE synthesis along the experiments as a function of temperature. As expected, the initial reaction rate is highly dependent on temperature doubling its value with each 10 K rise. However, reaction rate decreases along time (more sharply when the reaction temperature is high) and after 7 h the reaction rate for all the tested temperatures is very similar with values in the range of $2.3 - 11.1 \text{ mol/h} \cdot \text{kg}$. This decrease could be due to an inhibition effect caused by the reaction products (it is well known that water adsorbs strongly on acidic sites influencing the reaction rate¹³⁻¹⁶).

Given the important dissimilarity between the compounds presents in the medium, the system deviates from ideality. In order to take into account this non-ideality, the kinetic analysis was carried out as a function of activities instead of concentrations. The activity coefficients were estimated by the UNIFAC-Dortmund predictive method.³¹⁻³⁴

11

Figure 2 shows the dependence of the reaction rate as a function of activities of 1-butanol (a_{BuOH}), water (a_{H2O}) and di-n-butyl ether (a_{DNBE}). Due to the fact that a_{BuOH}, a_{H2O} and a_{DNBE} are not independent variables, it is difficult to analyze the influence that each activity has on the reaction rate. However, from Figure 2 it can be concluded that a decrease in a_{BuOH}, which is associated with an increase in a_{H2O} and a_{DNBE}, affects negatively the DNBE reaction rate for all the temperatures tested.

7 General (Table 3) and simplified models (see Supplementary Data) were fitted to 8 experimental data corresponding to runs starting from pure 1-butanol. Several kinetic models 9 with physicochemical meaning (positive activation energy, negative adsorption enthalpy and 10 negative adsorption entropy) fitted the experimental data satisfactorily. Models, fitted parameters, confidence intervals for a 95% probability, sum of squared relative errors and 11 12 goodness of the fit (R_{adi}^2) for the best kinetic models are gathered in Table 4. Among these 13 models, LHHW-RLS4/1b (Equation 13) and LHHW-RLS3/1b (Equation 14) present the lowest 14 sum of squared relative errors (SSRE) and the lowest parameters uncertainty Δ (calculated with 15 Equation 12, with ε_i being the uncertainty of parameter β_i and p de number of parameters in the 16 model). Both equations stem from a LHHW formalism in which the rate limiting step is 17 considered to be the desorption of one of the products (water and ether respectively) and assuming the amount of free active sites to be negligible in comparison with the other 18 adsorption terms. On the other hand, model LHHW-RLS2/1b (Equation 15) stems from a 19 20 LHHW formalism where the surface reaction is considered the rate limiting step. However, this 21 model presents higher SSRE and parameters uncertainties significantly high.

22
$$\Delta = \left[\sum_{i=1}^{p} \left(\frac{\varepsilon_{i}}{\beta_{i}}\right)^{2}\right]^{0.5} (12)$$

It must be pointed out that the concentration of alcohol, ether and water in the reaction medium are not independent variables, thus a_{BuOH}, a_{DNBE} and a_{H2O} are reciprocally dependent. Figure 3 shows the relation between water and DNBE activity. As it can be seen, the ratio a_{H2O}/a_{DNBE} is almost constant along the experiments for all the temperatures tested (except for

time = 0) with values ranging between 1.3 and 1.8, belonging the highest ratios to the highest 1 temperatures. This tendency is in accordance with the lower selectivity observed for higher 2 3 temperatures being water also produced through side-reactions. The significant high ratios observed at time = 0 h are probably due to residual water in the dry catalyst or in the reactant. 4 Due to the fact that the ratio a_{H2O}/a_{DNBE} is almost constant, models LHHW-RLS4/1b (Equation 5 13) and LHHW-RLS3/1b (Equation 14) are equivalent. Similarity between fitted parameters of 6 7 both models (Table 4) corroborates it. This fact makes impossible to differentiate, from this set 8 of experiments, which of the two mechanisms prevails.

9 Distribution of residual of fitted models gathered in Table 4 must also be taken into 10 account. As it can be seen in Figure 4a the model fits the experimental data satisfactorily. 11 However, residuals do not show a random distribution. From Figure 4b it can be concluded that 12 residuals corresponding to experiments performed at 463 K account significantly in the total 13 sum of residuals. Data shown in Figure 4 corresponds to model LHHW-RLS4/1b (Equation 13) but for the rest of models gathered in Table 4 the trends are very similar. Two circumstances 14 15 may be the cause of the important difference observed between the models fitting to data corresponding to 463 K runs and to data corresponding to the rest of temperatures: (1) a 16 17 temperature increase may lead to a change of the rate limiting step, thus a change of the kinetic 18 model and/or (2) the considerable amount of water produced in experiments carried out at high 19 temperatures (at 463 K the amount of water can reach up to 0.25 molar fraction) play an 20 important role on the catalytic reaction.

21

22 Experiments starting from 1-butanol/water and 1-butanol/DNBE mixtures.

To stress the effect of reaction products on the reaction rate and to break the constancy of the ratio a_{H2O}/a_{DNBE} a set of experiments starting from mixtures of 1-butanol/water and 1butanol/DNBE was performed at 413, 433 and 453 K. Figure 5 shows the effect of water and DNBE on the initial reaction rate as a function of the initial amount of water and DNBE in the mixture (% w/w). In Figure 5a it can be seen that the initial reaction rate is highly sensitive to water content decreasing as the amount of water in the initial mixture increases. This trend is in good agreement with the inhibitor character attributed to water. On the other hand, Figure 5b
 indicates that the effect of DNBE on the initial reaction rate is not remarkable suggesting that
 the adsorption of the ether may be negligible.

4 Besides reducing the initial reaction rate of DNBE synthesis, water also affects the catalyst selectivity. As it can be seen in Figure 6, mixtures with higher initial amount of water present, 5 6 after 7 hours of experiment, lower selectivity to DNBE. The drop in DNBE selectivity is due to an increase in the formation of olefins and the secondary alcohol, however, selectivity to the 7 8 branched ether, 1-(1-methylpropoxy) butane, is not affected. Water molecules adsorb 9 preferentially on the active sites, blocking them. As the number of active sites blocked by water 10 increases, the probability of finding two or more molecules of 1-butanol adsorbed on the 11 catalyst surface close enough decreases reducing the extent of the bimolecular dehydration of 1-12 butanol and enhancing the intramolecular dehydration to yield the olefin 1-butene. Data of 0 13 corresponds to experiments performed at 453 K. For lower temperatures (413 and 433 K) the amount of water in the initial mixture does not have a significant effect on the products 14 15 distribution which may be due to the fact that the intramolecular dehydration of 1-butanol to 1-16 butene is enhanced at high temperatures. The presence of DNBE in the starting mixture does not 17 have any significant effect on the product distribution either.

