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Title: The electrical properties of calcium sulphate rocks from decametric to micrometric scale

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Abstract: Sulphate rocks have a sedimentary evaporitic origin and are present in many deposits worldwide. Among them, gypsum (dihydrated calcium sulphate) is the most common and is exploited for industrial purposes. Anhydrite (calcium sulphate) is frequently found in gypsum quarries and in non-outcropping sulphates. The greater hardness of anhydrite compared to gypsum causes a problem for gypsum extraction; quarry fronts have to be halted as soon as anhydrite is found. In this work the electrical properties of calcium sulphates have been studied by means of geoelectrical methods.

A direct relationship between the electrical conductivity values of the calcium sulphate rocks and their lithological composition has been established with the lutitic matrix being the main controlling factor when it is well connected. When the matrix is under the percolation threshold the sulphate phases are dominant, and the electrical response of the rocks depends on the percentage of each phase. When the rock is matrix dominant, the electrical resistivity trend fits with the Hashin-Shtrikman lower bound for multiphase systems (considering gypsum, anhydrite and matrix as the components). On the other hand, when the rock is calcium sulphate dominant the trend shows the one of the Hashin-Shtrikman upper bound. The reference electrical resistivity value of pure anhydrite rocks has been defined as 104 Ω .m and geoelectrical classification for calcium sulphate rocks has been elaborated. With this classification it is possible to differentiate between calcium sulphate rocks with different composition from their electrical resistivity value. This classification has been checked with field examples and calculating the theoretical resistivity value of thin section photographs with the program ELECFEM2D. The electrical behavior of calcium sulphate rocks is a good reference for other type of rocks with electrically differentiated components, and similar methods can be used to define their geoelectrical responses.

A direct relationship between the electrical conductivity values of the calcium sulphate rocks and their lithological composition has been established being the lutitic matrix the main controlling factor when it is percolant (connected at long range). When the matrix is under the percolation threshold the dominant phases are the sulphate ones and the electrical response of the rocks depends on the percentage of each one in their composition. When the rock is matrix dominant, the electrical resistivity trend fits with the Hashin-Shtrikman lower bound for multiphase systems (considering gypsum, anhydrite and matrix as the components). On the other hand, when the rock is calcium sulphate dominant the trend shows the one of the Hashin-Shtrikman upper bound. The reference

electrical resistivity value of pure anhydrite rocks has been defined as 104 ohm.m and geoelectrical classification for calcium sulphate rocks has been elaborated. With this classification it is possible to differentiate between calcium sulphate rocks with different composition from their electrical resistivity value. This classification has been checked with field examples and calculating the theoretical resistivity value of thin section photographs with the program ELECFEM2D. The electrical behavior of calcium sulphate rocks is a good reference for other type of rocks with electrically differentiated components, and similar methods can be used to define their geoelectrical responses.

In this paper the electrical conductivity of Sulphate Rocks is studied. > Electrical Resistivity Tomography profiles are performed. > Conductivity measures are carried out in laboratory conditions. > The conductivity of sulphate rocks is theoretically calculated at microscopic scale from microphotographs. > An electrical classification of sulphate rocks has been elaborated.

Dear editor and reviewers,

I have performed the changes in the model calculated with the modified Archie's law using the coefficients suggested. I also have made some little changes in the text (marked in red) and in some figures (figures 4 and 6 and table 4) as required by the reviewer Paul Glover. I want to thank him for his comments because I really think that the quality of the paper has increased since the first submission thanks to them.

Yours sincerely

Ander Guinea and co-authors

University of Barcelona

THE ELECTRICAL PROPERTIES OF CALCIUM SULPHATE ROCKS FROM DECAMETRIC TO MICROMETRIC SCALE

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ABSTRACT

Sulphate rocks have a sedimentary evaporitic origin and are present in many deposits worldwide. Among them, gypsum (dihydrated calcium sulphate) is the most common and is exploited for industrial purposes. Anhydrite (calcium sulphate) is frequently found in gypsum quarries and in non-outcropping sulphates. The greater hardness of anhydrite compared to gypsum causes a problem for gypsum extraction; quarry fronts have to be halted as soon as anhydrite is found. In this work the electrical properties of calcium sulphates have been studied by means of geoelectrical methods.

A direct relationship between the electrical conductivity values of the calcium sulphate rocks and their lithological composition has been established with the lutitic matrix being the main controlling factor when it is well connected. When the matrix is under the percolation threshold the sulphate phases are dominant, and the electrical response of the rocks depends on the percentage of each phase. When the rock is matrix dominant, the electrical resistivity trend fits with the Hashin-

26 Shtrikman lower bound for multiphase systems (considering gypsum, anhydrite and matrix as the
27 components). On the other hand, when the rock is calcium sulphate dominant the trend shows the one
28 of the Hashin-Shtrikman upper bound. The reference electrical resistivity value of pure anhydrite
29 rocks has been defined as $10^4 \Omega.m$ and geoelectrical classification for calcium sulphate rocks has been
30 elaborated. With this classification it is possible to differentiate between calcium sulphate rocks with
31 different composition from their electrical resistivity value. This classification has been checked with
32 field examples and calculating the theoretical resistivity value of thin section photographs with the
33 program ELECFEM2D. The electrical behavior of calcium sulphate rocks is a good reference for other
34 type of rocks with electrically differentiated components, and similar methods can be used to define
35 their geoelectrical responses.

36

37 **Keywords:** Gypsum, Anhydrite, Sulphate, Electrical Conductivity

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40 1. INTRODUCTION

41 Evaporites are sedimentary rocks originated from evaporation of salty water. Sulphates are one
42 of the principal groups of evaporitic rocks and the principal sulphate minerals are: gypsum
43 ($\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$), anhydrite (CaSO_4), glauberite ($\text{Na}_2\text{Ca}(\text{SO}_4)_2$) and thenardite (Na_2SO_4) (Warren, 2006).
44 Texturally, sulphate rocks are mainly crystalline; but may appear with clastic textures when they are
45 reworked. They retain only a reduced primary porosity ($<1\%$), display a restricted mineralogical (and
46 geochemical) composition and can appear combined with a lutitic matrix (mainly composed of clay
47 and microcrystalline carbonates). The texture of rocks are affected extensively by diagenetic processes
48 which can become microcrystalline. Gypsum tends to transform to anhydrite when buried as a result of
49 dehydration, and the opposite process also takes place when anhydrite is affected by weathering and
50 superficial waters (Holliday, 1970).

51 Gypsum deposits are exploited for industrial purposes. It is mainly used in construction as
52 drywall and as an ingredient for plaster, but it is also used in other industries (Bustillo et al., 2001).
53 Gypsum quarries occur worldwide, with the USA and Iran as the largest producers. One of the most
54 important problems found while quarrying gypsum is the presence of anhydrite. By comparison with
55 gypsum, anhydrite is harder and denser. The drilling machines can be damaged by anhydrite bodies.
56 Hence, the exploitation must be stopped immediately. Anhydrite is also used by industry for different
57 purposes, but because of the exploitation difficulties it is mainly obtained by dehydration of previously
58 extracted gypsum. Anhydrite (from gypsum dehydration) is commonly found deeply buried (up to
59 1000 m; Shearman, 1985; Warren, 2006). It rarely crops out because it tends to hydrate and transform
60 into gypsum.

61 Geoelectrical techniques are proposed as a tool for studying these sulphate deposits. Electrical
62 resistivity tomography (ERT) is a geophysical technique which can be used to obtain an image of the
63 electrical resistivity distribution of the subsurface. For this purpose an array of metal electrodes are
64 planted in the soil and the difference of electrical potential is measured between pairs of them while a
65 direct current (DC) is passed between two others. The arrangement of these 4 electrodes depends on

66 the electrical array that has been selected and the measurement is repeated along the string of
67 electrodes at different spacings and positions. The apparent resistivity values obtained are inverted into
68 resistivity values as a function of depth and position using inversion software (RES2DINV, Geotomo
69 Software, ver. 3.5). This method is a rapid, non invasive and relatively low-cost.

70 Gypsum deposits have been successfully identified with ERT profiles (Lugo et al., 2008;
71 Guinea et al., 2009; Guinea et al., 2010a). Guinea et al. (2010b) produced a geoelectrical classification
72 of gypsum rocks establishing a direct relation between their electrical resistivity value and the
73 percentage of lutitic matrix (Table 1). In that study the anhydrite phase was not considered, but this
74 mineral very often appears in gypsum rocks. The scientific literature shows anhydrite to have a large
75 range of resistivities from <100 to 10^{10} Ω .m (Table 2; Jakosky, 1950; Parkhomenko, 1967; Rider,
76 1986; Robison and Çoruh, 1988; Choteau et al., 1997; Asfahani and Mohammad, 2002; Lugo et al.,
77 2008). The variation in the electrical resistivity value of anhydrite in these publications is related to the
78 presence of gypsum, but the influence of the lutitic matrix is not mentioned.

