

Document de treball de l'IEB 2013/26

FEEDBACK EQUILIBRIA IN A DYNAMIC RENEWABLE RESOURCE OLIGOPOLY:  
PRE-EMPTION, VORACITY AND EXHAUSTION

**Luca Lambertini, Andrea Mantovani**

**FEEDBACK EQUILIBRIA IN A DYNAMIC  
RENEWABLE RESOURCE OLIGOPOLY:  
PRE-EMPTION, VORACITY AND EXHAUSTION**

Luca Lambertini, Andrea Mantovani

The **Barcelona Institute of Economics (IEB)** is a research centre at the University of Barcelona which specializes in the field of applied economics. Through the **IEB-Foundation**, several private institutions (Applus, Abertis, Ajuntament de Barcelona, Diputació de Barcelona, Gas Natural and La Caixa) support several research programs.

Postal Address:

Institut d'Economia de Barcelona  
Facultat d'Economia i Empresa  
Universitat de Barcelona  
C/ Tinent Coronel Valenzuela, 1-11  
(08034) Barcelona, Spain  
Tel.: + 34 93 403 46 46  
Fax: + 34 93 403 98 32  
[ieb@ub.edu](mailto:ieb@ub.edu)  
<http://www.ieb.ub.edu>

The IEB working papers represent ongoing research that is circulated to encourage discussion and has not undergone a peer review process. Any opinions expressed here are those of the author(s) and not those of IEB.

**FEEDBACK EQUILIBRIA IN A DYNAMIC  
RENEWABLE RESOURCE OLIGOPOLY:  
PRE-EMPTION, VORACITY AND EXHAUSTION \***

Luca Lambertini, Andrea Mantovani

**ABSTRACT:** We extend Fujiwara's (2008) model to describe a differential oligopoly game of resource extraction under static, linear feedback and nonlinear feedback strategies, generalising his result that steady state feedback outputs are lower than monopoly and static oligopoly equilibrium outputs for any number of firms. Additionally, we show that (i) feedback rules entail resource exhaustion for a finite number of firms; and (ii) feedback strategies are more aggressive than static ones as long as the resource stock is large enough, in accordance with the acquired view based on the traditional pre-emption argument associated with feedback information.

JEL Codes: C73, L13, Q2

Keywords: Dynamic oligopoly, renewable resources, feedback strategies.

Luca Lambertini  
Department of Economics  
University of Bologna & ENCORE  
Strada Maggiore 45  
40125 Bologna, Italy  
E-mail : [lamberti@spbo.unibo.it](mailto:lamberti@spbo.unibo.it)

Andrea Mantovani  
Department of Economics  
University of Bologna & IEB  
Strada Maggiore 45  
40125 Bologna, Italy  
E-mail: [a.mantovani@unibo.it](mailto:a.mantovani@unibo.it)

---

\* We thank Luca Colombo, Paola Labrecciosa and Arsen Palestini for precious comments and suggestions. The usual disclaimer applies.

# 1 Introduction

The analysis of dynamic market interplay through differential games has revealed - among other things - that feedback information boosts strategic interaction among firms as compared to open-loop information, triggering a pre-emption mechanism leading firms to expand production (for an overview, see Dockner *et al.*, 2000, ch. 10). Fujiwara (2008), relying on Benckroun (2003, 2008), proposes a dynamic game of duopolistic extraction of a renewable resource, where at equilibrium output levels are lower under linear and nonlinear feedback information than under monopoly and the static oligopoly equilibria. We revisit his model allowing for the presence of  $n$  firms, to illustrate that his result that linear and nonlinear feedback equilibria are less competitive than monopoly and static oligopoly equilibria extend to the general case of an oligopoly with  $n$  firms.<sup>1</sup> This, however, implies that feedback information causes the exhaustion of the resource at the steady state for a finite number of firms (in correspondence of which equilibrium profits also drop to zero). This leads us to the main focus of our note, as the puzzling aspect of these results is that, taken together, they seem to imply that a less aggressive behavior goes along with exhaustion. The explanation lies in the fact that Fujiwara's appraisal is valid in steady state, but not at any generic instant during the game. Indeed, using the per-firm optimal output defined for a generic resource volume at a generic instant before doomsday, we show that, as long as the amount of the resource is large enough, the traditional wisdom applies and output levels are larger under feedback rules, respecting the intuition behind the standard pre-emption argument. To illustrate this fact, we explicitly identify the critical threshold of the resource stock below which Fujiwara's conclusion holds true. Finally, we also illustrate the presence of a *voracity effect* operating for sufficiently high levels of the resource growth rate, whereby higher growth rates lead to lower steady state resource stocks.

---

<sup>1</sup>The extension to the case of  $n$  firms is mentioned in Fujiwara (2008, fn. 8, p. 219) while it is investigated in Benckroun (2008) and Colombo and Labrecciosa (2013). The latter paper, in particular, focuses on the consequences of an *ex ante* resource parcelization among a population of firms. Fujiwara (2011) investigates the welfare effects of increasing the number of firms when these are characterised by different levels of technological efficiency.