18 General (Table 3) and simplified models (see Supplementary Data) were fitted to data 19 corresponding to experiments starting from mixtures of 1-butanol/water and 1-butanol/DNBE. 20 Data of experiments performed with pure 1-butanol were not included in this analysis with the 21 aim of facilitate differentiation among models that are equivalent when the relationship between 22 activities is almost constant. Best kinetic models are gathered in Table 5. As it can be seen, the 23 fact of breaking the constancy of a_{H2O}/a_{DNBE} makes possible to differentiate between models that 24 in the previous set of experiments (pure 1-butanol) were equivalent. In contrast to results 25 gathered in Table 4, the model which stems from a LHHW formalism where the desorption of 26 water is considered de rate limiting step and assuming the amount of free active sites negligible 27 (LHHW-RLS4/1b, see Equation 13) does not fit satisfactorily experimental data (with SSRE 28 higher than 20). Nevertheless, the LHHW model where the rate limiting steps is considered to

1 be the desorption of DNBE (LHHW-RLS3/1b, see Equation 14) still does. LHHW models 2 obtained assuming that the surface reaction is the rate limiting step, LHHW-RLS2/1b 3 (Equation 15) (considering the amount of free active sites negligible) and LHHW-RLS2/3b 4 (Equation 16) (considering negligible both the amount of free active sites and the adsorption of DNBE) with n = 0, 1 and 2 also fit adequately data (except for LHHW-RLS2/3b with n = 25 where the SSRE is 2.36) however, uncertainty of parameters corresponding to model LHHW-6 7 RLS2/1b with n = 0 and 1 is significant. It should be noted that all these models (Table 5) 8 include in their denominator the term of water adsorption.

9 Figure 7 shows the comparison between the calculated and experimental reaction rates, as 10 well as the residual distribution, for the two models of Table 5 which present the lowest SSRE (LHHW-RLS3/1b and LHHW-RLS2/1b with n = 2). As it can be seen, the model LHHW-11 12 RLS3/1b (Figures 7a and c) fits the experimental data satisfactorily with a random distribution 13 of residuals. However, in Figure 7b it can be observed that, at 453 K, model LHHW-RLS2/1b with n = 2 overestimates low and high values of reaction rates and, on the other hand, 14 15 underestimates medium values of reaction rates. Consequently, the residuals do not shown a 16 completely random distribution (Figure 7d).

Apparent activation energies computed by models LHHW-RLS3/1b and LHHW-RLS2/1b from experiments starting from mixtures of 1-butanol/water and 1-butanol/DNBE (Table 5) are slightly higher than values computed by the same model but from experiments starting from pure 1-butanol (Table 4). This fact is in agreement with the inhibiting effect attributed to water.¹³⁻¹⁶ In the next section, general and simplified kinetic models where modified in order to directly introduce the inhibiting effect of water.

23

24 Modified kinetic models

Several authors have reported the strong inhibition effect of water in reactions carried out over ion exchange resins¹³⁻¹⁶. In those works, water is considered to adsorb preferentially on the sulfonic groups, blocking the adsorption of reactants and thus, suppressing the catalytic reaction. The common approach to model the water inhibition effect is to modify the rate 1 constant in such a way that only the fraction of available active sites (not blocked by water 2 molecules, $1 - \theta_{H2O}$) are taken into account. The fraction of acid sites blocked by water molecules 3 (θ_{H2O}) can be expressed by an adsorption isotherm. In Table 6 three correction factors derived 4 from Langmuir (Equations 18 and 19) and Freundlich (Equation 17) adsorption isotherms are 5 shown. In these expressions *m* is the total number of active sites taking part in the rate-limiting 6 step.

7 Three new sets of models were obtained by adding the three correction factors gathered in
8 Table 6 to both the general kinetic models (Table 3) and the simplified kinetic models
9 (Supplementary Data section). In all the cases the variation of K_w with temperature was
10 supposed to be:

11
$$K_{w} = \exp\left[K_{w_{1}} - K_{w_{2}}\left(\frac{1}{T} - \frac{1}{T_{ref}}\right)\right]$$
 (20)

Modified models were fitted to experimental data. The fact of adding the correction factors defined by Equations 18 and 19 did not improve the fittings. However, the correction factor derived from the Freundlich adsorption isotherm (Equation 17) provides important improvements.

For experiments starting from pure 1-butanol, modified models (including the Freundlich 16 17 correction factor) that best fit rate date are the same as those obtained when the correction factor 18 was not included (Table 4) but eliminating the term of water adsorption from the denominator 19 of Equations 14 and 15 (or, given the equivalence between models due to the constancy of the 20 ratio a_{H2O}/a_{DNBE}, the term of DNBE adsorption in the denominator of Equations 13 and 15). 21 Models with the Freundlich correction factor present lower SSRE (mainly due to an 22 improvement of the fitting to data corresponding to experiments carried out at 463 K); however, 23 the uncertainty of the fitted parameter is higher.

When models including the Freundlich correction factor were fitted to rate data corresponding to experiments starting from mixtures 1-butanol/products, in contrast to the results obtained in the fitting of the models without correction factor (Table 5), modified models that do not include a water adsorption term in the denominator (LHHW-RLS2/2b, Equation 21, and LHHW-RLS4/2b, Equation 22) are the ones that best fit the experimental data (see Table 7). Model LHHW-RLS4/2b stems from a LHHW formalism where the desorption of water is considered the RLS and assuming negligible the amount of free active sites and the adsorption of DNBE. Model LHHW-RLS2/2b stems from a LHHW formalism where the RLS is the surface reaction and considering the amount of free active sites and the adsorption of water negligible. Furthermore, model LHHW-RLS2/1b also has very low values of SSRE but the uncertainty of the parameters is higher.

8 From the results gathered in Table 5 and Table 7 it can be concluded that water effect must 9 be included in the model either by means of the Freundlich correction factor (i.e., considering 10 that water molecules block the active sites reducing the number of available ones), or in the adsorption term. Nevertheless, including the Freundlich correction factor gives better results 11 because not only reduces the SSRE but also achieve a better residual distribution (models in 12 13 which the Freundlich correction factor is not included show higher residuals in experiments performed at higher temperatures). Taking into account both approach simultaneously does not 14 15 improve the fitting and besides introduces more parameters to the models.

These conclusions agree with the results obtained in the set of experiments starting from pure 1-butanol (both, when the Freundlich factor is included and when is not). Thus, we can conclude that the models that best fit the experimental data (for the whole range of water activities and temperatures explored) are:

20
$$r = \frac{\hat{k} \cdot \frac{K_{BuOH}^{2}}{K_{BuOH}^{2+n}} \left(a_{BuOH}^{2} - \frac{a_{DNBE} \cdot a_{H_{2}O}}{K_{eq}} \right)}{\left(a_{BuOH} + \frac{K_{DNBE}}{K_{BuOH}} \cdot a_{DNBE} \right)^{2+n}} \left(1 - K_{w} a_{H_{2}O}^{1/\alpha} \right)$$
(21)

21
$$r = \frac{\frac{k_{H_2O}}{K_{H_2O}} \left(K_{eq} \frac{a_{BuOH}^2}{a_{DNBE}} - a_{H_2O} \right)}{\frac{K_{BuOH}}{K_{H_2O}} \cdot a_{BuOH} + K_{eq} \frac{a_{BuOH}^2}{a_{DNBE}}} \left(1 - K_w a_{H_2O}^{1/\alpha} \right)$$
(22)

22 With $\alpha = K_{\alpha} / T$

17

1 Equation 21 stems from a LHHW formalism in which two adjacent adsorbed molecules of 2 1-butanol (from the results it is difficult to distinguish the number of additional active sites - 0, 3 1 or 2 - that participate in the surface reaction) react to yield ether and water, being the surface 4 reaction the rate limiting step. The formed water remains in the catalyst surface blocking the 5 active centers. Equation 21 assumes that the number of unoccupied sites is not significant compared with occupied ones and that the adsorption of water is negligible. Equation 22 stems 6 7 from a mechanism in which the rate limiting step is the desorption of water and where the 8 adsorption of DNBE is comparatively negligible (which agrees with the fact that adding DNBE 9 to the reaction medium does not influence the reaction rate, Figure 5) and the number of 10 unoccupied sites is not significant. From Equation 22 it is not possible to discern if the mechanism corresponds to a LHHW formalism or to a ER-H₂O formalism as both lead to the 11 same form of the rate equation (see in the Supplementary Data Section the models LHHW-12 13 RLS4/2b and ER_{H20}-RLS3/1b).

