Public debt and economic growth: Further evidence for the euro area*

(Short running title: Public debt and economic growth)

Marta Gómez-Puig, Simón Sosvilla-Rivero

aDepartment of Economics and Riskcenter, Universitat de Barcelona. 08034 Barcelona, Spain

bComplutense Institute for International Studies, Universidad Complutense de Madrid. 28223 Madrid, Spain

Abstract

This paper empirically investigates the short and long run impact of public debt on economic growth. We use annual data from both central and peripheral countries of the euro area (EA) for the 1961-2013 period and estimate a production function augmented with a debt stock term by applying the Autoregressive Distributed Lag (ARDL) bounds testing approach. Our results suggest different patterns across EA countries and tend to support the view that public debt always has a negative impact on the long-run performance of EA member states, whilst its short-run effect may be positive depending on the country.

Keywords: Public debt, economic growth, bounds testing, euro area, peripheral euro area countries, central euro area countries.

JEL Classification Codes: C22, F33, H63, O40, O52

* Corresponding author. Tel.: +34 913942342; fax: +34 913942591. Department of Quantitative Economics, Universidad Complutense de Madrid. Campus de Somosaguas, 28223 Madrid, Spain. Spain. E-mail addresses: marta.gomezpuig@ub.edu (M.Gómez-Puig), sosvilla@ccee.ucm.es (S. Sosvilla-Rivero)

The authors wish to thank an anonymous referee and the editor for their helpful comments and suggestions on a previous draft of this article, which have enabled us to introduce substantial improvements. This paper is based upon work supported by the Instituto de Estudios Fiscales [grants IEF 101/2014 and IEF 015/2017], the Banco de España [grant PR71/15-20229], the Spanish Ministry of Education, Culture and Sport [grant PRX16/00261] and the Spanish Ministry of Economy and Competitiveness [grant ECO2016-76203-C2-2-P]. Simón Sosvilla-Rivero thanks the members of the Department of Economics at the University of Bath for their hospitality during his research visit. Responsibility for any remaining errors rests with the authors.
1. Introduction

The origin of the sovereign debt crisis in the euro area (EA) goes deeper than the fiscal imbalances in member states. Some authors have pointed out that the EA faced three interlocking crises – banking, sovereign debt, and economic growth – which together challenged the viability of the currency union. Despite its relevance, an analysis of the interrelationship between sovereign and banking risk is beyond the scope of this paper. Rather, since the crisis led to an unprecedented increase in sovereign debt in EA countries\(^1\) we will focus on the interconnection between sovereign debt and growth in 11 of them, both central (Austria, Belgium, Finland, France, Germany and the Netherlands) and peripheral member states (Greece, Ireland, Italy, Portugal, and Spain). There is a widespread consensus on the potentially adverse consequences of high levels of public debt for these countries’ economic growth, but few macroeconomic policy debates have caused as much disagreement as the current austerity argument.

Overall, the theoretical literature favours the study of the effects of very high debt on the capital stock, growth, and risk, since it tends to point to a negative link between the public debt-to-Gross Domestic Product (GDP) ratio and the steady-state growth rate of GDP (see, for instance, Aizenman et al., 2007). However, it also stresses not only that the impact of debt on output may differ depending on the time horizon – while debt may crowd out capital and reduce output in the long run, in the short run it can stimulate aggregate demand and output [see Barro (1990), Elmendorf and Mankiw (1999) or Salotti and Trecroci (2016)] – but also that the presence of a tipping point, above which an increase in public debt has a detrimental effect on economic performance, does not mean that it has to be common across countries [see Ghosh et al. (2013) or Eberhardt and Presbitero (2015)]. The latter authors indicate that there may be at least three reasons for the differences in the

\(^1\) By the end of 2013, on average, public debt reached about 100% of GDP in EA countries – its highest level in 50 years.
relationships between public debt and growth across countries: (1) Production technology may differ; (2) The capacity to tolerate high levels of debt may depend on a number of country-specific characteristics related to the macro and institutional framework; and (3) Vulnerability to public debt may depend not only on debt levels, but also on debt composition.

Nevertheless, although the relevance of the heterogeneity of the debt-growth nexus (both across countries and time periods) has been stressed by the literature, and although certain authors have presented empirical analyses of this issue, hardly any empirical studies have examined the topic in EA countries. While there is a substantial body of research exploring the interconnection between debt and growth in both developed and emerging countries, few papers to date have looked at this link in the context of the EA. These exceptions make use of panel data techniques to obtain average results for EA countries, and do not distinguish between countries or between short and long run effects.

In this context, this paper presents a new approach to add to the as yet small body of literature on the relationship between public debt accumulation and economic performance in EA countries, by examining the potential heterogeneity in the debt-growth nexus both across different EA countries and across time horizons. Therefore, our contribution to the empirical literature is twofold. First, unlike previous studies, we do not make use of panel estimation techniques to combine the power of cross section averaging with all the subtleties of temporal dependence; rather, we explore the time series dimension of the issue to obtain further evidence based on the historical experience of each country in the sample in order to detect potential heterogeneities in the relationship across EA countries. Second, our econometric methodology is data-driven, and it allows us to select the statistical model that best approximates the relationship between the variables under study.
for any particular country and to assess both the short and long-run effects of public debt on output performance.