## 2 The model

The setup is the same as in Bencheikroun (2008) and Fujiwara (2008). We consider a differential oligopoly game of resource extraction over time  $t \in [0, \infty)$ . The industry consists of an  $n$  firms producing a homogeneous good, whose inverse demand function is  $p = a - Q$  at any time  $t$ , with  $Q = \sum_{i=1}^n q_i$ . Marginal cost  $c \in (0, a)$  is constant and common to all firms, which operate without any fixed costs. During production, each firm exploits a renewable natural resource, whose accumulation is governed by the following dynamics:

$$\dot{S} = F(S) - Q \quad (1)$$

with

$$F(S) = \begin{cases} \delta S \forall S \in (0, S_y] \\ \delta S_y \left( \frac{S_{\max} - S}{S_{\max} - S_y} \right) \forall S \in (S_y, S_{\max}] \end{cases} \quad (2)$$

where  $S$  is the resource stock,  $\delta > 0$  is its *implicit* growth rate when the stock is at most equal to  $S_y$  and  $\delta S_y$  is the maximum sustainable yield. Taken together, (1-2) imply that (i) if the resource stock is sufficiently small the population grows at an exponential rate; and (ii) beyond  $S_y$ , the asset grows at a decreasing rate. Moreover,  $S_{\max}$  is the *carrying capacity* of the habitat, beyond which the growth rate of the resource is negative, being limited by available amounts of food and space. In the remainder, we will confine our attention to the case in which  $F(S) = \delta S$ .

If firms don't internalise the consequences of their behaviour at any time and play the individual (static) Cournot-Nash output  $q^{CN} = (a - c) / (n + 1)$  at all times, then the residual amount of the natural resource in steady state is  $S^{CN} = n(a - c) / [\delta(n + 1)] = Q^{CN} / \delta$ . For future reference, it is worth noting that the static solution corresponds to the open-loop steady state one, which in this game is unstable (see Figure 1 in Fujiwara, 2008, p. 218; and Lambertini, 2013, p. 240). The initial condition is  $S(0) = S_0 > n(a - c) / [\delta(n + 1)]$ , which suffices to guarantee  $S > 0$  at all times under the static Cournot-Nash strategies.<sup>2</sup>

---

<sup>2</sup>To see this, just observe that if firms always play *à la* Cournot, the stock at a generic  $t$  is

$$S(t) = \frac{n(a - c) + e^{\delta t} [\delta(n + 1) S_0 - n(a - c)]}{\delta(n + 1)}$$

which is surely positive if the above condition holds.

### 3 Feedback Nash equilibria

Following Fujiwara (2008), we consider both linear feedback strategies *à la* Benckroun (2003) and non linear strategies *à la* Tsutsui and Mino (1990) and Shimomura (1991). We restrict our attention to symmetric equilibria. The Hamilton-Jacobi-Bellman equation writes as:

$$rV_i(S) = \max_{q_i} \{[a - c - Q]q_i + V'(S) [\delta S - Q]q_i\} \quad (3)$$

where  $r > 0$  is the discount rate, common to all firms and constant over time;  $V_i(S)$  is the firm  $i$ 's value function; and  $V'(S) = \partial V(S) / \partial S$ . The first order condition (FOC) on  $q_i$  is

$$a - c - 2q_i - \sum_{j \neq i} q_j - V'(S) = 0 \quad (4)$$

In view of the *ex ante* symmetry across firms, we impose  $q_j = q_i = q(S)$  and solve the FOC (4) to obtain  $V'(S) = a - c - (n + 1)q(S)$ . Substituting this into (3) yields an identity in  $S$ . Differentiating both sides with respect to  $S$  and rearranging terms, any feedback strategy is implicitly given by the following differential equation:

$$q'(S) = \frac{(\delta - r) [(n + 1)q(S) - (a - c)]}{2n^2q(S) - \delta(n + 1)S - (n - 1)(a - c)}, \quad (5)$$

which must hold together with terminal condition  $\lim_{t \rightarrow \infty} e^{-rt}V(s)$ . From Fujiwara (2008, p. 218), we borrow the assumption  $\delta > 5r/2$ , which amounts to requiring that the rate of reproduction of the natural resource be high enough to ensure the non negativity of steady state equilibrium magnitudes with  $n \geq 2$ . In general, to ensure non-negativity *for any number of firms*, one should assume  $\delta > (n^2 + 1)r/2$ , as in Benckroun (2008, p. 240). The more restrictive assumption we are adopting is interesting for reasons that will become clear in the remainder.

#### 3.1 Linear feedback strategy

If the strategy is linear in  $S$ , so that  $q(S) = \alpha S + \beta$ , equation (5) becomes:

$$\alpha = \frac{(\delta - r) [(n + 1)(\alpha S + \beta) - (a - c)]}{2n^2(\alpha S + \beta) - (n + 1)\delta S - (n - 1)(a - c)} \quad (6)$$

which is satisfied iff

$$\begin{aligned} & (\delta - r) [a - c - \beta (n + 1)] + \alpha [2\beta n^2 - (a - c) (n - 1)] \\ & + \alpha [r (n + 1) - 2 (\delta (n + 1) - \alpha n^2)] S = 0. \end{aligned} \quad (7)$$