14

15 General kinetic model

With the aim of finding a set of parameters that represent a wider range of activities,
equations 21 and 22 were fitted to all the experimental data simultaneously. Results are gathered
in Table 8.

In Figure 8a and b the reaction rate of DNBE formation estimated by models LHHWRLS2/2b (Equation 21) and LHHW-RLS4/2b (Equation 22) including the Freundlich correction
factor is compared with the experimental one. As it can be seen, both fittings are very similar.
Figure 8c and d show the residual distribution for the two models.

Figure 9 plots the values of the Freundlich correction factor, $1-K_w a_{H_2O}^{1/\alpha}$, as used in models LHHW-RLS2/2b and LHHW-RLS4/2b (Table 8), versus a_{H_2O} for all the temperatures tested. In both models the correction factor decreases on increasing a_{H_2O} (linearly in model LHHW-RLS2/2b and sharply for low values of water activity and more moderately for higher water activities in model LHHW-RLS4/2b) and seems to be independent on the operating temperature (which explains the high uncertainty associated with the parameter K_{w2}, see Table 8, indicating
 little sensitivity to this parameter in the fit).

3 Similar values of apparent activation energies (Table 8) were found for all the models (≈ 122 ± 2 kJ/mol). This value is slightly higher than those reported for the dehydration reactions 4 over Amberlyst-70 of 1-pentanol to di-n-pentyl ether²⁰ (114.0±0.1 kJ/mol) and 1-octanol to di-5 n-octyl ether²¹ (110±5 kJ/mol) and very similar to that reported for the dehydration of 1-hexanol 6 to di-n-hexyl ether³⁵ (121 \pm 3 kJ/mol). Regarding the molar adsorption enthalpy differences, it is 7 8 possible to see that adsorption of 1-butanol is stronger (more exothermic) than that of DNBE 9 (models LHHW-RLS2/2b) but weaker than that of water (model LHHW-RLS4/2b). For model 10 LHHW-RLS2/2b, the positive value of the difference between the free energy change for DNBE 11 adsorption (ΔG_{DNBE}) and the free energy change for 1-butanol adsorption (ΔG_{BuOH}), calculated as $(\Delta G_{\text{DNBE}} - \Delta G_{\text{BuOH}}) = (\Delta H_{\text{DNBE}} - \Delta H_{\text{BuOH}}) - T(\Delta S_{\text{DNBE}} - \Delta S_{\text{BuOH}})$, indicates that ΔG_{BuOH} is more 12 negative than ΔG_{DNBE} , being the 1-butanol adsorption a more favored process than DNBE 13 adsorption. In a similar way, for model LHHW-RLS4/2b, the positive value of 14 $(\Delta G_{BuOH} - \Delta G_{H,O})$ indicates that the adsorption of water over the catalyst is a more favored 15 16 process than 1-butanol adsorption. This trend is in agreement with the polarity of the compounds and the high water affinity of the resin. 17

18

19 Conclusions

20 The reaction rate of 1-butanol dehydration to di-n-butyl ether was found to be very 21 sensitive to temperature and to water presence. Two kinetic models are proposed to explain the 22 dehydration of 1-butanol to di-n-butyl ether over Amberlyst 70. One of them stems from a 23 LHHW formalism in which two adjacent adsorbed molecules of 1-butanol react to yield ether 24 and water, being the reversible surface reaction the rate limiting step and where the adsorption 25 of water is negligible. The other one stems from a mechanism in which the rate limiting step is the desorption of water and where the adsorption of DNBE is negligible. The two models 26 27 present several characteristics in common: (1) the strong inhibiting effect of water is taken into

1	account by means	of a correction factor derived from a Freundlich adsorption isotherm (water is				
2	not included in the adsorption term); (2) the number of free active sites is found to be negligible					
3	compared to the occupied ones; (3) both models present similar values of SSRE and apparent					
4	activation energies	$s (122 \pm 2 \text{ kJ/mol}).$				
5						
6						
7	Notation					
8	А	Preexponential factor				
9	a_j	Activity of compound <i>j</i>				
10	ABE	Acetone-Butanol-Ethanol				
11	BuOH	1-Butanol				
12	DNBE	Di-n-butyl ether				
13	d_p	Catalyst particle size				
14	EA	Activation Energy				
15	ER	Eley-Rideal				
16	ER _{DNBE}	Eley Rideal formalism where DNBE remains adsorbed				
17	ER _{H2O}	Eley Rideal formalism where H ₂ O remains adsorbed				
18	F ₀	Test estatistic				
19	$F_{\text{distribution}}$	Value of the continuous probability distribution				
20	Κα	Freundlich parameter				
21	\hat{k}	Forward rate constant for the surface reaction				
22	K _{eq}	Equilibrium constant of DNBE formation reaction				
23	\mathbf{k}_{j}	Adsorption rate constant of compound j				
24	\mathbf{K}_{j}	Adsorption equilibrium constant of compound j				
25	Ks	Surface reaction equilibrium constant				
26	\mathbf{k}_{w}	Water correction factor				
27	k_{w1}	First parameter of the water correction factor				
28	k _{w2}	Second parameter of the water correction factor				

1	LHHW	Langmuir-Hinselwood- Hougen-Watson
2	m	Number of total active sites participating in the surface reaction
3	Ν	Stirring speed
4	n	Number of additional active sites participating in the surface reaction
5	n _{DNBE}	Moles of DNBE
6	R	Ideal gas constant
7	R_{adj}^2	Goodness of the fit
8	r_{cal}	Estimated reaction rate
9	r _{exp}	Experimental reaction rate
10	RLS	Rate limiting step
11	r _{DNBE}	Reaction rate of DNBE formation
12	$r_{ m DNBE}^0$	Initial reaction rate of DNBE formation
13	S-DVB	Styrene-divinylbenzene
14	s_E^2	Variance due to the experimental error
15	s_{LOF}^2	Variance due to the lack of fit
16	$s_{ m PE}^2$	Variance due to pure error
17	s_R^2	Variance due to the regression
18	SSRE	Sum of squared relative errors
19	t	Time
20	Т	Temperature
21	$T_{\it ref}$	Midpoint T value of the analyzed range of temperatures
22	TCD	Thermal conductivity detector
23	W _{cat}	Mass of loaded catalyst
24	X_{BuOH}	1-Butanol conversion
25	Greek symbols	
26	α	Freundlich constant
27	β_i	Parameter <i>i</i>

1	ε _i	Uncertainty of parameter <i>i</i>
2	Δ	Parameters uncertainty
3	ΔG_j	Adsorption free energy of compound <i>j</i>
4	ΔH_j	Adsorption enthalpy of compound <i>j</i>
5	ΔS_j	Adsorption entropy of compound j
6	$\theta_{\rm H2O}$	Fraction of acid sites blocked by water molecules
7	σ	Active site
8		

1 References

1. Mascal M. Chemicals from biobutanol: technologies and markets. *Biofuel Bioprod Bioref*. 2012;6:483-493.

2. Harvey BG, Meylemans HA. The role of butanol in the development of sustainable fuel technologies. *J Chem Technol Biotechnol*. 2010;86:2–9.