79 The aim of this study is to measure the electrical resistivity of pure anhydrite at zero frequency
80 and to establish the effect of compositional variations in the gypsum-anhydrite-lutite rock system. This
81 problem will be studied from three different angles, namely numerical modeling, laboratory
82 measurements and field data. The information thus obtained should help to interpret geoelectrical data
83 in future surveys on sulphate rocks.

84

85 **2. FIELD DATA**

86 *2.1 Geological setting*

87 During the Lutetian (Middle Eocene) a large marine evaporitic sequence was deposited in the
88 South Pyrenean Foredeep (Rosell and Pueyo, 1997). In the La Garrotxa area (eastern Pyrenees)
89 secondary gypsum (as product of the hydration of anhydrite) crops out extensively and anhydrite has

90 been found in borehole logs with other evaporitic rocks such as halite (Carrillo, 2009). Close to the
91 village of Beuda (Girona, Spain) there is a quarry in which gypsum has been exploited since at least
92 the 1930s. There are many sculptures made of alabaster (pure secondary microcrystalline gypsum)
93 from the Middle Ages for which geochemical analysis has demonstrated that they were extracted from
94 the Beuda gypsum unit (Inglés et al., 2009).

95 Nowadays the quarry has been largely developed and anhydrite crops out in many places and
96 where the exploitation has consequently been stopped. The gypsum of the Beuda unit was produced by
97 hydration of anhydrite and therefore there are still some anhydrite relict bodies embedded in the
98 gypsum. In the walls of the quarry it is possible to observe boundaries between gypsum and anhydrite
99 usually displaying a quite pure anhydrite core and a transition to pure gypsum (Figure 1A). The purity
100 of the calcium sulphate varies from higher than 90% to close to 75% in certain layers (Figure 1B). The
101 changes in the purity of both gypsum and anhydrite rocks and the complex geometrical relations
102 between them make these deposits very heterogeneous. In some cases matrix bearing gypsum appears
103 in contact with pure anhydrite and in other cases the anhydrite does not appear as a body but as
104 fragments embedded in gypsum and filled with gypsum veins (Figure 1C). In other places anhydrite
105 appears massive with little gypsum within (Figure 1D). Three ERT profiles (figure 2, A, B, and C)
106 have been performed in the Beuda gypsum quarry. Profile D (Figure 2D) has been performed in the
107 same formation of the Beuda quarry, close to the village of Serinyà. In the area studied there are
108 sulphate layers under a soil. In the nearby outcrops pure secondary gypsum appears, but at depth, the
109 sulphates probably transform into anhydrite as it has been observed in the region (Carrillo, 2009).

110 Marine evaporitic deposition took place during the upper Eocene on the Catalan margin of the
111 Ebro basin (Ayora et al., 1994). The Odena gypsum unit was extensively exploited during the 20th
112 century and there are many abandoned quarries in the region. Profile E has been carried out in an
113 abandoned quarry near to the village of Odena where anhydrite crops out (Figure 2E).

114 In the Montes de Torrero area (Zaragoza, Spain) there is a Miocene evaporitic formation
115 hundreds of meters thick. The area has been studied by means of boreholes in which gypsum,

116 anhydrite, glauberite and halite were found among other minerals. This formation has a large quantity
117 of matrix in every layer (Ortí, 2000; Salvany, 2009). The outcropping materials are mainly gypsum,
118 which formed from the hydration of anhydrite or glauberite (Figure 1E), and more than 50% matrix
119 (composed of clay and marl). An ERT survey has been performed where borehole B4 was drilled
120 (Figure 2F). The log of the borehole shows gypsum to a depth of 35 m, then glauberite to a depth of 69
121 m followed by anhydrite to 80 m with some interbedded layers of halite or glauberite (Salvany, 2009).
122 The whole log shows significant fractions of matrix at all depths as such as at the surface.

123 *2.2 Methods*

124 A total of six ERT profiles have been carried out at anhydrite rock deposit areas in the South
125 Pyrenean Foredeep and Ebro Basin (North East of Spain; Figure 3). The examples are presented below
126 starting with those performed in quarries (Figure 3; A, B, C and D) and afterwards in areas with no
127 evaporites that crop out (Figure 3; E and F). All the profiles performed in quarries show a high
128 fraction of sulphates and therefore relatively high electrical resistivity values.

129 A Syscal Pro Switch ERT system with 48 electrodes and an external power supply has been
130 used to carry out the data acquisition. The electrode spacing for the measurements in quarries was 0.5,
131 1.5 or 2 m depending on the local conditions. In the profiles performed where no evaporates crop out,
132 the electrode spacing was 10 m to increase the depth of investigation because anhydrite deposits tend
133 to appear below other formations (because at shallow depth they transform into gypsum). The used
134 electrodes for the data acquisition were made of stainless steel and they were nailed in the terrain by
135 means of hammers. There are many possible array configurations in geophysical prospection (Ma et
136 al., 1997; Furman et al., 2003; Szalai and Szarka, 2008) which may be applied to anhydrite rocks. The
137 Wenner-Schlumberger and Dipole-Dipole arrays have been selected depending of the structure under
138 study, and the Dipole-Dipole has been used were lateral electrical resistivity changes are important.
139 The apparent resistivity data of performed ERT profiles has been inverted with the RES2DINV
140 program; that is available from 1995 (Loke and Barker, 1996). The inversion process has been carried
141 out with 5 iterations for each profile. With this number of iterations the data converges in all cases

142 achieving an acceptable RMS error. Additional iterations do not vary the RMS error significantly but
143 increase the electrical resistivity value in the low sensitivity areas (i.e., the pure sulphate rocks). As
144 explained later in Section 2.3, the resistivity range calculated (with 5 iterations) in pure anhydrite
145 bodies at depth is alike to the apparent resistivity measured in shallow pure anhydrite rocks.

146 Sulphate samples have also been collected in some of the profiled areas in order to measure
147 their composition. The samples have been powdered and 0.5 g from each one has been dissolved in
148 250 ml of distilled water in accordance with the solubility of calcium sulphate in water. The solutions
149 were shaken for 24 hours at 25 C° and then filtered. The residue left after filtering correspond to the
150 non-soluble phases, which are made up of the lutitic matrix (including carbonates, quartz and other
151 minor accompanying minerals). The residue was weighted in order to estimate the fraction of the in
152 sulphate phases.

153 *2.3 Results and discussion*

154 In the Beuda quarry some different areas have been studied. The profiles A and B have been
155 performed upon areas in which massive anhydrite was found and afterwards was buried under quarry
156 waste materials. The profiles were spread above the infilling. The result of the inversion for Profile A
157 (Figure 3A) display an upper part with relatively low electrical resistivity values (between 10 and 200
158 $\Omega.m$), which corresponds to the quarry waste. Underlying these materials there is a homogeneous body
159 with high resistivity value (up to $10^4 \Omega.m$), which has been interpreted as pure anhydrite (Lugo et al.,
160 2008). In the case of Profile B, which was performed perpendicularly to Profile A, the inverted
161 resistivity section (Figure 3B) displays a lateral electrical resistivity variation below the quarry waste
162 layer. A well was drilled in the middle of profile B and high hardness was found at 6 meter depth, but
163 no core was recovered. This hardness has been interpreted as anhydrite rock with certain quantity of
164 matrix.

165 The profile C has been measured in other location where anhydrite had also stopped the
166 exploitation of the quarry. The electrodes were inserted almost directly into the sulphate rocks and

167 both anhydrite and gypsum appeared in the ground surface. In the inverted resistivity section (Figure
168 3C) there is displayed a lateral variation of electrical resistivity ranging from 10^3 to 10^4 Ω .m. The
169 larger resistivity values are limited with the outcropping of massive anhydrite, while the lower ones
170 are related to the presence of gypsum, and the intermediate values correspond to the transition between
171 the two pure phases.

172 Profile D has been performed in an abandoned quarry near to the village of Odena where
173 anhydrite crops out. The inverted section (Figure 3D) shows electrical resistivities ranging from 10^3 to
174 10^4 Ω .m, similarly to the observations in the Beuda quarry. In the areas in which the value is larger,
175 massive anhydrite is observed. Lower electrical resistivity than 500 Ω .m are related to lutitic
176 sedimentary layers.

177 Profile E has been performed in an evaporitic basin with no outcrops. The inversion of the
178 profile (Figure 3E) displays a shallow deposit with a low electrical resistivity value (50 Ω .m) which
179 corresponds to the underlying materials. Below this layer there is a high resistivity body ranging from
180 1000 to more than 5000 Ω .m and with a more conductive structure in the central part (between 100
181 and 200 Ω .m). This structure represents a fault present in the area, and identified on the surface by
182 geological evidence (Carrillo, 2009).