The above equation gives rise to the following system of two equations

$$\begin{aligned} & \alpha [r (n + 1) - 2 (\delta (n + 1) - \alpha n^2)] = 0 \\ & (\delta - r) [a - c - \beta (n + 1)] + \alpha [2\beta n^2 - (a - c) (n - 1)] = 0 \end{aligned} \quad (8)$$

to be solved w.r.t. the unknown parameters  $\{\alpha, \beta\}$ . The pairs solving (8) are  $(\alpha = 0; \beta = (a - c) / (n + 1))$ , which replicates the static Cournot-Nash solution  $q^{CN}$ , and

$$\alpha = \frac{(n + 1) (2\delta - r)}{2n^2}; \beta = -\frac{(a - c) [2\delta - r (n^2 + 1)]}{2\delta (n + 1) n^2}. \quad (9)$$

In correspondence of (9), the individual output is

$$q_{LF}^N(S) = \frac{\delta (2\delta - r) (n + 1)^2 S - (a - c) [2\delta - r (n^2 + 1)]}{2\delta (n + 1) n^2} \quad (10)$$

where superscript  $N$  stands for *Nash equilibrium* while subscript  $LF$  stands for *linear feedback*. Leaving aside for brevity the replication of the stability analysis carried out by Fujiwara (2008, p. 218), we focus on (10). If  $Q_{LF}^* = nq_{LF}^*$ , the steady state amount of resource solving  $\dot{S} = 0$  is (henceforth, starred values indicate steady state equilibrium magnitudes):

$$S_{LF}^* = \frac{nq_{LF}^*}{\delta} = \frac{(a - c) [2\delta - r (n^2 + 1)]}{\delta [2\delta - r (n + 1)] (n + 1)} \quad (11)$$

which is non-negative for all  $\delta > r (n^2 + 1) / 2$ , the latter condition coinciding with the assumption  $\delta > 5r/2$  made by Fujiwara if  $n = 2$ . It is then easily verified that

$$\frac{\partial Q_{LF}^*}{\partial n} = -\frac{2(a - c) (\delta - r) [2\delta + r (n^2 - 1)]}{(n + 1)^2 [2\delta - r (n + 1)]^2} < 0 \quad (12)$$

for all  $n \geq 1$ . However, it is also true that  $S_{LF}^* = Q_{LF}^* = 0$  for all  $n \geq \sqrt{(2\delta - r)/r} > 2$  (under the above assumption).

To appreciate the bearings of the linear feedback solution on the residual resource stock, it is worth observing that, by construction, the game is a linear state one (this being the reason why the open-loop solution is sub-game perfect, although unstable). Therefore, the adoption of linear feedback strategies is formally equivalent to introducing a square term for the state variable which is not present in the initial definition of the setup, as is clear from section 2. Once firms behave as *if* the game were indeed quadratic in the state, they boost strategic interaction and therefore also exploitation, much the same way as they would if, paradoxically enough, they received a subsidy to their extraction activities.

### 3.2 Nonlinear feedback strategy

The case of nonlinear feedback strategies can be quickly dealt with. One imposes stationarity on the state equation, obtaining  $q = \delta S/n$ , whereby (5) becomes:

$$\frac{\delta}{n} = \frac{(\delta - r) [\delta(n + 1)S + n(a - c)]}{n(n - 1)(a - c - \delta S)}, \quad (13)$$

from which one obtains

$$S_{NLF}^* = \frac{(a - c)(\delta - nr)}{\delta [2\delta - r(n + 1)]} = \frac{nq_{NLF}^*}{\delta} \quad (14)$$

with  $\partial S_{NLF}^*/\partial n \propto \partial Q_{NLF}^*/\partial n < 0$  for all  $n \geq 1$ , and  $S_{NLF}^* = Q_{NLF}^* = 0$  for all  $n \geq \delta/r > \sqrt{(2\delta - r)/r}$ .<sup>3</sup>

The foregoing analysis can be summarised in

**Lemma 1** *Under both linear and nonlinear feedback strategies, the steady state industry output is everywhere decreasing in the number of firms. However, so is also the steady state equilibrium resource stock, and both magnitudes drop to zero in correspondence of a finite number of firms, which is increasing in the resource growth rate and decreasing in the discount rate.*

This generalises Fujiwara's conclusion to the general case of an oligopoly with  $n$  firms, making explicit an observation that can be found in Fujiwara (2008, fn. 8, p. 219) as to the fact that increasing the number of firms

---

<sup>3</sup>The initial amount of resource must be lower than  $S_{NLF}^*$  in order for  $q_{NLF}^*$  to be an equilibrium strategy (see Itaya and Shimomura, 2001; Rubio and Casino, 2002).