3. Cai L, Sudholt A, Lee DJ, Egolfopoulos FN, Pitsch H, Westbrook CK, Sarathy SM. Chemical kinetic study of a novel lignocellulosic biofuel: di-n-butyl ether oxidation in a laminar flow reactor and flames. *Combus Flame*. 2014;161:798–809.

4. Cascone R. Biobutanol – A replacement for bioethanol? *Chem Eng Pro.* 2008;104(8):S4 – S9.

5. Qureshi N, Ezeji TC. Butanol, 'a superior biofuel' production from agricultural residues (renewable biomass): recent progress in technology. *Biofuels, Bioprod Bioref.* 2008;2:319-330.

6. European biofuels technology platform. http://www.biofuelstp.eu/butanol.html (accessed April 2015)

7. Starkey LS. *Introduction to strategies for organic synthesis* (2nd edition). New Jersey: John Wiley & Sons, Inc., 2012.

8. Sheldon RA, van Bekkum H. *Fine Chemical through Heterogeneous Catalysis*. Weinheim (Germany):Wiley-VCH, 2001.

9. Pérez MA, Bringué R, Iborra M, Tejero J, Cunill F. Ion exchange resins as catalysts for the liquid-phase dehydration of 1-butanol to di-n-butyl ether. *Appl Catal, A.* 2014;482:38–48.

10. Olaofe O, Yue PL, Kinetics of dehydration of 1-butanol over zeolites. *Collect Czech Chem Commun.* 1985;501:1784-1800.

11. Krampera F, Beránek L. Kinetics of individual reactions in reaction network 1-butanol-di-(1-butyl) ether-butenes-water on alumina. *Collect Czech Chem Commun*.1986;51:774-785. 12. Sow B, Hamoudi S, Zahedi-Niaki MH, Kaliaguine S. 1-Butanol etherification over sulfonated mesostructured silica and organo-silica. *Microporous Mesoporous Mater*. 2005;79:129–136

Gates BC, Rodriguez W. General and specific acid catalysis in sulfonic acid resins. *J Catal*.
 1973;31:27-31.

14. du Toit E, Nicol W. The rate inhibiting effect of water as a product on reactions catalyzed by cation exchange resins: formation of mesityl oxide from acetone as case study. *App Catal, A*. 2004;277:219-225.

15. Limbeck U, Altwicker C, Kunz U, Hoffmann U. Rate expression for THF synthesis on acidic ion exchange resin. *Chem Eng Sci.* 2001;56:2171-2178.

16. Yang BL, Maeda M, Goto S. Kinetics of liquid phase synthesis of tert-amyl methyl ether from tert-amyl alcohol and methanol catalyzed by ion exchange resin. *J Chem Kinet*. 1997;30:137-143.

17. Fisher S, Kunin R. Routine Exchange Capacity Determinations of Ion Exchange Resins. J Anal Chem. 1955;27:1191-1194.

18. Guilera J, Bringué R, Ramírez E, Iborra M, Tejero J. Synthesis of ethyl octyl ether from diethyl carbonate and 1-octanol over solid catalysts. A screening study. *Appl Catal, A*. 2012;413–414:21–29.

19. Box GEP, Hunter JS, Hunter WH. Statistics for experimenters. *Design, Innovation and Discovery* (2nd edition). New Jersey: John Wiley & Sons Inc., 2005.

20. Bringué R, Ramírez E, Fité C, Iborra M, Tejero J. Kinetics of 1-pentanol etherification without water removal. *Ind Eng Chem Res.* 2011;50:7911-7919.

21. Casas C. Synthesis of C_{10} - C_{16} linear symmetrical ethers from n-alcohols over heterogeneous acid catalysts. PhD Thesis. University of Barcelona, 2013.

22. Montgomery DC. *Fitting regression models*. *Design and Analysis of Experiments* (5th edition). John Wiley & Sons Inc., 2001.

23. Pérez-Maciá MA, Bringué R, Iborra M, Tejero J, Cunill F. Thermodynamic equilibrium for the dehydration of 1-butanol to di-n-butyl ether. *Chem Eng Res Des*. 2015;102:186–195.

24. Hill CG Jr. *Elements of heterogeneous catalysis. An introduction to chemical engineering kinetics & reaction design.* John Wiley & Sons, Inc., 1977.

25. Yang KH, Hougen OA. Determination of mechanisms of catalyzed gaseous reactions. *Chem Eng Prog.* 1950;46 (3):146-157.

26. Levenberg K. A Method for the Solution of Certain Problems in Least Squares. *Quart Appl Math.* 1944;2:64–168.

27. Marquardt D. An Algorithm for Least-Squares Estimation of Nonlinear Parameters. *SIAM J Appl Math.* 1963;11:431–441.

28. Park H, Stefanski LA. Relative-error prediction. Statist Probab Lett. 1998;40:227-236.

29. Tofallis C. Least Squares Percentage Regression. J Mod App Stat Meth. 2008;7 (2):526-534.

30. Kittrell JR. Mathematical modeling of chemical reactions. Adv Chem Eng. 1970;8:97–183.

31. Weidlicht U, Gmehling J. A modified UNIFAC model. 1. Prediction of VLE, hE, and $\gamma \infty$. *Ind Eng Chem Res.* 1987;26 (7):1372-1381.

32. Gmehling J, Li J, Schiller M. A modified UNIFAC model. 2. Present parameter matrix and results for different thermodynamic properties. *Ind Eng Chem Res.* 1993;32:178-193.

33. Gmehling J, Lohmann J, Jakob A, Li J, Joh R. A modified UNIFAC (Dortmund) model. 3. Revision and extension. *Ind Eng Chem Res.* 1998;37:4876-4882.

34. Jakob A, Grensemann H, Lohmann J, Gmehling J. Further development of modified UNIFAC (Dortmund): revision and extension 5. *Ind Eng Chem Res.* 2006;45:7924-7933.

35. Bringué R, Ramírez E, Iborra M, Tejero J, Cunill F. Kinetics of 1-hexanol etherification on Amberlyst 70. *Chem Eng J*. 2014;246:71–78.

CAPTIONS TO FIGURES

Figure 1. (a) 1-butanol conversion, (b) selectivity to DNBE and (c) reaction rate of DNBE synthesis as a function of temperature: (**•**) 413 K; (\circ) 423 K; (\diamond) 433 K; (Δ) 443 K; (\bullet) 453 K; (\Box) 463 K. Experiments starting from pure 1-butanol, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm. The error bars indicate the confidence interval at a 95% probability level. Most error bars are smaller than markers.

Figure 2. Reaction rate of DNBE synthesis as a function of (a) 1-butanol activity; (b) water activity; (c) DNBE activity. (**n**) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Experiments starting from pure 1-butanol, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm. **Figure 3.** Evolution of the ratio a_{H20}/a_{DNBE} with time for experiments starting from pure 1-butanol. (**n**) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Experiments starting from pure 1-butanol. (**n**) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Experiments starting from pure 1-butanol. (**n**) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Experiments starting from pure 1-butanol, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm.

Figure 4. (a) Calculated reaction rates by model LHHW-RLS4/1b (Equation 13) versus experimental rates; (b) residuals distribution. (**•**) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Experiments starting from pure 1-butanol, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm.

Figure 5. Influence of (a) water and (b) DNBE on the initial reaction rate of DNBE formation. (**•**) 413 K, (**•**) 433 K, (**•**) 453 K, 1 g of catalyst, $d_p = 0.4 - 0.63$ mm, 4 MPa, 500 rpm.