The rest of the paper is organized as follows. Section 2 justifies our empirical approach on the basis of a review of the existing literature. Section 3 presents the analytical framework of the analysis and outlines the econometric methodology. Section 4 describes our data. Empirical results are presented in Section 5. Finally, Section 6 summarizes the findings and offers some concluding remarks.

2. Literature review

Under what conditions is debt growth-enhancing? This challenging question has been studied by economists for a long time, but has recently undergone a notable revival fuelled by the substantial deterioration of public finances in many economies as a result of the financial and economic crisis of 2008-2009.

From the theoretical perspective, there is no consensus regarding the sign of the impact of public debt on output in either the short or the long run. The “conventional” view (Elmendorf and Mankiw, 1999) states that in the short run, since output is demand-determined, government debt (manifesting deficit financing) can have a positive effect on disposable income, aggregate demand, and overall output. Moderate levels of debt are found to have a positive short-run impact on economic growth through a range of channels: improved monetary policy, strengthened institutions, enhanced private savings, deepened financial intermediation (Abbas and Christensen, 2007) or smoothed distortionary taxation over time (Barro, 1979). This positive short-run effect of budget deficits (and higher debt) is likely to be large when the output is far from capacity. However, things are different in the long run if the decrease in public savings brought about by a higher budget deficit is not fully compensated by an increase in private savings.
In this situation, national savings will decrease and total investment will fall; this will have a negative effect on GDP as it will reduce capital stock, increase interest rates, and reduce labour productivity and wages. The negative effect of an increase in public debt on future GDP can be amplified if high public debt increases uncertainty or leads to expectations of future confiscation, possibly through inflation and financial repression (see Cochrane, 2011).

The above “conventional” split between the short and long-run effects of debt disregards the fact that protracted recessions may reduce future potential output (as they increase the number of discouraged workers, with the associated loss of skills, and have a negative effect on organizational capital and investment in new activities). There is, in fact, evidence that recessions have a permanent effect on the level of future GDP (see, e.g., Cerra and Saxena, 2008), which implies that running fiscal deficits (and increasing debt) may have a positive effect on output in both the short and the long run. DeLong and Summers (2012) argue that, in a low interest rate environment, an expansionary fiscal policy is likely to be self-financing.

Finally, another strand of the literature also departs from the “conventional” view and establishes a link between the long-term effect of debt and the kind of public expenditure it funds. The papers by Devarajan et al. (1996) and Aschauer (1989), for instance, state that in the long run, the impact of debt on the economy’s performance depends on whether the public expenditure funded by government debt is productive or unproductive. Whilst the former (which includes physical infrastructure such as roads and railways, communication, information systems such as phone, internet, and education) may have a positive impact on the economy’s growth, the latter does not affect the economy’s long-run performance, although it may have positive short-run implications.
From the empirical perspective, the results from the literature on the relationship between public debt and economic growth are far from conclusive either [see Panizza and Presbitero (2013) or the technical Appendix in Eberhardt and Presbitero (2015) for two excellent summaries of this literature]. Some authors (Reinhart and Rogoff, 2010 or Pattillo et al., 2011) present empirical evidence indicating that the relationship is described by an inverted U-shaped pattern (low levels of public debt positively affect economic growth, but high levels have a negative impact). However, other empirical studies reach very different conclusions. While some of them find no evidence for a robust effect of debt on growth (Lof and Malinen, 2014), others detect an inverse relationship between the two variables (Woo and Koomar, 2015) or contend that the relationship between them is mitigated crucially by the quality of a country’s institutions (Kourtellos et al., 2013).

In the EA context, in a situation in which leverage was already very high, the recent economic recession and sovereign debt crisis has stimulated an intense debate both on the effectiveness of fiscal policies and on the possible adverse consequences of the accumulation of public debt in EA countries. Few macroeconomic policy debates have generated as much controversy as the current austerity argument, not only because pundits draw widely different conclusions for macroeconomic policy, but also because economists have not reached a consensus (see Alesina et al. 2015). Some suggest that now is precisely the time to apply the lessons learnt during the Great Depression and that policymakers should implement expansionary fiscal policies [Krugman (2011) or DeLong and Summers (2012)] since fiscal austerity may have been the main culprit for the recessions experienced by European countries; others argue that, since the high level of public sector leverage has a negative effect on economic growth, fiscal consolidation is fundamental to restoring confidence and improving expectations about the future evolution of the economy and therefore its rate of growth [Cochrane (2011) or Teles and Mussolini (2014)].
In our reading of the empirical evidence, few papers have examined the relationship between debt and growth for EA countries despite the effects of the severe sovereign debt crisis in several member states. Checherita-Westphal and Rother (2012) and Baum *et al.* (2013) analyse the non-linearities of the debt-growth nexus estimating a standard growth model and employing a panel approach. In contrast, Dreger and Reimers (2013) base their analysis on the distinction between sustainable and non-sustainable debt periods. Overall, this empirical literature lends support to the presence of a common debt threshold across (similar) countries like those in the EA, and does not distinguish between short- and-long run effects.

Therefore, to our knowledge, no strong case has yet been made for analysing the effect of debt accumulation on economic growth taking into account the particular characteristics of each EA economy and examining whether the effects differ depending on the time horizon, in spite of the fact that this potential heterogeneity has been stressed by the literature. For instance, Eberhardt and Presbitero (2015) and Êgert (2015) support the existence of nonlinearity in the debt-growth nexus, but state that there is no evidence at all for a threshold level common to all countries over time; while Gómez-Puig and Sosvilla-Rivero (2015) and Donayre and Taivan (2017), who analyse the causal relationship between public debt and economic growth, also suggest that the causal link is intrinsic to each country.