183 The profile F performed in Montes de Torrero area has been modified from Guinea et al.
184 (2010b). In the inverted image (Figure 3F) the whole deposit shows a general trend of 30-50 Ω .m with
185 some bodies slightly more resistive (up to 300 Ω .m at the most resistive points). Those bodies would
186 represent a higher grade of the deposit (up to 60% in sulphates) in these zones, this grade changes are
187 related to primary depositional processes and they are very common in these materials (Guinea et al.,
188 2010a). In any case it is not possible to differentiate between anhydrite and gypsum layers because the
189 electrical behavior of the deposit is dominated by the abundant matrix.

190 As general trend, sulphate rocks with high purity in anhydrite show an electrical resistivity
191 value up to 10^4 Ω .m after the inversion (Lugo et al., 2008). This value is considered to be the reference

192 for pure anhydrite rocks because in some profiles in which some of the shallowest points have been
193 measured almost directly above massive anhydrite rocks, show an apparent resistivity value larger
194 than 5000 Ω .m. In these cases the apparent and the inverted resistivities are similar but a slightly lower
195 for the apparent resistivity because the electrodes are inserted into a thin clay layer. When these rocks
196 are mixed with gypsum forming pure sulphate rocks with both phases, which are the most common in
197 the quarries, they display an intermediate value of resistivity ranging from 1500 to 5000 Ω .m
198 depending on the quantity of each phase. As the distribution of the anhydrite in the gypsum deposits is
199 very heterogeneous due to the rehydration processes, the tomography lines show heterogeneous bodies
200 with different electrical resistivity values and transitional zones. Values close to 1000 Ω .m are related
201 to the purest gypsum rocks or to pure anhydrite with a significant quantity of matrix rocks. When the
202 matrix has a large volume fraction, it is not possible to differentiate is gypsum from anhydrite with
203 ERT. In these cases, the rocks will display a resistivity below 100 Ω .m, which is significantly lower
204 than the resistivity of sulphate-rich deposits. The low electrical resistivity of sulphate deposits with
205 large matrix volume fraction was studied further by Guinea et al. (2010b) for the case of gypsum rocks
206 (without anhydrite).

207

208 **3. LABORATORY MEASUREMENTS**

209 *3.1 Methods*

210 Many authors have measured the electrical conductivity of geological materials (Keller, 1966;
211 Lockner and Byerlee, 1985; Guéguen and Palciauskas, 1994; Glover et al. 1996; Giao et al., 2003;
212 Rusell and Barker, 2010; among others). Guinea et al (2010b) made eleven gypsum-clay pills in
213 different proportions with a range from 0 to 100% of $\text{CaSO}_4 \cdot \text{H}_2\text{O}$ at intervals of 10% in composition
214 and measured their electrical conductivity. Three sets of eleven anhydrite-lutite pills and three sets of
215 gypsum-lutite pills have been made using the same methodology, parameters and resources. The
216 compositional error of the pills is below 1%, because the weight corresponding to the volume of each

217 fraction has been measured with a precision scale (Sarorius B3100S) with a resolution of 0.01 g (the
218 pills have a total weight of 13.5 g). The pills have a cylindrical shape with a radius of 2 cm and a
219 width of approximately 0.50 cm. The aim of these measures is to define the importance of the matrix
220 presence in calcium sulphate rocks.

221 The conductivity measurement was carried out in accordance with the UNE 21-303-33
222 regulation (1983) with an electrical circuit in which the samples act as electrical resistance (Figure 4).
223 The electrical power source was a laboratory DC converter power supply with switchable voltage (0–
224 32 V) and current (0-10 A). Changes in the amperage above 1 A do not affect the measurements so an
225 output current of 2 A has been selected. In order to measure the amperage of the electrical current after
226 traversing the resistance (the sample), an analogue microammeter (Demestres 540) with a range of 0-
227 100 μA and an accuracy of 1 μA , or a nanoammeter (Monroe 285) with a range of ± 200 nA, a 0.1 nA
228 resolution and an accuracy of 2% have been used. The potential difference is measured by a voltmeter
229 (MY-67) with a resolution of 0.001 V connected to both sides of the pills.

230 The electrodes used on the samples are made of stickers with metallic buttons such as those
231 used for electrocardiograms (Compex). The button has a conductive gel on the sticking side, forming a
232 0.75 cm-radius circled face (which will be considered the surface of the electrode). This gel is
233 connected directly to the samples. The pills and the electrodes are situated above a paperboard
234 insulator. The barrelling effect is low because the distance between the electrodes is relatively small
235 (approximately 0.50 cm) and can be neglected. Due to the difference between the area of the
236 electrodes and the area of the pills, there is a leak path for the electrical current (Roth, 1959). The
237 measurements were made after the reading stabilizes (10 seconds after the power supply is switched
238 on). Polarization causes errors after a certain time in the pills with large fractions of clay. Hence,
239 measurements made after current has flowed for a long time are not considered representative for
240 geophysical surveys because geoelectrical methods use a short current injection time. Each pill has
241 been measured three times, making a total of 6 measurements for each volume fraction. Ohm's law
242 can be applied to calculate the conductivity (σ) or resistivity (ρ) of the sample for a known current
243 density (j) and field (E) (Eq. 1):

244

$$j = \sigma E = E/\rho$$

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It is possible to measure the resistance (R) of the samples. As the thickness (L) of the sample and the surface area of the electrode (S) are known, the electrical resistivity (ρ) can be calculated (Eq. 2):

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$$R = \rho L/S$$

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3.2 Results and discussion

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The resistivity calculated for the gypsum-lutite and anhydrite-lutite pill sets is shown in Figure 5 (a full measurements table is shown in Annex 1). The mean resistivity is indicated by symbols together with an error bar representing the standard deviation. The measurements performed on gypsum-lutite pills showed a similar trend to the one presented by Guinea et al. (2010b). The pills ranging from 70 to 100% in gypsum fraction were more accurate in the present study because the current was measured with a nanoammeter instead of a microammeter. The pills ranging from 0 to 40% in gypsum fraction displayed a slightly increasing trend of the electrical resistivity (with a mean value ranging from 6 to 33 Ω .m). The 50 and 60% gypsum fraction pills displayed a transitional range of resistivity (with mean values of 72 and 137 Ω .m respectively). Finally, the pills with a volume fraction of gypsum ranging from 70 to 100% displayed a resistivity of >700 Ω .m. The trend shown by the anhydrite pills is similar to the one shown by the gypsum pills for the case of pills with a sulphate fraction from 0 to 50%. There are slight differences between them, but both sets are in the same range of resistivities. The anhydrite-pills with a sulphate fraction of 60% or above are noticeably more resistive than their equivalent in gypsum pills (ranging from 1012 to 7609 Ω .m mean resistivity).

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It is evident that the grades below 60% are dominated by the lutitic matrix and the sulphate component affects the measurement negligibly. The sulphate volume fractions above 70% showed high resistivity values in which the dominant component is the sulphate phase. Between the two differentiated trends there is a transitional zone which represents the loss of the connectivity of the

268 matrix. As in the measurements of the gypsum pills by Guinea et al. (2010b), the pills with a large
269 quantity of clay component polarize with measuring time. The chargeability of clay has been widely
270 described before (Takakura, 2006; Deucester and Kaufmann, 2009).

271 Percolation theory states that in a cluster with a component randomly distributed (meaning the
272 lutitic matrix for this case) there is a percolation threshold which represents the minimal quantity of
273 the component required in order to obtain a long-range connectivity (Stauffer and Aharony, 1985).
274 This theory has been widely used to predict characteristics of rocks as the connection of their porosity
275 or fractures (Karmakar et al., 2003; Wang et al., 2007). When the fraction of the component is below
276 the percolation threshold, the cluster is not considered to be connected. In our system the percolation is
277 controlled by conduction through matrix which is much more conductive than the sulphate phase.
278 Anhydrite or gypsum components are dielectric (act as resistances) and they conduct little electrical
279 current while the matrix fraction is above the percolation threshold. Below the percolation threshold,
280 the electrical current finds no connected pathways in the matrix and passes through the sulphates.
281 Hence, the relative proportion of gypsum and anhydrite phases when the presence of matrix is above
282 40%, do not affect the electrical resistivity value of the whole rock.