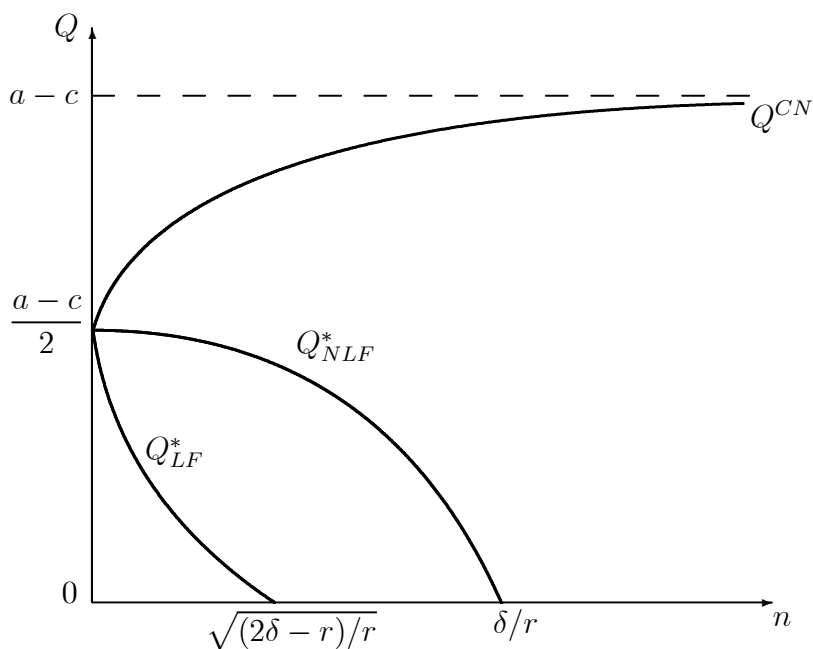


reduces aggregate extraction and output. However, may we really draw the implication that under feedback rules oligopolistic interaction is indeed less competitive than monopoly or static oligopoly? This question, which is a tricky one in connection with the exhaustion issue, is addressed in the next section.

### 3.3 Comparing equilibria

We are now in a position to comparatively assess firms' behaviour and its consequences across the three equilibria considered above. This exercise can be carried out graphically as in Figure 1, in the space  $\{n, Q\}$ , in which the curves representing the three possible aggregate outputs depart from the monopoly quantity  $q_M = (a - c) / 2$ .

**Figure 1** Equilibrium industry output and structure



Given the fixed proportion between  $S$  and  $Q$ , immediate implications can be drawn on the resource stock. Since the assumption  $\delta > 5r/2$  is equivalent to  $\sqrt{(2\delta - r)/r} > 2$ , Figure 1 illustrates the following:

**Proposition 2** *Feedback information leads to the exhaustion of the resource at the steady state for a finite number of firms, increasing in  $\delta$  and decreasing*

in  $r$ . Conversely, the residual resource stock at the static Cournot equilibrium is positive and increasing in  $n$ .

It is worth noting that resource exhaustion, being accompanied by nil output levels, implies that steady state profits are also zero in correspondence of a finite number of firms, while the annihilation of profits at the static equilibrium takes place only in the limit as  $n$  tends to infinity and the industry becomes perfectly competitive.

From the existing literature (see Fershtman and Kamien, 1987; Reynolds, 1987, 1991; and Cellini and Lambertini, 2004, *inter alia*), we are accustomed to think that feedback information intensifies strategic interaction among firms, which translates into larger outputs due to the incentive to pre-empt rivals generated by feedback rules themselves. How can we reconcile this acquired wisdom with the seemingly opposite picture emerging from Proposition 2? That is, to what extent it is true that feedback strategies are less competitive than monopolistic behaviour and, *a fortiori*, static Cournot-Nash strategies?

To answer these questions, observe that the difference

$$q_{LF}^N(S) - q^{CN} = \frac{(2\delta - r) [\delta (n + 1)^2 S - (a - c) (n^2 + 1)]}{2\delta (n + 1) n^2} > 0 \quad (15)$$

for all

$$S > \frac{(a - c) (n^2 + 1)}{\delta (n + 1)^2} \equiv \bar{S}, \quad (16)$$

with  $\bar{S} > S_{LF}^*$  for all  $\delta > (n + 1)r/2$ , which simplifies to  $\delta > 5r/2$  if  $n = 2$ . This reveals that, as long as the resource stock is larger than the threshold  $\bar{S}$ , linear feedback strategies are indeed more aggressive than static Cournot ones. As soon as  $S$  drops below  $\bar{S}$ , the opposite applies throughout the continuation of the game, up to the steady state, where indeed the result portrayed in Proposition 2 and Figure 1 appears.

The last step consists of verifying whether, during the game,  $Q_{LF}^N(S) = nq_{LF}^N(S) > q_M$  in an admissible range of  $S$ . It turns out that this holds true for all

$$S > \hat{S} \equiv \frac{(a - c) [\delta (2 + n(n + 1)) - (n^2 + 1)r]}{\delta (2\delta - r) (n + 1)^2} \quad (17)$$

with  $\hat{S} \in (S_{LF}^*, \bar{S})$  for all admissible values of parameters. Hence, at any instant in which  $S > \hat{S}$ , following linear feedback rules the oligopoly extracts and sells more than a monopolist. Thus, our analysis can be summarised in

**Proposition 3** Consider a generic instant  $t \in [0, \infty)$ . If, at time  $t$ ,  $S > \bar{S}$ , then  $Q_{LF}^N(S) > nq^{CN}$  for all  $n \geq 1$ . If instead  $S \in (\hat{S}, \bar{S})$ , then  $Q_{LF}^N(S) \in (q_M, nq^{CN})$ . Finally, if  $S < \hat{S}$ , then  $Q_{LF}^N(S) < q_M$ .

Proposition 3 tells that the intensity of aggregate production (or resource extraction) at a generic point in time before the steady state is reached is decreasing in the existing stock of resource, falling below the monopoly level if the stock falls below a well defined threshold. Put it differently, the steady state picture does not encompass the behaviour of the industry while the game is still unraveling.