Figure 6. Selectivity to products after 7 h reaction as a function of initial water content. T = 463 K, 1 g of catalyst, $d_p = 0.4 - 0.63$ mm, 4 MPa, 500 rpm. (**•**) DNBE, (\circ) 1-butene, (\blacklozenge) 2-butanol,

(\blacktriangle) cis-2-butene, (\bullet) trans-2-butene, (\Box) 1-(1-methylpropoxy) butane.

Figure 7. Calculated reaction rates by models (a) LHHW-RLS3/1b (Equation 14) and (b) LHHW-RLS2/1b with n = 2 (Equation 15) versus experimental rates; residuals distribution for models (c) LHHW-RLS3/1b and (d) LHHW-RLS2/1b with n = 2. (**n**) 413 K, (**•**) 433 K, (\circ) 453 K. Experiments starting from mixtures 1-butanol/water and 1-butanol/DNBE, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm. **Figure 8.** Calculated reaction rates by the *modified* models (a) LHHW-RLS2/2b (Equation 21) and (b) LHHW-RLS4/2b (Equation 22) versus experimental rates; residuals distribution for models LHHW-RLS4/2b (c) and LHHW-RLS2/2b (d). (\blacksquare) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Rate data corresponding to all the experiments, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm.

Figure 9. Freundlich factor corresponding to models LHHW-RLS2/2b (a) and LHHW-RLS4/2b (b) vs. a_{H2O} at different temperatures. (**•**) 413 K, (\circ) 423 K, (\bullet) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. All the experiments, 1 g of catalyst, $d_p = 0.4 - 0.63$ mm, 4 MPa, 500 rpm.

Catalyst	Amberlyst 70				
Structure	Macroreticular				
Divinylbenzene (%)	7-8				
Chlorinated	Yes				
Skeletal density ^a (kg/m ³)	1514				
Sulfonation type	Monosulfonated				
Acidity ^b (mol H ⁺ /kg)	2.65				
$T_{max}(K)$	463				
In Dry State					
Mean particle diameter ^c , d_p (mm)	0.55				
Surface area ^d (m ² /g)	0.02				
In Water Swollen S	tate				
d_p^c (mm)	0.78				
Surface area ^e (m^2/g)	176				
In 1-Butanol Swollen State					
d_p^c (mm)	0.73				

Table 1. Properties of Amberlyst 70.

^a Skeletal density measured by Helium displacement.

^b Titration against standard base following the procedure described by Fisher and Kunin.¹⁷

^c Determined by laser diffraction.

^d BET (Brunauer-Emmet-Teller) surface area.

^e Surface area determined from Inverse steric exclusion chromatography (ISEC) technique.

Factors				led Fac	tors	* ⁰ [mo]/b.ka]
N [rpm]	W _{cat.} [g]	d _p [mm]	A	B	С	r [moi/n·kg]
300	0.504	< 0.4	-1	-1.0	-1	147.7
700	0.502	< 0.4	1	-1.0	-1	150.4
300	2.067	< 0.4	-1	1.1	-1	163.6
300*	2.044	< 0.4	-1	1.1	-1	152.2
700	2.018	< 0.4	1	1.0	-1	161.0
300	0.53	0.63-0.8	-1	-1.0	1	142.2
300*	0.516	0.63-0.8	-1	-1.0	1	145.9
700	0.505	0.63-0.8	1	-1.0	1	147.6
300	2.023	0.63-0.8	-1	1.0	1	147.7
300*	2.024	0.63-0.8	-1	1.0	1	146.3
700	2.028	0.63-0.8	1	1.0	1	149.2
700^*	2.034	0.63-0.8	1	1.0	1	149.7
500 ^a	1.012	0.4-0.63	0	-0.3	0	155.2
500 ^a	1.011	0.4-0.63	0	-0.3	0	152.5
500 ^a	1.022	0.4-0.63	0	-0.3	0	153.8
500 ^a	1.001	0.4-0.63	0	-0.3	0	146.9

Table 2. Experimental design used to determine the optimum operational conditions.

^a From the four central point replicates an initial reaction rate mean value of 152.1 mol/h·kg (standard deviation = 3.7 mol/h·kg) can be obtained.

Table 3 . Kinetic models with <i>n</i> additional active centers participating in the surface reaction ranging from 0 to 2

	Reaction Mechanisms					
RLS	LHHW	ER with DNBE adsorption	ER with H ₂ O adsorption			
	LHHW-RLS1	ER _{DNBE} -RLS1	ER _{H20} -RLS1			
1-butanol adsorption	$r_{\text{DNBE}} = \frac{k_{\text{BuOH}} \left(a_{\text{BuOH}} - \left(\frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}}} \right)^{0.5} \right)}{1 + K_{\text{BuOH}} \left(\frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}}} \right)^{0.5} + K_{\text{DNBE}} \cdot a_{\text{DNBE}} + K_{\text{H}_2\text{O}} \cdot a_{\text{H}_2\text{O}}}$	$r_{\text{DNBE}} = \frac{k_{\text{BuOH}} \left(a_{\text{BuOH}} - \frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}} \cdot a_{\text{BuOH}}} \right)}{1 + K_{\text{BuOH}} \left(\frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}} \cdot a_{\text{BuOH}}} \right) + K_{\text{DNBE}} \cdot a_{\text{DNBE}}}$	$\mathbf{r}_{\text{DNBE}} = \frac{\mathbf{k}_{\text{BuOH}} \left(\mathbf{a}_{\text{BuOH}} - \frac{\mathbf{a}_{\text{DNBE}} \cdot \mathbf{a}_{\text{H}_{2}\text{O}}}{\mathbf{K}_{\text{eq}} \cdot \mathbf{a}_{\text{BuOH}}} \right)}{1 + \mathbf{K}_{\text{BuOH}} \left(\frac{\mathbf{a}_{\text{DNBE}} \cdot \mathbf{a}_{\text{H}_{2}\text{O}}}{\mathbf{K}_{\text{eq}} \cdot \mathbf{a}_{\text{BuOH}}} \right) + \mathbf{K}_{\text{H}_{2}\text{O}} \cdot \mathbf{a}_{\text{H}_{2}\text{O}}}$			
	LHHW-RLS2	ER _{DNBE} -RLS2	ER _{H20} -RLS2			
RLS 1-butanol adsorption Surface reaction DNBE desorption H ₂ O desorption	$r_{\text{DNBE}} = \frac{\hat{k} \cdot K_{\text{BuOH}}^2 \left(a_{\text{BuOH}}^2 - \frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}}} \right)}{\left(1 + K_{\text{BuOH}} \cdot a_{\text{BuOH}} + K_{\text{DNBE}} \cdot a_{\text{DNBE}} + K_{\text{H}_2\text{O}} \cdot a_{\text{H}_2\text{O}} \right)^{2+n}}$	$r_{\text{DNBE}} = \frac{\hat{k} \cdot K_{\text{BuOH}} \left(a_{\text{BuOH}}^2 - \frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}}} \right)}{\left(1 + K_{\text{BuOH}} \cdot a_{\text{BuOH}} + K_{\text{DNBE}} \cdot a_{\text{DNBE}} \right)^{l+n}}$	$r_{\text{DNBE}} = \frac{\hat{k} \cdot K_{\text{BuOH}} \left(a_{\text{BuOH}}^2 - \frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}}} \right)}{\left(1 + K_{\text{BuOH}} \cdot a_{\text{BuOH}} + K_{\text{H}_2\text{O}} \cdot a_{\text{H}_2\text{O}} \right)^{l+n}}$			
	LHHW-RLS3	ER _{DNBE} -RLS3				
DNBE desorption	$r_{\text{DNBE}} = \frac{k_{\text{DNBE}} \left(K_{\text{eq}} \frac{a_{\text{BuOH}}^2}{a_{\text{H}_2\text{O}}} - a_{\text{DNBE}} \right)}{1 + K_{\text{BuOH}} \cdot a_{\text{BuOH}} + K_{\text{DNBE}} \cdot \left(K_{\text{eq}} \frac{a_{\text{BuOH}}^2}{a_{\text{H}_2\text{O}}} \right) + K_{\text{H}_2\text{O}} \cdot a_{\text{H}_2\text{O}}}$	$\mathbf{r}_{\text{DNBE}} = \frac{\mathbf{k}_{\text{DNBE}} \left(\mathbf{K}_{\text{eq}} \frac{\mathbf{a}_{\text{BuOH}}^2}{\mathbf{a}_{\text{H}_2\text{O}}} - \mathbf{a}_{\text{DNBE}} \right)}{1 + \mathbf{K}_{\text{BuOH}} \cdot \mathbf{a}_{\text{BuOH}} + \mathbf{K}_{\text{DNBE}} \cdot \left(\mathbf{K}_{\text{eq}} \frac{\mathbf{a}_{\text{BuOH}}^2}{\mathbf{a}_{\text{H}_2\text{O}}} \right)}$				
	LHHW-RLS4		ER _{H20} -RLS3			
H ₂ O desorption	$\mathbf{r}_{\text{DNBE}} = \frac{\mathbf{k}_{\text{H}_{2}\text{O}} \left(\mathbf{K}_{\text{eq}} \frac{a_{\text{BuOH}}^2}{a_{\text{DNBE}}} - a_{\text{H}_{2}\text{O}} \right)}{1 + \mathbf{K}_{\text{BuOH}} \cdot a_{\text{BuOH}} + \mathbf{K}_{\text{DNBE}} \cdot a_{\text{DNBE}} + \mathbf{K}_{\text{H}_{2}\text{O}} \cdot \left(\mathbf{K}_{\text{eq}} \frac{a_{\text{BuOH}}^2}{a_{\text{DNBE}}} \right)}$		$r_{\text{DNBE}} = \frac{\frac{1}{k_{\text{H}_{2}\text{O}} \left(K_{\text{eq}} \frac{a_{\text{BuOH}}^2}{a_{\text{DNBE}}} - a_{\text{H}_{2}\text{O}} \right)}{1 + K_{\text{BuOH}} \cdot a_{\text{BuOH}} + K_{\text{H}_{2}\text{O}} \cdot \left(K_{\text{eq}} \frac{a_{\text{BuOH}}^2}{a_{\text{DNBE}}} \right)}$			