283

284 **4. THEORETICAL CALCULATIONS**

285 *4.1 Methods*

286 Physical properties of rocks are mainly functions of their microstructure (Guéguen and
287 Palciauskas, 1994). Two important mathematical approaches are effective medium theory (EMT) and
288 percolation theory. The EMT (Kirpatrick, 1973) approximation is quite good for rocks with quasi-
289 uniform distributions where only a small degree of heterogeneity is observed, although they cannot
290 describe correctly the phenomenon of clustering (Guéguen et al., 1997) when the heterogeneity is
291 large. Moreover, the knowledge of the geometric distribution and connectivity of the minor phase is of
292 great importance. Percolation theory describes the medium in terms of probabilities of the connectivity

293 but does not provide bulk physical properties. Here, we propose a method to determine the physical
294 properties of composite materials that combines the EMT and the percolation theory. On one hand, the
295 EMT is used to calculate the bounds of the physical properties depending on the amount of the matrix
296 phase present. These limits correspond to the two extreme situations where the matrix phase is totally
297 interconnected or disconnected. On the other hand, the percolation theory is used to determine the
298 probability of having a connected or interconnected matrix phase assuming that it is distributed in a
299 single cube distribution.

300 The effective properties of composites, in particular electrical conductivity, have been studied
301 analytically for a long time for a very simple cases (i.e., Maxwell (1881) used effective medium theory
302 to derive the bulk conductivity of spheres dispersed in a continuous medium). The rocks can be
303 considered as random materials of different property phases at various length scales. To compute the
304 effective properties of such materials requires knowledge of the microstructure and require numerical
305 computation. Garboczi (1999) wrote an algorithm and the consequent FORTRAN code to compute
306 using both finite difference and finite element codes to calculate the electrical an elastic effective
307 properties of materials with different phases from digital images.

308 In this paper the program ELECFEM2D.F from Garboczi (1999) has been used to compute the
309 effective conductivity of gypsum-anhydrite rock samples. The method to calculate the electrical
310 conductivity of these rocks is to analyze thin section images in which the amount of both anhydrite
311 and gypsum proportion together with the one of the lutitic matrix is known. With this software it is
312 possible to obtain a resistivity distribution model based on a microphotograph.

313 In order to perform the theoretical calculation of photographs with the program
314 ELECFEM2D.F, the pictures must be converted from an image format file (e.g., JPG, JPEG, GIF,
315 PNG) into an ASCII file. This has been carried out with a converter which creates numerical files from
316 the pixels of the input image. Depending on the color range of these pixels, a numeric value, which is
317 related to a user defined electrical resistivity value, is assigned. As the images used display lutite,
318 gypsum and anhydrite phases; 10 , 10^3 and 10^4 $\Omega\cdot\text{m}$ electrical resistivity values have been selected

319 respectively. This selection will be discussed further in Section 4.2. The number of variables is user
320 defined and 2 variables (1 and 2) have been selected for photographs displaying 2 phases (any couple
321 of lutite-gypsum-anhydrite) and 3 variables (1, 2 and 3) when the 3 of them are present. Each image
322 was previously treated with an image processing program in order to homogenize the colour ranges in
323 order to improve the detection of each phase.

324 Once the ASCII file is created, it can be used by the ELECFEM2D.F program. The program
325 divides the surface into 8400 (150×56) cells with an electrical resistivity value assigned to each one,
326 and calculates the current intensity remaining after crossing the system in the x or y direction. Both
327 directions and the arithmetic mean value have been calculated; the differences are related to the
328 anisotropic distribution of the phases. The selected potential gradient was set to 1 V/m.

329 4.2 *Mixing models for two and three phase systems*

330 Many mixing models have been published in order to predict the bulk conductivity of a porous
331 medium (Glover et al., 2000). In the case of sulphate rocks there is no porosity; hence, the resistivity
332 (or conductivity) of the bulk rock depends on the fraction (γ) and the electrical resistivity value (ρ) of
333 each component and on the connectivity and geometrical distribution of the matrix (which has the role
334 of a conducting fluid in a saturated porous medium). Different mixing models (Parallel, Perpendicular,
335 Random, Modified Archie's law and Hashin Shtrickman bounds) have been calculated for the case of
336 two-phase sulphate rocks (gypsum-lutite and anhydrite-lutite) with different proportions of sulphate
337 and matrix. The electrical resistivity values selected for gypsum and lutite phases have been 10^3 and
338 $10 \text{ } \Omega\cdot\text{m}$, respectively (Guinea et al., 2010b). The electrical resistivity value selected for pure anhydrite
339 phase has been $10^4 \text{ } \Omega\cdot\text{m}$, in accordance with the maximum value measured in field examples and the
340 bibliography (Table 2).

341 Parallel and Perpendicular mixing models (Table 3A and B; Somerton, 1992; Guéguen and
342 Palciauskas, 1994) describe the conductivity of a layered distribution of phases with a constant
343 arbitrary thickness arranged axially or normally (in each case) to the current flow. The random model

344 (Table 3C; Warren and Price, 1961; Shankland and Waff, 1977) describes the bulk conductivity of a
345 material with randomly distributed arbitrary volumes of the conductive phase. Glover (2000)
346 described a mixing model (Table 3D) derived from Archie's law (Archie, 1942), considering the
347 boundary conditions implied by geometrical constraints. To calculate this model, the cementation
348 exponent m has to be defined for each phase. This variable depends on the connectedness of the phases
349 and, as long as in the present case there is no information about this connectedness, **it has been tested**
350 **with different values of m to adjust the data. When the matrix is dominant, $m=0.25$ is consistent with**
351 **the data obtained for both anhydrite and gypsum pills, which indicates that the structure of the matrix**
352 **is the same for both types of sample. In the case of pills with higher sulphate fractions, $m=0.01$ and**
353 **$m=0.006$ has been selected for gypsum and anhydrite pills respectively.** Hashin and Shtrikman (1963)
354 defined the electrical resistivity value bounds (HS bounds) of a bulk rock from effective medium
355 considerations. These bounds represent the theoretical maximum (upper bound; Table 3E) and
356 minimum (lower bound; Table 3F) electrical resistivity value that any material formed of two different
357 phases with a certain fraction can display.

358 The mentioned mixing models are displayed in the Figure 6 for both gypsum-lutite (Figure
359 6A) and anhydrite-lutite (Figure 6B) systems. Additionally to the theoretical trends of the mixing
360 models, the resistivities calculated in the laboratory measurements are displayed. The pill samples
361 with a fraction of sulphate phases of 50% or below show a similar trend to the one displayed by the
362 HS⁻ model. This is also shown in the field data in the profiles in which the sulphate formations have a
363 high quantity of matrix within. On the other hand, the resistivity of the pills with a sulphate fraction of
364 70% or above is closer to the perpendicular or HS⁺ models. In the case of the anhydrite pills with high
365 sulphate fraction, they fit better to the random model; but this can be related to the fact that the
366 anhydrite pills are slightly watered during their elaboration. **The modified Archie's law also fits well**
367 **to the laboratory data; the two different trends (low sulphate fractions and high sulphate fractions)**
368 **have been bridged by means of variations of m in their end ranges (showed as dashed lines in the**
369 **graphic).** The field data obtained in anhydrite rocks indicate that the observed resistivity ranges fit
370 better to the perpendicular or HS⁺ models. The values obtained for the pills with 60% in sulphate

371 fraction are transitional, which represents the percolation threshold. Theoretically the percolation
372 threshold occurs in a single phase fraction but in the case of real rocks transitional values are displayed
373 in this range of composition.

374 From the trends observed for these two-phase systems, it can be considered, as approximation,
375 that the HS bounds define the resistivity of gypsum and anhydrite rocks depending on the quantity of
376 matrix present (modified Archie's law is also a good approximation, but the value of m has to be
377 defined). When the matrix is percolating (sulphate fraction of 50% or below), the resistivity of the
378 sulphate rocks is bounded to the HS⁻ model. In the case of non percolating matrix (sulphate fraction of
379 70% or above), the resistivity is bounded to the HS⁺ model. A general form of the bounds for n -phases
380 was given by Berriman (1995). With his formula it is possible to construct a ternary graphic for 3-
381 phased rocks (Ledo and Jones, 2005). The gypsum-Anhydrite-Lutite (GAL) system has been
382 calculated for both upper (Table 3G) and lower (Table 3H) HS bounds. In the case of lower bound
383 (Figure 7A), the system is clearly dominated by the lutitic component; the iso-resistivity lines are
384 parallel between them showing no appreciable variation in the gypsum-anhydrite axis but when the
385 lutite fraction is less than 10%. The values of resistivity are very low in general, showing less than 100
386 $\Omega\cdot\text{m}$ for a sulphate fraction of 70%. The upper bound (Figure 7B) displays a very different trend
387 dominated by the anhydrite fraction, but in this case the 3 components affect the bulk resistivity value
388 of the rock. The electrical resistivity values are much larger than in the case of lower bound achieving
389 1000 $\Omega\cdot\text{m}$ with only 40% of anhydrite. As it has been previously shown, the electrical behavior of the
390 rocks is the one of lower HS bound when the quantity of sulphate is of 50% or below and the one of
391 upper bound when is of 70% or above. Thus it is expected that the real distribution of the electrical
392 resistivity for the GAL system should be a combination between the upper and lower HS bounds
393 (Figure 7C).