## 4 Voracity effect

Our exercise is also connected with the so-called *voracity effect* first explored in Lane and Tornell (1996) and Tornell and Lane (1999) and then investigated by Benckroun (2008, pp. 245-48) using the same resource extraction game we have adopted here. In a nutshell, the voracity effect says that the *a priori* intuition suggesting that the higher is the resource growth rate, the higher should be the steady state volume of that resource, in fact may not be correct. This happens because a higher reproduction rate drives firms to hasten extraction, as indeed illustrated by (15-16) above. In this regard, we briefly complement the above analysis by looking at the comparative statics properties of the steady state levels of  $S$  in the three cases under examination:

$$\begin{aligned} \frac{\partial S^{CN}}{\partial \delta} &= -\frac{n(a-c)}{(n+1)\delta^2} < 0 \text{ everywhere} \\ \frac{\partial S_{LF}^*}{\partial \delta} &= -\frac{(a-c)[(n+1)(n^2+1)r^2 + 4\delta(\delta - (n^2+1)r)]}{(n+1)[2\delta - r(n+1)]^2 \delta^2} < 0 \forall \delta > \tilde{\delta} \\ \frac{\partial S_{NLF}^*}{\partial \delta} &= -\frac{(a-c)[n(n+1)r^2 + 2\delta(\delta - 2nr)]}{[2\delta - (n+1)r]^2 \delta^2} < 0 \forall \delta > \hat{\delta} \end{aligned} \quad (18)$$

with

$$\begin{aligned} \tilde{\delta} &= \frac{r}{2} \left[ n^2 + 1 + \sqrt{(n^2+1)(2+n(n+1))} \right] \\ \hat{\delta} &= r \left[ n + \sqrt{\frac{n(3n+1)}{2}} \right] \end{aligned} \quad (19)$$

and  $\tilde{\delta} > \max \left\{ \hat{\delta}, (n^2 + 1) r/2 \right\}$ . It is also easily ascertained that  $\tilde{\delta}$  and  $\hat{\delta}$  are increasing and convex in  $n$ . This allows us to formulate our final result:

**Proposition 4**  *$\delta > \tilde{\delta}$  suffices to ensure that the steady state resource stock be decreasing in the growth rate, irrespective of the structure of information underlying firms' equilibrium strategies. Under feedback rules, increasing the number of firms makes the appearance of voracity progressively less likely.*

## 5 Concluding remarks

Revisiting the dynamic game of renewable resource extraction by Benckroun (2008) and Fujiwara (2009), we have singled out a feature that has been previously overlooked, namely, that feedback strategies, although appearing less aggressive than static ones in steady state, indeed imply a higher pressure on the resource on the part of firms, whereby the steady state stock may indeed be driven to zero at equilibrium for a finite number of firms. This can be explained on the basis of a pre-emption incentive operating during the game, accompanied by a voracity effect if the growth rate of the resource is high enough.

## References

- [1] Benckroun, H. (2003). Unilateral production restrictions in a dynamic duopoly. *Journal of Economic Theory* **111**, 214-39.
- [2] Benckroun, H. (2008). Comparative dynamics in a productive asset oligopoly. *Journal of Economic Theory* **138**, 237-61.
- [3] Benckroun, H., Long, N.V. (2002). Transboundary fishery: a differential game model. *Economica* **69**, 207-21.
- [4] Cellini, R. and Lambertini, L. (2004). Dynamic oligopoly with sticky prices: closed-loop, feedback and open-loop solutions. *Journal of Dynamical and Control Systems* **10**, 303-14.
- [5] Colombo, L. and Labrecciosa, P. (2013). Oligopoly exploitation of a private property productive asset. *Journal of Economic Dynamics and Control*, **37**, 838-53.
- [6] Dockner, E.J., Jørgensen, S., Long, N.V. and Sorger, G. (2000). *Differential Games in Economics and Management Science*, Cambridge, Cambridge University Press.
- [7] Fershtman, C., Kamien, M. (1987). Dynamic duopolistic competition with sticky prices. *Econometrica* **55**, 1151-64.
- [8] Fujiwara, K. (2008). Duopoly can be more anti-competitive than monopoly. *Economics Letters* **101**, 217-19.
- [9] Fujiwara, K. (2011). Losses from competition in a dynamic game model of a renewable resource oligopoly. *Resource and Energy Economics*, **33**, 1-11
- [10] Itaya, J., Shimomura, K. (2001). A dynamic conjectural variations model in the private provision of public goods: a differential game approach. *Journal of Public Economics* **81**, 153-72.
- [11] Lambertini, L. (2013). *Oligopoly, the Environment and Natural Resources*, London, Routledge.
- [12] Lane, P.R. and Tornell, A. (1996). Power, growth, and the voracity effect. *Journal of Economic Growth* **1**, 213-41.

- [13] Reynolds, S. (1987). Preemption and commitment in an infinite horizon model. *International Economic Review* **28**, 69-88.
- [14] Reynolds, S. (1991). Dynamic oligopoly with capacity adjustment costs. *Journal of Economic Dynamics and Control* **15**, 491-514.
- [15] Rubio, S.J., Casino, B. (2002). A note on cooperative versus non-cooperative strategies in international pollution control. *Resource and Energy Economics* **24**, 251-61.
- [16] Shimomura, K. (1991). The feedback equilibria of a differential game of capitalism. *Journal of Economic Dynamics and Control* **15**, 317-38.
- [17] Tornell, A. and Lane, P.R. (1999). The voracity effect. *American Economic Review* **89**, 22-46.
- [18] Tsutsui, S., Mino, K. (1990). Nonlinear strategies in dynamic duopolistic competition with sticky prices. *Journal of Economic Theory* **52**, 136-61.