Table 4. Best kinetic models (fitted parameters, confidence interval for a 95% of probability, sum of squared relative errors and goodness of the fit) for experiments starting from pure 1-butanol.

RLS	LHHW-RLS4/1b RLS: water desorption. Assuming the amount of free active sites to be negligible.						
	(13)						
S	SSRE = 0.59 $R_{adj}^2 = 0.99$ $\Delta = 0.60$						
			Parameters				
А	E _A [kJ/mol]	$\begin{array}{c} \Delta S_{\rm BuOH} \text{-} \Delta S_{\rm H2O} \\ [J/mol \cdot K] \end{array}$	ΔH_{BuOH} - ΔH_{H2O} [kJ/mol]	$\frac{\Delta S_{\text{DNBE}} - \Delta S_{\text{H2O}}}{[J/\text{mol} \cdot K]}$	ΔH_{DNBE} - ΔH_{H2O} [kJ/mol]		
24.2±1.0	112.8±3.5	38.9±1.9	-50.7±17.8	44.8 ± 2.8	48.0±22.7		
		Ĵ,	HW-RLS3/1b				
RLS:	DNBE desor	ption. Assumin	g the amount of fro	ee active sites to b	e negligible.		
	$r_{\text{DNBE}} = \frac{\frac{K_{\text{DNBE}}}{K_{\text{DNBE}}} \left(K_{\text{eq}} \frac{a_{\text{BuOH}}^2}{a_{\text{H}_2\text{O}}} \cdot a_{\text{DNBE}} \right)}{\frac{K_{\text{BuOH}}}{K_{\text{DNBE}}} \cdot a_{\text{BuOH}} + K_{\text{eq}} \frac{a_{\text{BuOH}}^2}{a_{\text{H}_2\text{O}}} + \frac{K_{\text{H}_2\text{O}}}{K_{\text{DNBE}}} \cdot a_{\text{H}_2\text{O}}} $ (14)						
S	$\mathbf{SRE} = 0.60$		$R_{adj}^2 = 0.99$	Δ	= 0.65		
			Parameters				
А	E _A [kJ/mol]	$\begin{array}{l} \Delta S_{\text{BuOH}}\Delta S_{\text{DNBE}} \\ [J/mol {\cdot} K] \end{array}$	$\Delta H_{BuOH}-\Delta H_{DNBE}$ [kJ/mol]	ΔS_{H2O} - ΔS_{DNBE} [J/mol·K]	ΔH_{H2O} - ΔH_{DNBE} [kJ/mol]		
24.7±1.1	110.7 ± 4.0	37.3±1.3	-53.9±16.5	36.0±3.4	47.9 ± 27.1		
RLS	S: surface read	LI ction. Assuming	HHW-RLS2/1b the amount of free	e active sites to be	e negligible.		
	$\mathbf{r}_{\text{DNBE}} = \frac{\hat{\mathbf{k}} \cdot \frac{\mathbf{K}_{\text{BuOH}}^2}{\mathbf{K}_{\text{BuOH}}^2} \left(\mathbf{a}_{\text{BuOH}}^2 - \frac{\mathbf{a}_{\text{DNBE}} \cdot \mathbf{a}_{\text{H_2O}}}{\mathbf{K}_{\text{eq}}} \right)}{\left(\mathbf{a}_{\text{BuOH}} + \frac{\mathbf{K}_{\text{DNBE}}}{\mathbf{K}_{\text{BuOH}}} \cdot \mathbf{a}_{\text{DNBE}} + \frac{\mathbf{K}_{\text{H_2O}}}{\mathbf{K}_{\text{BuOH}}} \cdot \mathbf{a}_{\text{H_2O}} \right)^{2+n}} $ (15)						
n		(1	2		
SSRE:		0.9	94	0.96	1.01		
$\mathbf{R}_{\mathrm{adj}}^2$:		0.9	97	0.98	0.97		
Δ:		1.'	79	1.99	2.59		
			Parameters				
A:		25.4	± 1.1 2	5.5±1.1	25.6±1.1		
E _A [kJ/mol	[]: a (1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1	118.5	0±3.9 1]	8./±4.0	118.9±4.1		
$\Delta S_{DNBE} - \Delta S_{DNBE}$	S _{BuOH} [J/mol·k	≤j: 6.9±	2.6 4	1.1±3.6	2.2±4.3		
$\Delta H_{\rm DNBE} - \Delta$	H _{BuOH} [kJ/mo]	IJ: -26.3	±26.4 -2'	7.3±28.9	-28.0±29.7		
$\Delta S_{H2O} - \Delta S$	BuOH [J/mol·K	.j: -12.8:	± 15.3 -10	0.0±12.1	-8.3±9.8		
$\Delta H_{H2O} - \Delta$	H _{BuOH} [kJ/mol	lj: 116.7	±92.2 83	3.4±12.1	66.6 ± 48.4		

 Table 5. Best kinetic models (fitted parameters, confidence interval for a 95% of probability,

 sum of squared relative errors and goodness of the fit) for experiments starting from mixtures 1

 butanol/water and 1-butanol/DNBE.