394 *4.3 Results and discussion*

395 In order to check the accurateness of this GAL diagram, the theoretical electrical resistivity
396 value of real thin section rock photographs (Figure 8) has been calculated with ELECFEM2D

397 program. Lutitic matrix display brownish colouring while both anhydrite and gypsum have are
398 transparent underplane polarized light; having anhydrite higher relief than gypsum (its bounds are well
399 marked with dark lines). With crossed polarized light, gypsum and anhydrite can be easily
400 differentiated because of the different coloring of the anhydrite (pink, green, blue) in contrast with the
401 gray colors of the gypsum crystals. The standard electrical resistivity values selected for the gypsum,
402 anhydrite and lutitic matrix phases have been 10^3 , 10^4 and 10 Ω .m respectively, as has been assigned
403 before. The electrical resistivity of the bulk sections has been measured in both x and y directions;
404 when the distribution of the components is homogeneous these values would be considered similar.
405 For each thin section the fractions of the components are calculated by the program so it is possible to
406 obtain the electrical resistivity value corresponding to these fractions calculated with different mixing
407 models (Table 4). Modified Archie's law has not been calculated for the case of 3-phase system
408 because it would require writing and implementing a numerical inversion program to calculate m and
409 p in function of the volume fraction, which is not the aim of this article.

410 The results show that the mean of the calculated electrical resistivity values in x and y
411 directions are in general close to HS^+ bound when the fraction of sulphate is 70% or higher (Figure 8,
412 thin sections A, D, E, F, G and H; Table 4) and to the HS^- bound when the fraction of matrix is
413 abundant (Figure 8, B and I; Table 4). There is a good match between the corresponding position of
414 each sample in the figure 7C, according to their components percentages, and the calculated resistivity
415 values. In the case of thin sections C and J there is abundant matrix (58 and 52% respectively);
416 nevertheless, the calculated resistivity values are slightly larger than that expected for such mixture.
417 This is due to that the phases are not scattered and randomly distributed within the samples but
418 forming compact and pure areas. This represents large heterogeneities which change the percolating
419 behavior (we have considered it only for regular distributions of the phases as in the case of the pills)
420 of the bulk rock and makes the transition zone larger. In any case the values are always much closer to
421 the lower bound than to the upper one. The parallel and perpendicular (series) models do not fit well to
422 the calculated resistivities. The random model fits well in many cases but in samples with large
423 fraction of anhydrite, calculated resistivity is too high (especially in C thin section).

424 At larger scale (as in the ERT profiles) the rocks are in general more homogeneous and should
425 fit to the HS lower bound for compositions of 0-60% in lutitic matrix. The microscopic anisotropies do
426 not affect to the electrical conductivity of the bulk deposit if we increase the scale. In any case, it is
427 possible to observe cases of heterogeneities at metric scale. When these heterogeneities are large, they
428 can be considered as different rocks (for example a gypsum-rich lutite body within a larger pure
429 gypsum host-rock). In any case, heterogeneities below the detection limit of the method will be
430 considered as a single rock. Another possible case is a layered deposit in which every layer has
431 different purity in the sulphate phase. If the difference among grades is low, which is the most
432 common case, the whole sequence can be considered as a single member with a mean grade. Rarely
433 sulphate deposits have great variations of grade from layer to layer forming a heterogeneous sequence.
434 Sudden variations in the grade exist, but are normally associated with the limit of a sequence or a
435 stable change in the depositional conditions. In the case of having layering between almost pure matrix
436 and highly pure sulphates, the transitional values of resistivity will increase their range as happens in
437 the case of the microphotographs.

438

439 **5 GEOELECTRICAL CLASSIFICATION OF CALCIUM SULPHATE ROCKS**

440 With the GAL diagram obtained combining both HS^+ and HS^- boundaries for a gypsum
441 anhydrite-lutite system (Figure 7C) a geoelectrical classification has been elaborated differentiating 6
442 calcium sulphate rock types (Figure 9). When the lutitic matrix is connected at long range (in the case
443 of sulphate fraction of 50% or below) the system is matrix dominant and therefore there is no
444 possibility of differentiating between gypsum and anhydrite components; these rocks are classified as
445 lutites and gypsum/anhydrite rich lutites. The electrical resistivity of this groups range from 10 to 100
446 $\Omega.m$. When the sulphate grade is of 70% or above, the rock will be considered as pure gypsum when it
447 ranges from 700 to 1000 $\Omega.m$ as was stated by Guinea et al. (2010b) for the case of gypsum-lutite
448 systems. If the sulphate mineral is mainly anhydrite (more than 90%) the rock is considered pure
449 anhydrite and its electrical resistivity value range from 2500 to 10^4 $\Omega.m$ depending on the rock grade.

450 In the case of presence of both gypsum and anhydrite sulphate phases, the rock is considered gypsum
451 with anhydrite (1000 to 2000 Ω .m) or anhydrite with gypsum (2000 to 5000 Ω .m). The values of pure
452 anhydrite and anhydrite with gypsum overlap; in this case it is possible to bond the electrical value to
453 pure anhydrite rocks when there is no evidence of rehydration and to the anhydrite with gypsum
454 otherwise. Between lutites and gypsum/anhydrite rich lutites and the sulphate pure rocks there is a
455 transitional area displaying transitional values from 100 to 700-2500 Ω .m (depending on the sulphate
456 composition). The lower boundary of Transitional gypsum/anhydrite rocks has been selected as 55%
457 in sulphate fraction instead of 60% because the measures in pills have shown that the 60% values
458 display an electrical resistivity increasing trend; the upper boundary is 70% in gypsum fraction. This
459 transitional area is displayed with a resistivity-trend calculated by interpolation between lower and
460 upper HS bounds, but the resistivity in the transition zone is uncertain and therefore the displayed
461 trend is only a reference.

462 For the microscopic scale, it has been shown that the transitional range is wider (including
463 rocks between 55 and 70% in sulphate fraction, depending of the anisotropy). For the cases of sulphate
464 fractions of 55% or below or higher than 70%, the values obtained are similar to the corresponding HS
465 bound. At larger scale, the ERT lines have shown relationships between composition and resistivity
466 values similar to the ones displayed in the classification of the Figure 9; that is, higher than 5000 Ω .m
467 when the dominant phase is the anhydrite, 1500 to 5000 Ω .m for different proportions of gypsum and
468 anhydrite (with presence of little lutite) and close to 1000 Ω .m when the gypsum is the dominant
469 phase. For deposits with large amount of lutites, the obtained value has been <60 Ω .m in all cases.

470

471 **6. CONCLUSIONS**

472 The electrical properties of calcium sulphate rocks have been widely studied at different scales
473 with microphotographs, synthetic pills and geological deposits. Laboratory tests in pills have shown
474 that the matrix of calcium sulphate rocks may be affected by the percolation phenomena and therefore,

475 when the sulphate fraction in a rock is of 55% or below, the matrix controls the resistivity of the bulk
476 rock. When the sulphate fraction is of 70% or above, the sulphate minerals control the electrical
477 resistivity of the bulk rock.

478 The electrical resistivity value of anhydrite rocks range from 10 to 10^4 Ω .m, being larger in the
479 purest anhydrite rocks. This value is found in the field examples where the anhydrite appears in
480 massive form. The values observed in rocks with both gypsum and anhydrite (with minor matrix) have
481 ranged between 1500 and 5000 Ω .m depending on the quantity of each other. Large quantity of matrix
482 in sulphate rocks have shown low electrical resistivity values been unable to differentiate between
483 gypsum and anhydrite.

484 When the matrix of the calcium sulphate rocks is above the percolation threshold (i.e., more
485 than 45%), the electrical resistivity value fits the value calculated with the Hashin-Shtrikman lower
486 bound (HS^-), and when is embedded in the sulphate phase (i.e., 30% of matrix or less) the resistivity
487 follows the Hashin-Shtrikman upper bound (HS^+). If there are large heterogeneities in the distribution
488 of the phases, the resistivities of rocks with a matrix quantity ranging from 30 to 45% can display
489 transitional values (more than 100 Ω .m, without reaching values of the purest sulphate rocks).
490 Therefore, it is possible to calculate any combination of these 3 components and the geoelectrical
491 classification has been elaborated for calcium sulphate rocks. With this classification is possible to
492 determine the purity of the sulphates and the presence of anhydrite in gypsum rocks, which is useful
493 for the characterization of the deposit.