## 2011

- 2011/1, **Oppedisano, V; Turati, G.:** "What are the causes of educational inequalities and of their evolution over time in Europe? Evidence from PISA"
- 2011/2, **Dahlberg, M; Edmark, K; Lundqvist, H.:** "Ethnic diversity and preferences for redistribution "
- 2011/3, **Canova, L.; Vaglio, A.:** "Why do educated mothers matter? A model of parental help"
- 2011/4, **Delgado, F.J.; Lago-Peñas, S.; Mayor, M.:** "On the determinants of local tax rates: new evidence from Spain"
- 2011/5, **Piolatto, A.; Schuett, F.:** "A model of music piracy with popularity-dependent copying costs"
- 2011/6, **Duch, N.; García-Estévez, J.; Parellada, M.:** "Universities and regional economic growth in Spanish regions"
- 2011/7, **Duch, N.; García-Estévez, J.:** "Do universities affect firms' location decisions? Evidence from Spain"
- 2011/8, **Dahlberg, M.; Mörk, E.:** "Is there an election cycle in public employment? Separating time effects from election year effects"
- 2011/9, **Costas-Pérez, E.; Solé-Ollé, A.; Sorribas-Navarro, P.:** "Corruption scandals, press reporting, and accountability. Evidence from Spanish mayors"
- 2011/10, **Choi, A.; Calero, J.; Escardíbul, J.O.:** "Hell to touch the sky? private tutoring and academic achievement in Korea"
- 2011/11, **Mira Godinho, M.; Cartaxo, R.:** "University patenting, licensing and technology transfer: how organizational context and available resources determine performance"
- 2011/12, **Duch-Brown, N.; García-Quevedo, J.; Montolio, D.:** "The link between public support and private R&D effort: What is the optimal subsidy?"
- 2011/13, **Breuilé, M.L.; Duran-Vigueron, P.; Samson, A.L.:** "To assemble to resemble? A study of tax disparities among French municipalities"
- 2011/14, **McCann, P.; Ortega-Argilés, R.:** "Smart specialisation, regional growth and applications to EU cohesion policy"
- 2011/15, **Montolio, D.; Trillas, F.:** "Regulatory federalism and industrial policy in broadband telecommunications"
- 2011/16, **Pelegrín, A.; Bolancé, C.:** "Offshoring and company characteristics: some evidence from the analysis of Spanish firm data"
- 2011/17, **Lin, C.:** "Give me your wired and your highly skilled: measuring the impact of immigration policy on employers and shareholders"
- 2011/18, **Bianchini, L.; Revelli, F.:** "Green polities: urban environmental performance and government popularity"
- 2011/19, **López Real, J.:** "Family reunification or point-based immigration system? The case of the U.S. and Mexico"
- 2011/20, **Bogliacino, F.; Piva, M.; Vivarelli, M.:** "The impact of R&D on employment in Europe: a firm-level analysis"
- 2011/21, **Tonello, M.:** "Mechanisms of peer interactions between native and non-native students: rejection or integration?"
- 2011/22, **García-Quevedo, J.; Mas-Verdú, F.; Montolio, D.:** "What type of innovative firms acquire knowledge intensive services and from which suppliers?"
- 2011/23, **Banal-Estañol, A.; Macho-Stadler, I.; Pérez-Castrillo, D.:** "Research output from university-industry collaborative projects"
- 2011/24, **Lighthart, J.E.; Van Oudheusden, P.:** "In government we trust: the role of fiscal decentralization"
- 2011/25, **Mongrain, S.; Wilson, J.D.:** "Tax competition with heterogeneous capital mobility"
- 2011/26, **Caruso, R.; Costa, J.; Ricciuti, R.:** "The probability of military rule in Africa, 1970-2007"
- 2011/27, **Solé-Ollé, A.; Viladecans-Marsal, E.:** "Local spending and the housing boom"
- 2011/28, **Simón, H.; Ramos, R.; Sanromá, E.:** "Occupational mobility of immigrants in a low skilled economy. The Spanish case"
- 2011/29, **Piolatto, A.; Trotin, G.:** "Optimal tax enforcement under prospect theory"
- 2011/30, **Montolio, D; Piolatto, A.:** "Financing public education when altruistic agents have retirement concerns"
- 2011/31, **García-Quevedo, J.; Pellegrino, G.; Vivarelli, M.:** "The determinants of YICs' R&D activity"
- 2011/32, **Goodspeed, T.J.:** "Corruption, accountability, and decentralization: theory and evidence from Mexico"
- 2011/33, **Pedraja, F.; Cordero, J.M.:** "Analysis of alternative proposals to reform the Spanish intergovernmental transfer system for municipalities"
- 2011/34, **Jofre-Monseny, J.; Sorribas-Navarro, P.; Vázquez-Grenno, J.:** "Welfare spending and ethnic heterogeneity: evidence from a massive immigration wave"
- 2011/35, **Lyytikäinen, T.:** "Tax competition among local governments: evidence from a property tax reform in Finland"
- 2011/36, **Brühlhart, M.; Schmidheiny, K.:** "Estimating the Rivalness of State-Level Inward FDI"
- 2011/37, **García-Pérez, J.I.; Hidalgo-Hidalgo, M.; Robles-Zurita, J.A.:** "Does grade retention affect achievement? Some evidence from Pisa"
- 2011/38, **Boffa, f.; Panzar, J.:** "Bottleneck co-ownership as a regulatory alternative"