LHHW-RLS3/1b (see Equation 14) RLS: DNBE desorption. Assuming the amount of free active sites to be negligible.								
SS	SRE = 0.36		$R_{adj}^2 = 1.00$		A = 2.53			
	Parameters							
А	E _A [kJ/mol]	$\frac{\Delta S_{\text{BuOH}} \text{-} \Delta S_{\text{DNBE}}}{[J/\text{mol} \cdot K]}$	$\Delta H_{BuOH}-\Delta H_{DM}$ [kJ/mol]	NBE $\Delta S_{H2O} - \Delta S_{DNBE}$ [J/mol·K]	$ \Delta H_{H2O} - \Delta H_{DNBE} $ [kJ/mol]			
14.4 ± 0.8	117.8±6.7	33.6±1.8	-18.4±18.5	38.9±0.9	3.9±9.1			
		LHHW-RLS	S2/1b (see Eq	uation 15)				
RLS	: surface rea	ction. Assuming	the amount of	free active sites to b	oe negligible.			
n			0	1	2			
SSRE:			0.52	0.45	0.43			
$\mathbf{R}_{\mathrm{adj}}^{2}$:			0.98	0.98	0.98			
Δ:			13.59	6.61	1.89			
			Parameters					
A:		16	5.9 ± 1.0	16.9 ± 0.8	16.9 ± 0.8			
E _A [kJ/mol]:	12	0.7 ± 5.8	122.7 ± 4.7	123.9 ± 4.4			
$\Delta S_{\text{DNBE}} - \Delta S_{\text{DNBE}}$	S _{BuOH} [J/mol·	K]: -10	5.7 ± 7.9	-9.5 ± 1.9	-7.8 ± 1.1			
$\Delta H_{\text{DNBE}} - \Delta$	H _{BuOH} [kJ/mo	ol]: -5	9 ± 162	3.4 ± 21.8	10.2 ± 12.0			
$\Delta S_{H2O} - \Delta S$	_{BuOH} [J/mol·k	K]: 4	$.9 \pm 0.5$	2.0 ± 0.3	0.2 ± 0.3			
$\Delta H_{\rm H2O} - \Delta I$	H _{BuOH} [kJ/mo	1]: 463	$.2 \pm 6159$	2.8 ± 4.3	4.0 ± 3.4			
			HW-RLS2/3	b				
Assu	ming negligi	KLS: ble the amount of	surface reacti free active sit	0n. es and the adsorpti	on of DNRF			
	Assuming negligible the amount of free active sites and the adsorption of DNBE. $r_{\text{DNBE}} = \frac{\hat{k} \cdot \frac{K_{\text{BuOH}}^2}{K_{\text{BuOH}}^{2+n}} \left(a_{\text{BuOH}}^2 - \frac{a_{\text{DNBE}} \cdot a_{\text{H}_2\text{O}}}{K_{\text{eq}}} \right)}{\left(a_{\text{BuOH}} + \frac{K_{\text{H}_2\text{O}}}{K} \cdot a_{\text{H}_2\text{O}} \right)^{2+n}} $ (16)							
n			0	1	2			
SSRE:			0.54	1.02				
$\mathbf{R}_{\mathrm{adj}}^{2}$:			0.98	0.98				
Δ:			2.35	0.70				
			Parameters					
A:		16	5.1 ± 0.7	14.2 ± 0.7				
E _A [kJ/mol]:	12	2.1 ± 5.4	125.2 ± 6.5				
$\Delta S_{H2O} - \Delta S_{II}$	_{виОН} [J/mol·K	4]: 4	$.6 \pm 0.4$	1.2 ± 0.5				
$\Delta H_{H2O} - \Delta H$	I _{BuOH} [kJ/mol]: 2	$.5 \pm 6.0$	10.7 ± 6.1				

Equation	Correction factor	Comments	Ref.
(17)	$(1 - K_w \cdot a_{H_{2O}}^{1/\alpha})^m$ with $\alpha = K_{\alpha}/T$	Freundlich isotherm.	14
(18)	$\left(\frac{1}{1+K_{w}\cdot a_{H_{2}O}}\right)^{m}$	Langmuir isotherm where a molecule of water adsorbs on one active site.	16
(19)	$\left(\frac{1}{1+K_{w}\cdot a_{H_{2}O}^{0.5}}\right)^{m}$	Langmuir isotherm where a molecule of water adsorbs on two active sites.	15

 Table 6. Correction factors to represent water inhibiting effect on reaction rate

Table 7. Best *modified* kinetic models (fitted parameters, confidence interval for a 95% of

 probability, sum of squared relative errors and goodness of the fit) for experiments starting from

 mixtures 1-butanol/water and 1-butanol/DNBE.

LHHW-RLS2/1b (see Equation 15) RLS: surface reaction. Assuming the amount of free active sites to be negligible.							
n			0	1		2	
SSRE:			0.14	0.15	().16	
$\mathbf{R}_{\mathrm{adj}}^{2}$:			1.00	1.00	1	1.00	
Δ:			3.21	1.37	1	1.59	
			Parameters				
A:		1	6.6 ± 0.6	16.6 ± 0.6	16.0	6 ± 0.6	
E _A [kJ/mo	l]:	11	4.6 ± 3.9	115.9 ± 3.7	116.	$.7 \pm 3.7$	
$\Delta S_{\text{DNBE}} - \Delta$	S _{BuOH} [J/mol	•K]: -1	1.4 ± 2.4	-8.3 ± 1.0	-7.1	1 ± 0.7	
$\Delta H_{\text{DNBE}} - \Delta$	H _{BuOH} [kJ/m	ol]: 20	0.5 ± 24.7	-19.5 ± 10.8	19.0	0 ± 7.0	
$\Delta S_{H2O} - \Delta S_{H2O}$	BuOH [J/mol·]	K]: 4	4.0 ± 0.4	1.3 ± 0.3	-0.3	3 ± 0.3	
$\Delta H_{\rm H2O} - \Delta$	H _{BuOH} [kJ/m	ol]: -1	4.3 ± 5.3	-9.4 ± 4.3	-6.4	1 ± 3.7	
K_{w1} :		-0.	$.19 \pm 0.55$	$\textbf{-0.64} \pm 0.65$	-0.99	$\theta \pm 0.70$	
K_{w2} :		57	14 ± 2112	7572 ± 2902	8670	± 3475	
Κ _α :		65	5.4±26.5	88.3 ± 26.6	86.8	S ± 27.6	
		LHHW-RL	S2/2b (see Equ	ation 21)			
		RLS:	Surface reacti	on.			
Ass	uming negli	gible the amount	of free active si	tes and the ads	sorption of H	$I_2O.$	
n			0	1		2	
SSRE:			0.22	0.23	().24	
$\mathbf{R}_{\mathrm{adj}}^{2}$:			0.99	0.99	().99	
Δ:			0.81	0.53	().41	
			Parameters				
A:		1	6.4 ± 0.8	16.3 ± 0.7	16.	3 ± 0.7	
E _A [kJ/mo]	l]:	12	23.2 ± 2.3	123.2 ± 2.4	123.	2 ± 2.5	
$\Delta S_{\text{DNBE}} - \Delta$	S _{BuOH} [J/mol-	•K]: -9	9.5 ± 1.5	-7.6 ± 0.8	$\textbf{-6.7}\pm0.6$		
$\Delta H_{\text{DNBE}} - \Delta$	H _{BuOH} [kJ/m	ol]: 34	4.0 ± 14.5	25.5 ± 8.2	22.5	5 ± 5.8	
K_{w1} :		-0.	10 ± 0.02	-0.23 ± 0.02	-0.32	2 ± 0.02	
K_{w2} :		2	65 ± 166	415 ± 164	527	±156	
Κ _α :		55	0.0 ± 34.8	499.6 ± 25.5	477.4	4 ± 21.0	
		LHHW-RL	S4/2b (see Equ	ation 22)			
RLS: Desorption of water.							
ASSU			$\mathbf{D}^2 = 0 \cdot 0$	s and the auso			
5	SKE = 0.25		N _{adj} – 0.99		Δ = 1.50		
A		4.0 4.0	Parameters	17	V	IZ.	
A	E _A [kJ/mol]	$\Delta S_{BuOH} - \Delta S_{H2O}$ [J/mol·K]	$\Delta H_{BuOH} - \Delta H_{H2O}$ [kJ/mol]	\mathbf{K}_{w1}	K _{w2}	Κα	
19.2 ± 1.4	121.8±2.2	22.7±1.9	55.8±17.5	0.08 ± 0.02	56.8 ± 81.8	991±108	