494

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504

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619

620 **TABLE CAPTIONS**

621 *Table 1:* Geoelectrical classification of gypsum rocks (modified after Guinea et al. 2010b).

622 *Table 2:* Electrical resistivity values for anhydrite rocks in the literature.

623 *Table 3:* Summary of the equations of the mixing models used in the present study (modified from
624 Glover et al., 2000).

625 *Table 4:* Results of the theoretical calculations of electrical resistivity of the thin section photographs
626 with ELECFEM2D software. Parallel, Series, Random, Archie's modified law and Lower (HS^-) and
627 upper (HS^+) Hashin-Shtrikman bounds have been calculated, only considering the proportion of each
628 phase. The calculated resistivity for each sample in both x and y directions is listed in the right
629 column. The corresponding images of the thin sections A to J are displayed in Figure 8.

630

631 **FIGURE CAPTIONS**

632 *Figure 1:* Photographs of the areas studied with ERT, A to C are taken in the Beuda quarry while D is
633 taken in the area of Odena and E in the Zaragoza formation. A) pure gypsum-anhydrite boundary with
634 a interdigitation between them; B) sulphate layers showing less gypsum fraction than in other areas;
635 C) anhydrite blocks filled with gypsum veins and embedded in a gypsum matrix; D) massive anhydrite
636 body; E) impure sulphate layers in Montes de Torrero area.

637 *Figure 2:* Distribution of evaporite formations in the Tertiary basins northeastern Spain indicating the
638 location of the nine studied ERT profiles with black dots (modified from Ortí et al., 2010).

639 *Figure 3:* Inverted electrical resistivity tomography data for the different areas studied (the locations
640 of the profiles are shown in figure 2). Profile F modified from Guinea et al. (2010b).

641 *Figure 4:* Electrical circuit to measure the electrical resistivity of the samples. It consists of a
642 switchable laboratory power-supply (EA-PS 3032-10B), two electrodes, a voltmeter (MY-67) and a
643 micro- or nanoammeter depending on the samples (Demestres 540 and Monroe 285, respectively).

644 *Figure 5:* Semi-logarithmic plots representing the results of the measurements of gypsum-lutite (A)
645 and anhydrite-lutite (B) pills. The symbols represent the mean of the calculated resistivities for each
646 sulphate fraction (calculated from a total of 6 measurements for every fraction) and the error bar
647 represents the standard deviation. The error on the X axis is not showed because is below 1%.

648 *Figure 6:* Different mixing models calculated for the case of gypsum-lutite (A) and anhydrite-lutite
649 rocks (B). **The dashed lines in the modified Archie's model represent the transition between the low**
650 **sulphate fraction and high sulphate fraction trends.** The resistivity ranges obtained in the laboratory
651 essays (Figure 5) are superimposed for both cases.

652 *Figure 7:* Ternary plots showing Hashin-Shtrikman bounds for gypsum-anhydrite-lutite (GAL)
653 system. A) lower HS bound; B) upper HS bound; C) combined diagram considering the percolation
654 phenomena.

655 *Figure 8:* Microphotographs of thin sections of calcium sulphate rocks; D, E, H and I are taken with
656 cross-polarized light and the rest with plane polarized light. The different phases are indicated with
657 numbers 1 (gypsum), 2 (anhydrite) and 3 (lutite/carbonate).

658 *Figure 9:* Geoelectrical classification of calcium sulphate rocks, depending on their gypsum-
659 anhydrite-lutite fraction. The resistivity values are shown in the background (Figure 7C).

660
661
662 ANNEX

663 *Annex 1:* Results of the laboratory measurements on synthetic pills made by mixing powdered pure
664 anhydrite or gypsum with clay. G samples correspond to gypsum-lutite pills, while A samples
665 correspond to anhydrite-lutite pills. Samples with a sulphate fraction of 70% or above have been

666 measured with a nanoammeter and the rest with a microammeter. The mean resistivity for each
667 fraction and the standard deviation is showed in Figure 5.

THE ELECTRICAL PROPERTIES OF CALCIUM SULPHATE ROCKS FROM DECAMETRIC TO MICROMETRIC SCALE

UNCHANGED FIRST REVISION (second revision is placed after this one)

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ABSTRACT

Sulphate rocks have a sedimentary evaporitic origin and are present in many deposits worldwide. Among them, gypsum (dihydrated calcium sulphate) is the most common and is exploited for industrial purposes. Anhydrite (calcium sulphate) is frequently found in gypsum quarries and in non-outcropping sulphates. The greater hardness of anhydrite compared to gypsum causes a problem for gypsum extraction; quarry fronts have to be halted as soon as anhydrite is found. In this work the electrical properties of calcium sulphates have been studied by means of geoelectrical methods.

A direct relationship between the electrical conductivity values of the calcium sulphate rocks and their lithological composition has been established with the lutitic matrix being the main controlling factor when it is well connected. When the matrix is under the percolation threshold the sulphate phases are dominant, and the electrical response of the rocks depends on the percentage of each phase. When the rock is matrix dominant, the electrical resistivity trend fits with the Hashin-

26 Shtrikman lower bound for multiphase systems (considering gypsum, anhydrite and matrix as the
27 components). On the other hand, when the rock is calcium sulphate dominant the trend shows the one
28 of the Hashin-Shtrikman upper bound. The reference electrical resistivity value of pure anhydrite
29 rocks has been defined as $10^4 \Omega.m$ and geoelectrical classification for calcium sulphate rocks has been
30 elaborated. With this classification it is possible to differentiate between calcium sulphate rocks with
31 different composition from their electrical resistivity value. This classification has been checked with
32 field examples and calculating the theoretical resistivity value of thin section photographs with the
33 program ELECFEM2D. The electrical behavior of calcium sulphate rocks is a good reference for other
34 type of rocks with electrically differentiated components, and similar methods can be used to define
35 their geoelectrical responses.

36

37 **Keywords:** Gypsum, Anhydrite, Sulphate, Electrical Conductivity

38

39

40 1. INTRODUCTION

41 Evaporites are sedimentary rocks originated from evaporation of salty water. Sulphates are one
42 of the principal groups of evaporitic rocks and the principal sulphate minerals are: gypsum
43 ($\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$), anhydrite (CaSO_4), glauberite ($\text{Na}_2\text{Ca}(\text{SO}_4)_2$) and thenardite (Na_2SO_4) (Warren, 2006).
44 Texturally, sulphate rocks are mainly crystalline; but may appear with clastic textures when they are
45 reworked. They retain only a reduced primary porosity ($<1\%$), display a restricted mineralogical (and
46 geochemical) composition and can appear combined with a lutitic matrix (mainly composed of clay
47 and microcrystalline carbonates). These rocks are extensively affected by diagenetic processes which
48 can change their texture into microcrystalline. Gypsum tends to transform to anhydrite when buried
49 because of dehydration, and the opposite process also takes place when anhydrite is affected by
50 weathering and superficial waters (Holliday, 1970).

51 Gypsum deposits are exploited for industrial purposes. It is mainly used in construction as
52 drywall and as an ingredient for plaster, but it is also used in other industries (Bustillo et al., 2001).
53 Gypsum quarries occur worldwide, with the USA and Iran as the largest producers. One of the most
54 important problems found while quarrying gypsum is the presence of anhydrite. By comparison with
55 gypsum, anhydrite is harder and denser. The drilling machines can be damaged by anhydrite bodies.
56 Hence, the exploitation must be stopped immediately. Anhydrite is also used by industry for different
57 purposes, but because of the exploitation difficulties it is mainly obtained by dehydration of previously
58 extracted gypsum. Anhydrite (from gypsum dehydration) is commonly found deeply buried (until 500-
59 1000 m; Shearman, 1985; Warren, 2006). It rarely crops out because it tends to hydrate and transform
60 into gypsum.

61 Geoelectrical techniques are proposed as tool for studying these sulphate deposits. Electrical
62 resistivity tomography (ERT) is a geophysical technique which can be used to obtain an image of the
63 electrical resistivity distribution of the subsurface. For this purpose an array of metal electrodes are
64 planted in the soil and the difference of electrical potential is measured between pairs of them while a
65 direct current (DC) is passed between two others. The arrangement of these 4 electrodes depends on

66 the electrical array that has been selected and the measurement is repeated along the string of
67 electrodes at different spacings and positions. The apparent resistivity values obtained are inverted into
68 resistivity values as a function of depth and position using inversion software (RES2DINV, Geotomo
69 Software, ver. 3.5). This method is a rapid, non invasive and relatively low-cost.