3. **Analytical framework and econometric methodology**

An important line of research, based on the empirical growth literature (e.g., Barro and Sala-i-Martin, 2004), has considered growth regressions augmented by public debt to assess whether the latter has an impact on growth over and above other determinants – population growth, human capital, financial development, innovation intensity, openness to
trade, fiscal indicators, saving or investment rate and macroeconomic uncertainty, to name just a few — (see, e.g., Cecchetti et al., 2011; Pattillo et al., 2011; or Checherita-Westphal and Rother, 2012)

Our empirical strategy departs from this approach and explores the debt–growth nexus using an aggregate production function augmented by adding a debt variable. This allows us to test the impact of debt after controlling for the basic drivers of growth: the stock of physical capital, the labour input and a measure of human capital. The stock of physical capital and the labour input have been the two key determinants of economic growth since Solow’s classic model (1956) and many empirical studies have examined their relationship with economic growth (see, e.g., Frankel, 1962). Regarding human capital, Becker (1962) stated that investment in human capital contributed to economic growth by investing in people through education and health, and Mankiw et al. (1992) augmented the Solow model by including accumulation of human as well as physical capital (see Savvides and Stengos, 2009).

Therefore, we extend Eberhardt and Presbitero (2015)’s approach and consider the following aggregate production function, in which public debt is included as a separate factor of production:\(^2\):

\[
Y_t = AF(K_t, L_t, H_t, D_t)
\]

(1)

where \(Y\) is the level of output, \(A\) is an index of technological progress, \(K\) is the stock of physical capital, \(L\) is the labour input, \(H\) is the human capital, and \(D\) is the stock of public debt.

For simplicity, the technology is assumed to be of the Cobb-Douglas form:

\(^2\) Eberhardt and Presbitero (2015) do not consider \(H\) in the basic equation of interest for their analysis of the debt–growth nexus.
\[ Y_t = AK_t^{\alpha} L_t^{\alpha} H_t^{\alpha} D_t^{\alpha} \quad (2) \]

so that, after taking logs and denoting by a small letter the log of its corresponding capital letter, we obtain

\[ y_t = \alpha + \alpha_k k_t + \alpha_l l_t + \alpha_h h_t + \alpha_d d_t \quad (3) \]

As can be seen, equation (3) postulates a long-run relationship between (the log of) the level of production \( y_t \), (the log of) the stock of physical capital \( k_t \), (the log of) the labour employed \( l_t \), (the log of) the human capital \( h_t \) and (the log of) the stock of public debt \( d_t \). In contrast to Eberhardt and Presbitero (2015), we do not impose any constraint regarding the returns to scale of production factors in the production function.

Equation (3) can be estimated from sufficiently long-time series by cointegration econometric techniques. In this paper, we make use of the Autoregressive Distributed Lag (ARDL) bounds testing approach to cointegration proposed by Pesaran and Shin (1999) and Pesaran, Shin and Smith (2001). This approach presents at least three significant advantages over the two alternatives commonly used in the empirical literature: the single-equation procedure developed by Engle and Granger (1987) and the maximum likelihood method postulated by Johansen (1991, 1995) which is based on a system of equations. First, both these approaches require the variables under study to be integrated of order 1; this inevitably requires a previous process of tests on the order of integration of the series, which may lead to some uncertainty in the analysis of long-run relations. In contrast, the ARDL bounds testing approach allows the analysis of long-term relationships between variables, regardless of whether they are integrated of order 0 [I(0)], of order 1 [I(1)] or mutually cointegrated. This avoids some of the common pitfalls faced in the empirical analysis of time series, such as the lack of power of unit root tests and doubts about the order of integration of the variables examined (Pesaran et al., 2001). Second, the ARDL
bounds testing approach allows a distinction to be made between the dependent variable and the explanatory variables, an obvious advantage over the method proposed by Engle and Granger; at the same time, like the Johansen approach, it allows simultaneous estimation of the short-run and long-run components, eliminating the problems associated with omitted variables and the presence of autocorrelation. Finally, while the estimation results obtained by the methods proposed by Engle and Granger and Johansen are not robust to small samples, Pesaran and Shin (1999) show that the short-run parameters estimated using their approach are $\sqrt{T}$-consistent and that the long-run parameters are super-consistent in small samples.

In our particular case, the application of the ARDL approach to cointegration involves estimating the following unrestricted error correction model (UECM):

$$
\Delta y_t = \beta + \sum_{i=1}^{p} \gamma_i \Delta y_{t-i} + \sum_{i=1}^{q_1} \phi_{i1} \Delta k_{t-i} + \sum_{i=1}^{q_2} \phi_{i2} \Delta l_{t-i} + \sum_{i=1}^{q_3} \phi_{i3} \Delta h_{t-i} + \sum_{i=1}^{q_4} \phi_{i4} \Delta d_{t-i} + \\
+ \lambda_1 y_{t-1} + \lambda_2 k_{t-1} + \lambda_3 l_{t-1} + \lambda_4 h_{t-1} + \lambda_5 d_{t-1} + \varepsilon_t
$$