- 2011/39, **González-Val, R.; Olmo, J.:** "Growth in a cross-section of cities: location, increasing returns or random growth?"
- 2011/40, **Anesi, V.; De Donder, P.:** "Voting under the threat of secession: accommodation vs. repression"
- 2011/41, **Di Pietro, G.; Mora, T.:** "The effect of the l'Aquila earthquake on labour market outcomes"
- 2011/42, **Brueckner, J.K.; Neumark, D.:** "Beaches, sunshine, and public-sector pay: theory and evidence on amenities and rent extraction by government workers"
- 2011/43, **Cortés, D.:** "Decentralization of government and contracting with the private sector"
- 2011/44, **Turati, G.; Montolio, D.; Piacenza, M.:** "Fiscal decentralisation, private school funding, and students' achievements. A tale from two Roman catholic countries"

---

2012

---

- 2012/1, **Montolio, D.; Trujillo, E.:** "What drives investment in telecommunications? The role of regulation, firms' internationalization and market knowledge"
- 2012/2, **Giesen, K.; Suedekum, J.:** "The size distribution across all "cities": a unifying approach"
- 2012/3, **Foremny, D.; Riedel, N.:** "Business taxes and the electoral cycle"
- 2012/4, **García-Estévez, J.; Duch-Brown, N.:** "Student graduation: to what extent does university expenditure matter?"
- 2012/5, **Durán-Cabré, J.M.; Esteller-Moré, A.; Salvadori, L.:** "Empirical evidence on horizontal competition in tax enforcement"
- 2012/6, **Pickering, A.C.; Rockey, J.:** "Ideology and the growth of US state government"
- 2012/7, **Vergolini, L.; Zanini, N.:** "How does aid matter? The effect of financial aid on university enrolment decisions"
- 2012/8, **Backus, P.:** "Gibrat's law and legacy for non-profit organisations: a non-parametric analysis"
- 2012/9, **Jofre-Monseny, J.; Marín-López, R.; Viladecans-Marsal, E.:** "What underlies localization and urbanization economies? Evidence from the location of new firms"
- 2012/10, **Mantovani, A.; Vandekerckhove, J.:** "The strategic interplay between bundling and merging in complementary markets"
- 2012/11, **García-López, M.A.:** "Urban spatial structure, suburbanization and transportation in Barcelona"
- 2012/12, **Revelli, F.:** "Business taxation and economic performance in hierarchical government structures"
- 2012/13, **Arqué-Castells, P.; Mohnen, P.:** "Sunk costs, extensive R&D subsidies and permanent inducement effects"
- 2012/14, **Boffa, F.; Piolatto, A.; Ponzetto, G.:** "Centralization and accountability: theory and evidence from the Clean Air Act"
- 2012/15, **Cheshire, P.C.; Hilber, C.A.L.; Kaplanis, I.:** "Land use regulation and productivity – land matters: evidence from a UK supermarket chain"
- 2012/16, **Choi, A.; Calero, J.:** "The contribution of the disabled to the attainment of the Europe 2020 strategy headline targets"
- 2012/17, **Silva, J.I.; Vázquez-Grenno, J.:** "The ins and outs of unemployment in a two-tier labor market"
- 2012/18, **González-Val, R.; Lanaspá, L.; Sanz, F.:** "New evidence on Gibrat's law for cities"
- 2012/19, **Vázquez-Grenno, J.:** "Job search methods in times of crisis: native and immigrant strategies in Spain"
- 2012/20, **Lessmann, C.:** "Regional inequality and decentralization – an empirical analysis"
- 2012/21, **Nuevo-Chiquero, A.:** "Trends in shotgun marriages: the pill, the will or the cost?"
- 2012/22, **Piil Damm, A.:** "Neighborhood quality and labor market outcomes: evidence from quasi-random neighborhood assignment of immigrants"
- 2012/23, **Ploeckl, F.:** "Space, settlements, towns: the influence of geography and market access on settlement distribution and urbanization"
- 2012/24, **Algan, Y.; Hémet, C.; Laitin, D.:** "Diversity and local public goods: a natural experiment with exogenous residential allocation"
- 2012/25, **Martinez, D.; Sjögren, T.:** "Vertical externalities with lump-sum taxes: how much difference does unemployment make?"
- 2012/26, **Cubel, M.; Sanchez-Pages, S.:** "The effect of within-group inequality in a conflict against a unitary threat"
- 2012/27, **Andini, M.; De Blasio, G.; Duranton, G.; Strange, W.C.:** "Marshallian labor market pooling: evidence from Italy"
- 2012/28, **Solé-Ollé, A.; Viladecans-Marsal, E.:** "Do political parties matter for local land use policies?"
- 2012/29, **Buonanno, P.; Durante, R.; Prarolo, G.; Vanin, P.:** "Poor institutions, rich mines: resource curse and the origins of the Sicilian mafia"
- 2012/30, **Anghel, B.; Cabrales, A.; Carro, J.M.:** "Evaluating a bilingual education program in Spain: the impact beyond foreign language learning"