70 Gypsum deposits have been successfully identified with ERT profiles (Lugo et al., 2008;
71 Guinea et al., 2009; Guinea et al., 2010a). Guinea et al. (2010b) produced a geoelectrical classification
72 of gypsum rocks establishing a direct relation between their electrical resistivity value and the
73 percentage of lutitic matrix (Table 1). In that study the anhydrite phase was not considered, but this
74 mineral very often appears in gypsum rocks. The scientific literature shows anhydrite to have a large
75 range of resistivities from <100 to 10^{10} Ω .m (Table 2; Jakosky, 1950; Parkhomenko, 1967; Rider,
76 1986; Robison and Çoruh, 1988; Choteau et al., 1997; Asfahani and Mohammad, 2002; Lugo et al.,
77 2008). The variation in the electrical resistivity value of anhydrite in these publications is related to the
78 presence of gypsum, but the influence of the lutitic matrix is not mentioned.

79 The aim of this study is to measure the electrical resistivity of pure anhydrite at zero frequency
80 and to establish the effect of compositional variations in the gypsum-anhydrite-lutite rock system. This
81 problem will be studied from three different angles, namely numerical modeling, laboratory
82 measurements and field data. The information thus obtained should help to interpret geoelectrical data
83 in future surveys on sulphate rocks.

84

85 **2. FIELD DATA**

86 *2.1 Geological setting*

87 During the Lutetian (Middle Eocene) a large marine evaporitic sequence was deposited in the
88 South Pyrenean Foredeep (Rosell and Pueyo, 1997). In the La Garrotxa area (eastern Pyrenees)
89 secondary gypsum (as product of the hydration of anhydrite) crops out extensively and anhydrite has

90 been found in borehole logs with other evaporitic rocks such as halite (Carrillo, 2009). Close to the
91 village of Beuda (Girona, Spain) there is a quarry in which gypsum has been exploited since at least
92 the 1930s. There are many sculptures made of alabaster (pure secondary microcrystalline gypsum)
93 from the Middle Ages for which geochemical analysis has demonstrated that they were extracted from
94 the Beuda gypsum unit (Inglés et al., 2009).

95 Nowadays the quarry has been largely developed and anhydrite crops out in many places and
96 where the exploitation has consequently been stopped. The gypsum of the Beuda unit was produced by
97 hydration of anhydrite and therefore there are still some anhydrite relict bodies embedded in the
98 gypsum. In the walls of the quarry it is possible to observe boundaries between gypsum and anhydrite
99 usually displaying a quite pure anhydrite core and a transition to pure gypsum (Figure 1A). The purity
100 of the calcium sulphate varies from higher than 90% to close to 75% in certain layers (Figure 1B). The
101 changes in the purity of both gypsum and anhydrite rocks and the complex geometrical relations
102 between them make these deposits very heterogeneous. In some cases matrix bearing gypsum appears
103 in contact with pure anhydrite and in other cases the anhydrite does not appear as a body but as
104 fragments embedded in gypsum and filled with gypsum veins (Figure 1C). In other places anhydrite
105 appears massive with little gypsum within (Figure 1D). Three ERT profiles (figure 2, A, B, and C)
106 have been performed in the Beuda gypsum quarry. Profile D (Figure 2D) has been performed in the
107 same formation of the Beuda quarry, close to the village of Serinyà. In the area studied there are
108 sulphate layers under a soil. In the nearby outcrops pure secondary gypsum appears, but at depth, the
109 sulphates probably transform into anhydrite as it has been observed in the region (Carrillo, 2009).

110 Marine evaporitic deposition took place during the upper Eocene on the Catalan margin of the
111 Ebro basin (Ayora et al., 1994). The Odena gypsum unit was extensively exploited during the 20th
112 century and there are many abandoned quarries in the region. Profile E has been carried out in an
113 abandoned quarry near to the village of Odena where anhydrite crops out (Figure 2E).

114 In the Montes de Torrero area (Zaragoza, Spain) there is a Miocene evaporitic formation
115 hundreds of meters thick. The area has been studied by means of boreholes in which gypsum,

116 anhydrite, glauberite and halite were found among other minerals. This formation has a large quantity
117 of matrix in every layer (Ortí, 2000; Salvany, 2009). The outcropping materials are mainly gypsum,
118 which formed from the hydration of anhydrite or glauberite (Figure 1E), and more than 50% matrix
119 (composed of clay and marl). An ERT survey has been performed where borehole B4 was drilled
120 (Figure 2F). The log of the borehole shows gypsum to a depth of 35 m, then glauberite to a depth of 69
121 m followed by anhydrite to 80 m with some interbedded layers of halite or glauberite (Salvany, 2009).
122 The whole log shows significant fractions of matrix at all depths as such as at the surface.

123 *2.2 Methods*

124 A total of six ERT profiles have been carried out at anhydrite rock deposit areas in the South
125 Pyrenean Foredeep and Ebro Basin (North East of Spain; Figure 3). The examples are presented below
126 starting with those performed in quarries (Figure 3; A, B, C and D) and afterwards in areas with no
127 evaporites that crop out (Figure 3; E and F). All the profiles performed in quarries show a high
128 fraction of sulphates and therefore relatively high electrical resistivity values.

129 A Syscal Pro Switch ERT system with 48 electrodes and an external power supply has been
130 used to carry out the data acquisition. The electrode spacing for the measurements in quarries was 0.5,
131 1.5 or 2 m depending on the local conditions. In the profiles performed where no evaporates crop out,
132 the electrode spacing was 10 m to increase the depth of investigation because anhydrite deposits tend
133 to appear below other formations (because at shallow depth they transform into gypsum). The used
134 electrodes for the data acquisition were made of stainless steel and they were nailed in the terrain by
135 means of hammers. There are many possible array configurations in geophysical prospection (Ma et
136 al., 1997; Furman et al., 2003; Szalai and Szarka, 2008) which may be applied to anhydrite rocks. The
137 Wenner-Schlumberger and Dipole-Dipole arrays have been selected depending of the structure under
138 study, and the Dipole-Dipole has been used were lateral electrical resistivity changes are important.
139 The apparent resistivity data of performed ERT profiles has been inverted with the RES2DINV
140 program; that is available from 1995 (Loke and Barker, 1996). The inversion process has been carried
141 out with 5 iterations for each profile. With this number of iterations the data converges in all cases

142 achieving an acceptable RMS error. Additional iterations do not vary the RMS error significantly but
143 increase the electrical resistivity value in the low sensitivity areas (i.e., the pure sulphate rocks). As
144 explained later in Section 2.3, the resistivity range calculated (with 5 iterations) in pure anhydrite
145 bodies at depth is alike to the apparent resistivity measured in shallow pure anhydrite rocks.

146 Sulphate samples have also been collected in some of the profiled areas in order to measure
147 their composition. The samples have been powdered and 0.5 g from each one has been dissolved in
148 250 ml of distilled water in accordance with the solubility of calcium sulphate in water. The solutions
149 were shaken for 24 hours and then filtered. The residue left after filtering correspond to the non-
150 soluble phases, which are made up of the lutitic matrix (including carbonates, quartz and other minor
151 accompanying minerals). The residue was weighted in order to estimate the fraction of the in sulphate
152 phases.

153 *2.3 Results and discussion*

154 In the Beuda quarry some different areas have been studied. The profiles A and B have been
155 performed upon areas in which massive anhydrite was found and afterwards was buried under quarry
156 waste materials. The profiles were spread above the infilling. The result of the inversion for Profile A
157 (Figure 3A) display an upper part with relatively low electrical resistivity values (between 10 and 200
158 $\Omega.m$), which corresponds to the quarry waste. Underlying these materials there is a homogeneous body
159 with high resistivity value (up to $10^4 \Omega.m$), which has been interpreted as pure anhydrite (Lugo et al.,
160 2008). In the case of Profile B, which was performed perpendicularly to Profile A, the inverted
161 resistivity section (Figure 3B) displays a lateral electrical resistivity variation below the quarry waste
162 layer. A well was drilled in the middle of profile B and high hardness was found at 6 meter depth, but
163 no core was recovered. This hardness has been interpreted as anhydrite rock with certain quantity of
164 matrix.

165 The profile C has been measured in other location where anhydrite had also stopped the
166 exploitation of the quarry. The electrodes were inserted almost directly into the sulphate rocks and

167 both anhydrite and gypsum appeared in the ground surface. In the inverted resistivity section (Figure
168 3C) there is displayed a lateral variation of electrical resistivity ranging from 10^3 to 10^4 Ω .m. The
169 larger resistivity values are limited with the outcropping of massive anhydrite, while the lower ones
170 are related to the presence of gypsum, and the intermediate values correspond to the transition between
171 the two pure phases.

172 Profile D has been performed in an abandoned quarry near to the village of Odena where
173 anhydrite crops out. The inverted section (Figure 3D) shows electrical resistivities ranging from 10^3 to
174 10^4 Ω .m, similarly to the observations in the Beuda quarry. In the areas in which the value is larger,
175 massive anhydrite is observed. Lower electrical resistivity than 500 Ω .m are related to lutitic
176 sedimentary layers.