(4)

where $\Delta$ denotes the first difference operator, $\beta$ is the drift component, and $\varepsilon_t$ is assumed to be a white noise process. Note that $p$ is the number of lags of the dependent variable and $q_i$ is the number of lags of the $i$-th explanatory variable. The optimal lag structure of the first differenced regression (4) is selected by the Akaike Information Criterion (AIC) and the Schwarz Bayesian Criterion (SBC) to simultaneously correct for residual serial correlation and the problem of endogenous regressors (Pesaran and Shin, 1999, p. 386). In order to determine the existence of a long-run relationship between the variables under study, Pesaran, Shin and Smith (2001) propose two alternative tests. First, an $F$-statistic is used to test the joint significance of the first lag of the variables in levels used in the
analysis (i.e. $\lambda_1 = \lambda_2 = \lambda_3 = \lambda_4 = \lambda_5 = 0$), and then a \textit{t-statistic} is used to test the individual significance of the lagged dependent variable in levels (i.e. $\lambda = 0$).

Based on two sets of critical values: I(0) and I(1) (Pesaran, Shin, and Smith 2001), if the calculated $F$- or \textit{t}-statistics exceed the upper bound I(1), we conclude in favour of a long-run relationship, regardless of the order of integration. However, if these statistics are below the lower bound I(0), the null hypothesis of no cointegration cannot be rejected. Finally, if the calculated $F$- and \textit{t}-statistics fall between the lower and the upper bound, the results are inconclusive.

If cointegration exists, the conditional long-run model is derived from the reduced form equation (4) when the series in first differences are jointly equal to zero (i.e., $\Delta y = \Delta k = \Delta l = \Delta d = 0$). The calculation of these estimated long-run coefficients is given by:

$$y_t = \delta_0 + \delta_1 k_t + \delta_2 l_t + \delta_3 d_t + \xi_t$$ \hspace{1cm} (5)

Finally, if a long-run relation is found, an error correction representation exists which is estimated from the following reduced form equation:

$$\Delta y_t = \sum_{i=1}^{q_1} \theta_i \Delta y_{t-i} + \sum_{i=1}^{q_2} \sigma_i \Delta k_{t-i} + \sum_{i=1}^{q_3} \tau_i \Delta l_{t-i} + \sum_{i=1}^{q_4} \psi_i \Delta d_{t-i} + \eta_{ECM_{t-i}}$$ \hspace{1cm} (6)

4. Data

We estimate equation (4) with annual data for eleven EA countries: both central (Austria, Belgium, Finland, France, Germany and the Netherlands) and peripheral member states (Greece, Ireland, Italy, Portugal and Spain). Even though the ARDL-based estimation procedure used in the paper can be reliably used in small samples, we use long spans of data covering the period 1961-2013 (i.e., a total of 52 annual observations) to explore the
dimension of historical specificity and to capture the long-run relationship associated with
the concept of cointegration (see, e.g., Hakkio and Rush, 1991).

To maintain as much homogeneity as possible for a sample of 11 countries over the course
of five decades, our primary source is the European Commission’s AMECO database.
We then strengthen our data with the use of supplementary data sourced from
International Monetary Fund (International Financial Statistics) and the World Bank
(World Development Indicators). We use GDP, net capital stock and public debt (all
expressed at 2010 market prices) for \( Y, K \) and \( D \), as well as civilian employment and life
expectancy at birth for \( L \) and \( H \).

5. Empirical Results

5.1. Time series properties

Before carrying out the ARDL cointegration exercise, we test for the order of integration
of the variables by means of the Augmented Dickey-Fuller (ADF) tests. This is necessary
just to ensure that none of our variables are only stationary at second differences, since the
ARDL bounds test fails to provide robust results in the presence of I(2) variables. The
results decisively reject the null hypothesis of non-stationarity, suggesting that all variables
can be treated as first-difference stationary. Then, following Cheung and Chinn’s (1997)

---

3 http://ec.europa.eu/economy_finance/db_indicators/ameco/index_en.htm
4 Following Sachs and Warner (1997), we use life expectancy at birth as the human-capital proxy. Other proxies commonly
used for human capital such as years of secondary education, enrolment at secondary school and measures of human
capital using a Mincerian equation (e.g. Morrisson and Murtin, 2007) were available on homogenous form for all EA
countries under study only from 1980. Additionally, the proxy years of secondary education did not change during the
sample period. As shown in Jayachandran and Lleras-Muney (2009), longer life expectancy encourages human capital
accumulation, since a longer time horizon increases the value of investments that pay out over time. Moreover, better
health and greater education are complementary with longer life expectancy (Becker, 2007). We also considered the index
of human capital per person provided by the Penn World Table (version 8.0, Feenstra et al., 2013), based on years of
schooling (Barro and Lee, 2013) and returns to education (Psacharopoulos, 1994). This index is only available until 2011
and, for the countries under study, is a I(2) variable that cannot be included in our analysis. Nevertheless, life expectancy
at birth correlates strongly with the index of human capital per person during the 1961-2011 period.
5 We summarize the results by pointing out the main regularities and focusing on public debt. The reader is asked to
browse through Tables 1 and 2 to find evidence for a particular country of her/his special interest.
6 These results (not shown here in order to save space, but available from the authors upon request) were confirmed using
suggestion, we confirm these results using the Kwiatkowski et al. (1992) (KPSS) tests, where the null is a stationary process against the alternative of a unit root. The single order of integration of the variables encourages the application of the ARDL bounds testing approach to examine the long-run relationship between the variables.