Table 8. Best *modified* kinetic models (fitted parameters, confidence interval for a 95% of probability, sum of squared relative errors and goodness of the fit) for all experimental data.

LHHW-RLS2/2b (see Equation 21) RLS: Surface reaction.							
Assuming negligible the amount of free active sites and the adsorption of H ₂ O.							
n			0	1		2	
SSRE:			1.24	1.38		1.50	
$\mathbf{R}_{\mathrm{adj}}^2$:			0.99	0.99		0.99	
Δ:		2.50	0.84	0.54			
Parameters							
A:	A:		25.4 ± 1.1	24.9 ± 1.0	24.7 ± 1.0		
$E_A [kJ/mol]:$		21.7 ± 1.8	122.2 ± 1.9	122.6 ± 2.0			
$\Delta S_{\text{DNBE}} - \Delta S_{\text{BuOH}} [J/mol \cdot K]$:			9.6 ± 1.7	-7.2 ± 0.9	-6.3 ± 0.7		
$\Delta H_{\text{DNBE}} - \Delta H_{\text{BuOH}} [kJ/mol]:$			1.2 ± 12.9	42.6 ± 7.5	36.1 ± 5.4		
K_{w1} :		-0	$.08 \pm 0.03$	$\textbf{-0.20} \pm 0.03$	-0.2	$\textbf{-0.29} \pm 0.02$	
K _{w2} :		73	3.3 ± 180.4	233.1 ± 184.6	5 364.	364.2 ± 178.6	
Κ _α : 56		53.2 ± 42.4	499.4 ± 31.5	471.8 ± 26.2			
LHHW-RLS4/2b (see Equation 22)							
RLS: Desorption of water.							
Assuming negligible the amount of free active sites and the adsorption of DNBE.							
SSRE = 1.34			$R_{adj}^2 = 0.98$		$\Delta = 2.54$		
Parameters							
Α	EA	ΔS_{BuOH} - ΔS_{H2O}	ΔH_{BuOH} - ΔH_{H2O}	K_{w1}	K _{w2}	K_{α}	
	[kJ/mol]	$[J/mol \cdot K]$	[kJ/mol]				
29.7±2.1	121.3±1.8	22.8±2.0	83.7±15.4	0.09 ± 0.02	36.8±92.5	1018±128	



Figure 1. (a) 1-butanol conversion, (b) selectivity to DNBE and (c) reaction rate of DNBE synthesis as a function of temperature: (**■**) 413 K; (\circ) 423 K; (\diamond) 433 K; (Δ) 443 K; (\bullet) 453 K; (\Box) 463 K. Experiments starting from pure 1-butanol, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm. The error bars indicate the confidence interval at a 95% probability level. Most error bars are smaller than markers.



Figure 2. Reaction rate of DNBE synthesis as a function of (a) 1-butanol activity; (b) water activity; (c) DNBE activity. (**n**) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Experiments starting from pure 1-butanol, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm.



Figure 3. Evolution of the ratio a_{H2O}/a_{DNBE} with time for experiments starting from pure 1butanol. (**•**) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Experiments starting from pure 1-butanol, 1 g of catalyst, $d_p = 0.4 - 0.63$ mm, 4 MPa, 500 rpm.



Figure 4. (a) Calculated reaction rates by model LHHW-RLS4/1b (Equation 13) versus experimental rates; (b) residuals distribution. (**•**) 413 K, (\circ) 423 K, (\diamond) 433 K, (Δ) 443 K, (\bullet) 453 K, (\Box) 463 K. Experiments starting from pure 1-butanol, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm.



Figure 5. Influence of (a) water and (b) DNBE on the initial reaction rate of DNBE formation. (**•**) 413 K, (**•**) 433 K, (**•**) 453 K, 1 g of catalyst, $d_p = 0.4 - 0.63$ mm, 4 MPa, 500 rpm.



Figure 6. Selectivity to products after 7 h reaction as a function of initial water content. T = 463 K, 1 g of catalyst, $d_p = 0.4 - 0.63$ mm, 4 MPa, 500 rpm. (**a**) DNBE, (\circ) 1-butene, (\blacklozenge) 2-butanol, (\blacktriangle) cis-2-butene, (\bullet) trans-2-butene, (\Box) 1-(1-methylpropoxy) butane.



Figure 7. Calculated reaction rates by models (a) LHHW-RLS3/1b (Equation 14) and (b) LHHW-RLS2/1b with n = 2 (Equation 15) versus experimental rates; residuals distribution for models (c) LHHW-RLS3/1b and (d) LHHW-RLS2/1b with n = 2. (**n**) 413 K, (**•**) 433 K, (\circ) 453 K. Experiments starting from mixtures 1-butanol/water and 1-butanol/DNBE, 1 g of catalyst, d_p = 0.4 - 0.63 mm, 4 MPa, 500 rpm



Figure 8. Calculated reaction rates by the *modified* models (a) LHHW-RLS2/2b (Equation 21) and (b) LHHW-RLS4/2b (Equation 22) versus experimental rates; residuals distribution for models LHHW-RLS4/2b (c) and LHHW-RLS2/2b (d). (**•**) 413 K, (\circ) 423 K, (**•**) 433 K, (Δ) 443 K, (**•**) 453 K, (\Box) 463 K. Rate data corresponding to all the experiments, 1 g of catalyst, d_p = 0.4 – 0.63 mm, 4 MPa, 500 rpm.



Figure 9. Freundlich factor corresponding to models LHHW-RLS2/2b (a) and LHHW-RLS4/2b (b) vs. a_{H2O} at different temperatures. (**•**) 413 K, (\circ) 423 K, (**•**) 433 K, (Δ) 443 K, (**•**) 453 K, (\Box) 463 K. All the experiments, 1 g of catalyst, $d_p = 0.4 - 0.63$ mm, 4 MPa, 500 rpm.