- 2012/31, **Curto-Grau, M.; Solé-Ollé, A.; Sorribas-Navarro, P.:** "Partisan targeting of inter-governmental transfers & state interference in local elections: evidence from Spain"
- 2012/32, **Kappeler, A.; Solé-Ollé, A.; Stephan, A.; Väilä, T.:** "Does fiscal decentralization foster regional investment in productive infrastructure?"
- 2012/33, **Rizzo, L.; Zanardi, A.:** "Single vs double ballot and party coalitions: the impact on fiscal policy. Evidence from Italy"
- 2012/34, **Ramachandran, R.:** "Language use in education and primary schooling attainment: evidence from a natural experiment in Ethiopia"
- 2012/35, **Rothstein, J.:** "Teacher quality policy when supply matters"
- 2012/36, **Ahlfeldt, G.M.:** "The hidden dimensions of urbanity"
- 2012/37, **Mora, T.; Gil, J.; Sicras-Mainar, A.:** "The influence of BMI, obesity and overweight on medical costs: a panel data approach"
- 2012/38, **Pelegrín, A.; García-Quevedo, J.:** "Which firms are involved in foreign vertical integration?"
- 2012/39, **Agasisti, T.; Longobardi, S.:** "Inequality in education: can Italian disadvantaged students close the gap? A focus on resilience in the Italian school system"

---

## 2013

---

- 2013/1, **Sánchez-Vidal, M.; González-Val, R.; Viladecans-Marsal, E.:** "Sequential city growth in the US: does age matter?"
- 2013/2, **Hortas Rico, M.:** "Sprawl, blight and the role of urban containment policies. Evidence from US cities"
- 2013/3, **Lampón, J.F.; Cabanelas-Lorenzo, P.; Lago-Peñas, S.:** "Why firms relocate their production overseas? The answer lies inside: corporate, logistic and technological determinants"
- 2013/4, **Montolio, D.; Planells, S.:** "Does tourism boost criminal activity? Evidence from a top touristic country"
- 2013/5, **García-López, M.A.; Holl, A.; Viladecans-Marsal, E.:** "Suburbanization and highways: when the Romans, the Bourbons and the first cars still shape Spanish cities"
- 2013/6, **Bosch, N.; Espasa, M.; Montolio, D.:** "Should large Spanish municipalities be financially compensated? Costs and benefits of being a capital/central municipality"
- 2013/7, **Escardíbul, J.O.; Mora, T.:** "Teacher gender and student performance in mathematics. Evidence from Catalonia"
- 2013/8, **Arqué-Castells, P.; Viladecans-Marsal, E.:** "Banking towards development: evidence from the Spanish banking expansion plan"
- 2013/9, **Asensio, J.; Gómez-Lobo, A.; Matas, A.:** "How effective are policies to reduce gasoline consumption? Evaluating a quasi-natural experiment in Spain"
- 2013/10, **Jofre-Monseny, J.:** "The effects of unemployment benefits on migration in lagging regions"
- 2013/11, **Segarra, A.; García-Quevedo, J.; Teruel, M.:** "Financial constraints and the failure of innovation projects"
- 2013/12, **Jerrim, J.; Choi, A.:** "The mathematics skills of school children: How does England compare to the high performing East Asian jurisdictions?"
- 2013/13, **González-Val, R.; Tirado-Fabregat, D.A.; Viladecans-Marsal, E.:** "Market potential and city growth: Spain 1860-1960"
- 2013/14, **Lundqvist, H.:** "Is it worth it? On the returns to holding political office"
- 2013/15, **Ahlfeldt, G.M.; Maennig, W.:** "Homevoters vs. leasevoters: a spatial analysis of airport effects"
- 2013/16, **Lampón, J.F.; Lago-Peñas, S.:** "Factors behind international relocation and changes in production geography in the European automobile components industry"
- 2013/17, **Guío, J.M.; Choi, A.:** "Evolution of the school failure risk during the 2000 decade in Spain: analysis of Pisa results with a two-level logistic model"
- 2013/18, **Dahlby, B.; Rodden, J.:** "A political economy model of the vertical fiscal gap and vertical fiscal imbalances in a federation"
- 2013/19, **Acacia, F.; Cubel, M.:** "Strategic voting and happiness"
- 2013/20, **Hellerstein, J.K.; Kutzbach, M.J.; Neumark, D.:** "Do labor market networks have an important spatial dimension?"
- 2013/21, **Pellegrino, G.; Savona, M.:** "Is money all? Financing versus knowledge and demand constraints to innovation"
- 2013/22, **Lin, J.:** "Regional resilience"
- 2013/23, **Costa-Campi, M.T.; Duch-Brown, N.; García-Quevedo, J.:** "R&D drivers and obstacles to innovation in the energy industry"

**2013/24, Huisman, R.; Stradnic, V.; Westgaard, S.:** "Renewable energy and electricity prices: indirect empirical evidence from hydro power"

**2013/25, Dargaud, E.; Mantovani, A.; Reggiani, C.:** "The fight against cartels: a transatlantic perspective"