5.2. Empirical results from the ARDL bounds test

The estimation proceeds in stages. In the first stage, we specify the optimal lag length for the model (in this stage, we impose the same number of lags on all variables as in Pesaran, Shin and Smith, 2001). The ARDL representation does not require symmetry of lag lengths; each variable may have a different number of lag terms. As mentioned above, we use the AIC and SBC information criteria to guide our choice of the lag length, selecting 4 as the maximum number of lags both for the dependent variable and the regressors. For the test of serial correlation in the residual, we use the maximum likelihood statistics for the first and fourth autocorrelation, denoted as $\chi^2_{SC}(1)$ and $\chi^2_{SC}(4)$ respectively. Due to constraints of space, these results are not shown here but they are available from the authors upon request.

Next, we test for the existence of a long-run relation between the output and its components, as suggested by equation (3).

[Insert Table 1 here]

Panel A in Table 1 gives the values of the $F$- and $t$-statistics for the case of unrestricted intercepts and no trends (case III in Pesaran, Shin and Smith, 2001). These statistics are

---

Optimal and Ng and Perron (2001) unit root tests for testing non-stationarity against the alternative of high persistence. These additional results are also available from the authors.

7 The results are not shown here due to space restrictions but are available from the authors upon request.

8 Since the hypothesis of the expected values of the first differences of the series is equal to zero cannot be rejected, there is no evidence of linear deterministic trends in the data. Therefore, we conclude that the cointegrating relationship should be formulated with the constant term unrestricted and without deterministic trend terms (case III). Nevertheless, we also consider two additional scenarios for the deterministics: unrestricted intercepts, restricted trends; and unrestricted intercepts, unrestricted trends (cases IV and V in Pesaran, Shin and Smith, 2001). These additional results are not shown.
compared with the critical value bounds provided in Tables C I and C II of Pesaran, Shin and Smith (2001) and depend on whether an intercept and/or trend is included in the estimations, suggesting the existence of a single long-term relationship in which the production level would be the dependent variable and the stock of physical capital, the labour employed, the human capital and the stock of public debt the independent variables. Then, the estimated long-run relationships between the variables are reported in Panel B in Table 1.

Some very interesting results can be drawn from the empirical evidence presented in Table 1. First, the long-term effect of debt on economic performance is in line with the findings in previous empirical literature based on panel data techniques, since it registers a negative value in all EA countries. However, the magnitude of the negative impact differs significantly across countries, implying that our conclusions need to be qualified. While comparatively high impacts are estimated in the case of France (-0.544), Portugal (-0.354), Spain (-0.336), and Austria (-0.129), in the rest of countries, although negative, the magnitude is very small with values close to zero. Ireland (-0.049), Finland (-0.049) and Germany (-0.040) are the countries with the lowest negative impact. Therefore, our results suggest that, even though debt has a long run negative impact on output in all EA countries, with the exception of France, Portugal, Spain and Austria its magnitude is negligible.

In order to examine the short-term dynamics of the model, we estimate an error-correction model associated with the above long-run relationship. As can be seen in Table 2, the short-run impact of debt on economic performance differs clearly across countries, both in terms of the estimated coefficients for $\Delta d_t$ and in terms of the significance of lagged terms here due to space constraints, but they are available from the authors upon request. Our estimation results indicate that the intercepts are always statistically significant, whereas the trends are not.
of $Δd$. In order to compare results, we follow Hendry (1995)’s suggestion and calculate the short-term effects of debt on growth as follows for the significant coefficients:

$$\text{short-term effects} = \frac{\sum_{i=1}^{q_i} \psi_i}{(1 - \sum_{i=1}^{p_i} \theta)}$$

(7)

[Insert Table 2 here]

Table 2 shows that with respect to peripheral EA countries, in spite of the important long-run negative impact in Portugal and Spain, the short-term effect is positive (0.063 and 0.067), although quite small. However, in Greece, Ireland and Italy an increase in public debt has a negative effect on GDP, not only in the long run but in the short run as well. Among central EA countries, it is noticeable that in Germany and Finland the effect of public debt on GDP is positive in the short run (0.375 and 0.059) despite the negative (though very small) effect in the long run. Finally, in the case of Austria, Belgium, France and the Netherlands our results suggest that public debt has a negative impact on economic activity in both the short and the long run.

All in all, it should be noted that we do not find a positive long-run relationship between public debt and output in any country, although the short-run link is positive in four EA countries. Interestingly, in two peripheral countries, Spain and Portugal, while debt exerts an important negative effect on the long run, its impact, although small, is positive in the short run. These results are in line with some recent literature which has investigated how different country characteristics (e.g., the state of the public finances, the health of the financial sector or the degree of openness to trade) might influence the size of fiscal multipliers. In particular, Corsetti et al. (2012) and Ilzetzki et al. (2013) find that negative multipliers can be observed in high-debt countries (i.e., with debt-to-GDP ratios above 60%), but they could be much larger in countries under sound public finances. Furthermore, Eberhart and Presbitero (2015) stress that one of the reasons that explains
the differences in the relationships between public debt and growth across countries is the
dependence of vulnerability to public debt on current debt levels. Among peripheral EA
countries, only Portugal and Spain registered an average debt ratio below the 60% threshold during the 1961-2013 period (37% and 35% respectively), while the debt ratio
was also moderate in Finland and Germany (28% and 40% on average). Therefore, our
results confirm that in countries with low or moderate indebtedness levels (i.e., in a
sustainable public debt context, see Dreger and Reiners, 2013), an additional increase in
public debt might exert a short-run positive effect on GDP. These findings are highly
relevant since these two peripheral countries have been hit especially hard by both the
economic and sovereign debt crises. And, amid the crisis, they received rescue packages (in
the Spanish case, to save its banking sector) which were conditional on the implementation
of structural reforms to improve competitiveness and highly controversial fiscal austerity
measures (whose positive effects are nevertheless typically related to the long run).

Although our results must be regarded with caution since they present the average effects
over the 50-year estimated period, they do not seem to favour the same austerity argument
in all EA countries. In particular, they indicate that, in the short term, expansionary fiscal
policies may not have a negative effect on output – but a marginal positive one – in some
countries such as Spain and Portugal, regardless of its large negative impact in the long run.
Then, although our findings support the view that the unprecedented sovereign debt levels
reached in EA countries might have adverse consequences for their economies in the long
run, they also suggest that the pace of adjustment may differ across these countries. In
particular, within peripheral EA countries, policymakers should bear in mind that while the
short-run impact of debt on economic performance is negative in Greece, Ireland and Italy,
it is slightly positive in Spain and Portugal.
Regarding the estimated coefficients for the error correction terms (ECM,.) representing the speed of adjustment needed to restore equilibrium in the dynamic model following a disturbance, Table 2 shows that they range from -0.301 to -0.543 for the central countries (suggesting that, with the exception of Belgium and the Netherlands, more than half of the disequilibrium is corrected within one year), while ranging from -0.129 to -0.262 for the peripheral EA countries (suggesting relatively slow reactions to deviations from equilibrium and implying that short-term effects may dominate at longer horizons), corroborating the above results. Besides, the highly significant estimated error correction terms provide further support for the existence of stable long-run relationships such as those reported in Table 1 (Banerjee et al., 1998).

As Table 2 indicates, the short-run analysis seems to pass diagnostic tests such as normality of error term, second-order residual autocorrelation and heteroskedasticity ($\chi^2_N, \chi^2_{SC}$ and $\chi^2_H$ respectively). The regressions fit reasonably well, with $R^2$ values ranging from 0.625 for France to 0.895 for Finland.

The estimated parameters presented in Table 2 are average values for the entire sample period (1961-2013) and do not take into account the possibility that they could change over time if a structural break occurred\(^9\). Therefore, we also explore the possibility of multiple structural changes in the parameter relating the public debt variable to the real growth rate ($\psi_t$) in equation (6) by using the Bai and Perron (1998) test. The results (not shown here to save space, but available from the authors upon request) seem to suggest strongly that there are two structural breaks in each of the estimated models. Re-estimating the regression model including a dummy variable that incorporates the detected breakpoints and gauge whether structural breaks have disturbed the effect of public debt on the real growth rate, we find very different results across central and peripheral countries. Regarding central EA

\(^9\) We are grateful to an anonymous referee for suggesting this analysis.
countries, with the exception of France, in countries where debt had a negative short-run effect on growth (Austria, Belgium, and the Netherlands), these inverse relationships between debt and growth seem to strengthen throughout the detected regimes. However, in Germany and Finland (where debt had a positive short-run effect on growth), we only detect a positive relationship between these two variables during the first regime (i.e., before the first break point). Subsequently, debt also exerts a negative effect on growth in Germany and Finland respectively. All in all, our results seem to suggest that the debt-to-GDP ratio at which public debt exerts the strongest negative impact on economic growth changes over time and across EA countries.

6. Concluding remarks

Despite the severe sovereign debt crisis in the EA, few papers have examined the relationship between debt and growth for member states. The limited body of literature available lends support to the presence of a common debt threshold across EA countries and does not distinguish between short and long-run effects. To our knowledge, no strong case has yet been made for analysing the incidence of debt accumulation on economic growth taking into account the particular characteristics of each EA economy and examining whether the effects differ depending on the time horizon, even though this potential heterogeneity has been stressed by the literature.

This paper aims to fill this gap. Unlike previous studies in the EA, we do not make use of panel techniques but study cross-country differences in the debt-growth nexus both across EA countries and across time horizons using time series analyses. To this end, our empirical examination of 11 member states (both central and peripheral) during the 1961-2013 period is based on the estimation, for each country, of a log-linearized Cobb–Douglas

---

10 These additional results are not shown here to save space, but they are available from the authors upon request
production function augmented with a debt stock term, by means of the ARDL testing approach to cointegration.

As in every empirical analysis, the results must be regarded with caution since they are based on a set of countries over a certain period and a given econometric methodology. This is particularly true of the comparison of the results with those of previous papers, since we adopt a time series analysis instead of a panel data approach, and since we use an analytical framework based on a production function augmented with public debt instead of growth regressions augmented by public debt. Nonetheless, our findings are in concordance with the predominant view that the positive effect of debt on output is more likely to be felt in the short rather than in the long run. In particular, our empirical evidence suggests a negative effect of public debt on output in the long run. Thus, our results support previous reports indicating that high public debt tends to hamper growth by increasing uncertainty over future taxation, crowding out private investment, and weakening a country’s resilience to shocks (see, e.g., Krugman, 1988). However, they detect the possibility that a public debt increase may have a positive effect in the short run by raising the economy’s productive capacity and improving efficiency depending on the characteristics of the country and the final allocation of public debt. Specifically, this short-run positive effect is found in Finland, Germany, Portugal and Spain, suggesting that in a context of low rates of economic growth, the path of fiscal consolidation may differ across the different EA countries.

This issue is particularly relevant to policymakers because of its implications for the effectiveness of a common fiscal policy, in view of the pronounced differences in the responsiveness of output in the long and short run and across countries. These findings seem to corroborate the idea that there is no “one size fits all” definition of fiscal space but
that, conversely, debt limits and fiscal space may be country-specific and depend on each country’s track record of adjustment (see, e. g., Ostry et al., 2010).

Extensions from the present research might take a number of directions. First, it would be interesting to examine possible non-linear effects (smooth or sudden structural changes) using the time-series approach applied in this paper to detect further potential heterogeneities among EA countries, complementing the evidence from existing literature using panel data techniques. A second natural extension to the analysis presented in this paper would be to further explore the main determinants of the detected differences in the relationships between public debt and economic growth across countries, with special emphasis on the economic and institutional factors suggested in Kourtellos et al. (2013) and in Eberhardt and Presbitero (2015). Both items are on our future research agenda.

References


Table 1. Long-run analysis

Panel A: Bound testing to cointegration

| ARDL(p,q1,q2,q3,q4) | AT      | BE      | FI      | FR      | GE      | GR      | IE      | IT      | NL      | PT      | SP      |
|---------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
|                     | (4, 3, 3, 4, 4) | (1, 2, 4, 4, 0) | (1, 4, 3, 1, 2) | (1, 0, 2, 4, 3) | (2, 1, 0, 2) | (1, 3, 0, 0, 0) | (1, 2, 1, 0, 0) | (2, 0, 0, 0, 0) | (3, 2, 0, 4, 1) | (1, 4, 3, 4, 4) | (1, 3, 3, 0, 2) | (1, 3, 2, 0, 3) |
| F-statistic         | 6.815** | 5.045** | 5.035** | 4.163** | 6.007** | 4.509** | 4.612** | 5.396** | 6.773** | 4.323** | 4.350** |

Panel B: Long-run coefficients

<table>
<thead>
<tr>
<th>Intercept</th>
<th>AT</th>
<th>BE</th>
<th>FI</th>
<th>FR</th>
<th>GE</th>
<th>GR</th>
<th>IE</th>
<th>IT</th>
<th>NL</th>
<th>PT</th>
<th>SP</th>
</tr>
</thead>
<tbody>
<tr>
<td>p</td>
<td>0.412*</td>
<td>0.398*</td>
<td>0.363*</td>
<td>0.450*</td>
<td>0.463*</td>
<td>0.155*</td>
<td>0.274*</td>
<td>0.232*</td>
<td>0.322*</td>
<td>0.174*</td>
<td>0.162*</td>
</tr>
<tr>
<td>q1</td>
<td>0.296*</td>
<td>0.396*</td>
<td>0.426*</td>
<td>0.429*</td>
<td>0.497*</td>
<td>0.245*</td>
<td>0.232*</td>
<td>0.312*</td>
<td>0.444*</td>
<td>0.330*</td>
<td>0.489*</td>
</tr>
<tr>
<td>q2</td>
<td>0.328*</td>
<td>0.452*</td>
<td>0.411*</td>
<td>0.428*</td>
<td>0.520*</td>
<td>0.312*</td>
<td>0.395*</td>
<td>0.472*</td>
<td>0.358*</td>
<td>0.373*</td>
<td>0.324*</td>
</tr>
<tr>
<td>q3</td>
<td>0.085*</td>
<td>0.421*</td>
<td>0.538*</td>
<td>0.507*</td>
<td>0.584*</td>
<td>0.346*</td>
<td>0.131*</td>
<td>0.142*</td>
<td>0.357*</td>
<td>0.205*</td>
<td>0.353*</td>
</tr>
<tr>
<td>q4</td>
<td>-0.129*</td>
<td>-0.062*</td>
<td>-0.049*</td>
<td>-0.544*</td>
<td>-0.040*</td>
<td>-0.079*</td>
<td>-0.049*</td>
<td>-0.083*</td>
<td>-0.097*</td>
<td>-0.354*</td>
<td>-0.336*</td>
</tr>
<tr>
<td></td>
<td>(-4.335)</td>
<td>(-5.512)</td>
<td>(-5.137)</td>
<td>(-5.867)</td>
<td>(-3.135)</td>
<td>(-3.135)</td>
<td>(-7.783)</td>
<td>(-8.623)</td>
<td>(-7.318)</td>
<td>(-8.336)</td>
<td>(-4.871)</td>
</tr>
</tbody>
</table>

Notes: AT, BE, FI, FR, GE, GR, IE, IT, NL, PT and SP stand for Austria, Belgium, Finland, France, Germany, Greece, Ireland, Italy, the Netherlands, Portugal and Spain respectively.
In Panel A, p, q1, q2, q3, q4 and q5 denote respectively the optimal lag length for Δyt, Δkt, Δlt, Δht, and Δlt in the UECM model (4) without deterministic trend.
* and ** indicate that the calculated F- and t-statistics are above the upper critical bound at 1% and 5% respectively.
In Panel B, in the ordinary brackets below the parameter estimates, the corresponding t-statistics are shown, while * denotes statistical significance at the 1% level.

24
Table 2. Short-run analysis

<table>
<thead>
<tr>
<th></th>
<th>AT</th>
<th>BE</th>
<th>FI</th>
<th>FR</th>
<th>GE</th>
<th>GR</th>
<th>IE</th>
<th>IT</th>
<th>NL</th>
<th>PT</th>
<th>SP</th>
</tr>
</thead>
<tbody>
<tr>
<td>( A_{h+2} )</td>
<td>0.336'</td>
<td>0.125'</td>
<td>0.282'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(4.959)</td>
<td>(3.401)</td>
<td>(3.912)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{h+2} )</td>
<td>0.227'</td>
<td>0.181'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(3.985)</td>
<td>(3.568)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{t-2} )</td>
<td>3.464'</td>
<td>3.914'</td>
<td>4.531'</td>
<td>5.308'</td>
<td>3.307'</td>
<td></td>
<td>1.942'</td>
<td></td>
<td></td>
<td>3.138'</td>
<td></td>
</tr>
<tr>
<td>( A_{t-2} )</td>
<td>1.641'</td>
<td>4.295'</td>
<td>2.949'</td>
<td>4.149'</td>
<td>3.409'</td>
<td>2.119'</td>
<td>1.563'</td>
<td></td>
<td></td>
<td>1.134'</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(3.228)</td>
<td>(6.552)</td>
<td>(4.897)</td>
<td>(4.252)</td>
<td>(5.691)</td>
<td>(5.544)</td>
<td>(5.202)</td>
<td></td>
<td></td>
<td>(5.022)</td>
<td></td>
</tr>
<tr>
<td>( A_{t-2} )</td>
<td>2.068'</td>
<td>0.895'</td>
<td>0.868'</td>
<td>0.644'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(3.829)</td>
<td>(3.121)</td>
<td>(3.688)</td>
<td>(3.052)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{h-2} )</td>
<td>0.512'</td>
<td>0.545'</td>
<td>0.767'</td>
<td>0.607'</td>
<td>0.959'</td>
<td>0.147'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(4.211)</td>
<td>(6.570)</td>
<td>(6.745)</td>
<td>(5.009)</td>
<td>(5.297)</td>
<td>(3.991)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{h-2} )</td>
<td>0.149'</td>
<td>1.358'</td>
<td>0.328'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(3.263)</td>
<td>(3.237)</td>
<td>(3.528)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{h-3} )</td>
<td>1.836'</td>
<td>2.125'</td>
<td>2.757'</td>
<td>3.662'</td>
<td>0.147'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(3.897)</td>
<td>(3.791)</td>
<td>(3.448)</td>
<td>(3.331)</td>
<td>(3.904)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{h-3} )</td>
<td>1.874'</td>
<td>1.537'</td>
<td>0.808'</td>
<td>1.706'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(5.540)</td>
<td>(3.544)</td>
<td>(3.648)</td>
<td>(4.305)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{h-3} )</td>
<td>-0.105'</td>
<td>-0.186'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(-3.561)</td>
<td>(-4.346)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{h-3} )</td>
<td>-0.117'</td>
<td>0.059'</td>
<td>0.089'</td>
<td>-0.195'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(-3.560)</td>
<td>(-3.252)</td>
<td>(3.326)</td>
<td>(-3.731)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_{h-3} )</td>
<td>0.077'</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(3.060)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \hat{\xi}_{SC} )</td>
<td>-0.581'</td>
<td>-0.543'</td>
<td>-0.594'</td>
<td>-0.543'</td>
<td>-0.190'</td>
<td>-0.175'</td>
<td>-0.262'</td>
<td></td>
<td></td>
<td>-0.130'</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(-7.540)</td>
<td>(-5.060)</td>
<td>(-5.791)</td>
<td>(-5.353)</td>
<td>(-6.854)</td>
<td>(-8.176)</td>
<td>(-6.387)</td>
<td></td>
<td></td>
<td>(-6.166)</td>
<td></td>
</tr>
<tr>
<td>( \hat{\xi}_{H} )</td>
<td>-0.331'</td>
<td>-0.186'</td>
<td>0.059'</td>
<td>-0.054'</td>
<td>0.375'</td>
<td>-0.195'</td>
<td>-0.077'</td>
<td>-0.143'</td>
<td></td>
<td></td>
<td>-0.063'</td>
</tr>
<tr>
<td>( \hat{\xi}_{H} )</td>
<td>-0.317'</td>
<td>-0.186'</td>
<td>0.059'</td>
<td>-0.054'</td>
<td>0.375'</td>
<td>-0.195'</td>
<td>-0.077'</td>
<td>-0.143'</td>
<td></td>
<td></td>
<td>-0.063'</td>
</tr>
</tbody>
</table>

Notes: AT, BE, FI, FR, GE, GR, IE, IT, NL, PT and SP stand for Austria, Belgium, Finland, France, Germany, Greece, Ireland, Italy, the Netherlands, Portugal and Spain respectively.

In the ordinary brackets below the parameter estimates, the corresponding \( t \)-statistics are shown.

The short-run effects of public debt are calculated using equation (7)

\* and \** denote statistical significance at the 1% and 5% level, respectively.

\( \hat{\xi}_N, \hat{\xi}_{SC} \) and \( \hat{\xi}_H \) are the Jarque-Bera test for normality, the Breusch-Godfrey LM test for second-order serial correlation and the Breusch-Pagan-Godfrey test for heteroskedasticity. In the square brackets, the associated probability values are given.