177 Profile E has been performed in an evaporitic basin with no outcrops. The inversion of the
178 profile (Figure 3E) displays a shallow deposit with a low electrical resistivity value (50 Ω .m) which
179 corresponds to the underlying materials. Below this layer there is a high resistivity body ranging from
180 1000 to more than 5000 Ω .m and with a more conductive structure in the central part (between 100
181 and 200 Ω .m). This structure represents a fault present in the area, and identified on the surface by
182 geological evidence (Carrillo, 2009).

183 The profile F performed in Montes de Torrero area has been modified from Guinea et al.
184 (2010b). In the inverted image (Figure 3F) the whole deposit shows a general trend of 30-50 Ω .m with
185 some bodies slightly more resistive (up to 300 Ω .m at the most resistive points). Those bodies would
186 represent a higher grade of the deposit (up to 60% in sulphates) in these zones, this grade changes are
187 related to primary depositional processes and they are very common in these materials (Guinea et al.,
188 2010a). In any case it is not possible to differentiate between anhydrite and gypsum layers because the
189 electrical behavior of the deposit is dominated by the abundant matrix.

190 As general trend, sulphate rocks with high purity in anhydrite show an electrical resistivity
191 value up to 10^4 Ω .m after the inversion (Lugo et al., 2008). This value is considered to be the reference

192 for pure anhydrite rocks because in some profiles in which some of the shallowest points have been
193 measured almost directly above massive anhydrite rocks, show an apparent resistivity value larger
194 than 5000 Ω .m. In these cases the apparent and the inverted resistivities are similar but a slightly lower
195 for the apparent resistivity because the electrodes are inserted into a thin clay layer. When these rocks
196 are mixed with gypsum forming pure sulphate rocks with both phases, which are the most common in
197 the quarries, they display an intermediate value of resistivity ranging from 1500 to 5000 Ω .m
198 depending on the quantity of each phase. As the distribution of the anhydrite in the gypsum deposits is
199 very heterogeneous due to the rehydration processes, the tomography lines show heterogeneous bodies
200 with different electrical resistivity values and transitional zones. Values close to 1000 Ω .m are related
201 to the purest gypsum rocks or to pure anhydrite with a significant quantity of matrix rocks. When the
202 matrix has a large volume fraction, it is not possible to differentiate is gypsum from anhydrite with
203 ERT. In these cases, the rocks will display a resistivity below 100 Ω .m, which is significantly lower
204 than the resistivity of sulphate-rich deposits. The low electrical resistivity of sulphate deposits with
205 large matrix volume fraction was studied further by Guinea et al. (2010b) for the case of gypsum rocks
206 (without anhydrite).

207

208 **3. LABORATORY MEASUREMENTS**

209 *3.1 Methods*

210 Many authors have measured the electrical conductivity of geological materials (Keller, 1966;
211 Lockner and Byerlee, 1985; Guéguen and Palciauskas, 1994; Glover et al. 1996; Giao et al., 2003;
212 Rusell and Barker, 2010; among others). Guinea et al (2010b) made eleven gypsum-clay pills in
213 different proportions with a range from 0 to 100% of $\text{CaSO}_4 \cdot \text{H}_2\text{O}$ at intervals of 10% in composition
214 and measured their electrical conductivity. Three sets of eleven anhydrite-lutite pills and three sets of
215 gypsum-lutite pills have been made using the same methodology, parameters and resources. The
216 compositional error of the pills is below 1%, because the weigh corresponding to the volume of each

217 fraction has been measured with a precision scale (mod. Sarorius B3100S) with a resolution of 0.01 g
218 (the pills have a total weight of 13.5 g). The pills have a cylindrical shape with a radius of 2 cm and a
219 width of approximately 0.50 cm. The aim of these measures is to define the importance of the matrix
220 presence in calcium sulphate rocks.

221 The conductivity measurement was carried out in accordance with the UNE 21-303-33
222 regulation (1983) with an electrical circuit in which the samples act as electrical resistance (Figure 4).
223 The electrical power source was a laboratory DC converter power supply with switchable voltage (0–
224 32 V) and current (0-10 A). Changes in the amperage above 1A do not affect the essays so an output
225 current of 2A has been selected. In order to measure the amperage of the electrical current after
226 traversing the resistance (the sample), an analogical microammeter (Demestres, mod. 540) with a
227 range of 0-100 μ A with an accuracy of 1 μ A or a nanoammeter (Monroe, mod. 285) with a range of
228 \pm 200 nA and 0.1 nA resolution and an accuracy of 2% have been used. The potential difference is
229 measured by a voltmeter (MY-67) with a resolution of 0.001 V connected to both sides of the pills.
230 The electrodes used on the samples are made of stickers with metallic buttons as the ones used for
231 electrocardiograms. The button has a conductive gel in the sticking side, forming a 0.75 cm-radius
232 circled face (which will be considered the surface of the electrode). This gel is directly connected to
233 the samples. The pills and the electrodes are situated above a paperboard insulator. The barreling
234 effect is low because the distance between the electrodes is relatively small (approximately 0.50 cm).
235 Due to the difference between the area of the electrodes and the area of the pills, there is a leak path
236 for the electrical current (Roth, 1959). The measurements were made after the reading stabilizes (10
237 seconds after the power supply is switched on). Polarization causes errors after a certain time in the
238 pills with large fractions of clay. The longest time measures are not considered representative for
239 geophysical surveys because geoelectrical methods use a short current injection time. Each pill has
240 been measured three times, making a total of 6 measurements for each volume fraction. Ohm's law
241 can be applied to calculate the conductivity (σ) or resistivity (ρ) of the sample for a known current
242 density (j) and field (E) (Eq. 1):

243

$$j = \sigma E = E/\rho$$

244

245

246

It is possible to measure the resistance (R) of the samples. As the thickness (L) of the sample and the surface area of the electrode (S) are known, the electrical resistivity (ρ) can be calculated (Eq. 2):

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$$R = \rho L/S$$

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3.2 Results and discussion

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The resistivity calculated for the gypsum-lutite and anhydrite-lutite pill sets is shown in Figure 5 (full measurements table is shown in Annex 1). The mean resistivity is indicated by symbols together with an error bar representing the standard deviation. The measures performed on gypsum-lutite pills showed a similar trend to the one presented by Guinea et al. (2010b). The pills ranging from 70 to 100% in gypsum fraction were more accurate in the present study because the current was measured with a nanoammeter instead a microammeter. The pills ranging from 0 to 40% in gypsum fraction displayed a slightly increasing trend of the electrical resistivity (with a mean value ranging from 6 to 33 Ω .m). The 50 and 60% gypsum fraction pills displayed a transitional range of resistivity (with mean values of 72 and 137 Ω .m respectively). Finally, the pills with a volume fraction of gypsum ranging from 70 to 100% displayed a resistivity of >700 Ω .m. The trend showed by the anhydrite pills is similar to the one showed by the gypsum pills for the case of pills with a sulphate fraction from 0 to 50%. There are slight differences between them, but both sets are in the same range of resistivities. The anhydrite-pills with a sulphate fraction of 60% or above are noticeably more resistive than their equivalent in gypsum pills (ranging from 1012 to 7609 Ω .m in mean resistivity).

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It is evident that the grades below 60% are dominated by the lutitic matrix and the sulphate component affects the measurement negligibly. The sulphate volume fractions above 70% showed high resistivity values in which the dominant component is the sulphate phase. Between the two differentiated trends there is a transitional zone which represents the loose of the connectivity of the

267 matrix. As in the measures of gypsum pills by Guinea et al. (2010b), the pills with large quantity of
268 clay component polarize with measuring time. The chargeability of clay has been widely described
269 before (Takakura, 2006; Deucester and Kaufmann, 2009).

270 Percolation theory states that in a cluster with a component randomly distributed (meaning the
271 lutitic matrix for this case) there is a percolation threshold which represent the minimal quantity of the
272 component required in order to obtain a long-range connectivity (Stauffer and Aharony, 1985). This
273 theory has been widely used to predict characteristics of rocks as the connection of their porosity or
274 fractures (Karmakar et al., 2003; Wang et al., 2007). When the fraction of the component is below the
275 percolation threshold, the cluster is not considered to be connected. In our system the percolation is
276 controlled by conduction through matrix which is much more conductive than the sulphate phase.
277 Anhydrite or gypsum components are dielectric (act as resistances) and they conduct little electrical
278 current while the matrix fraction is above the percolation threshold. Below the percolation threshold,
279 the electrical current finds no connected pathways in the matrix and passes through the sulphates.
280 Hence, the relative proportion of gypsum and anhydrite phases when the presence of matrix is above
281 40%, do not affect the electrical resistivity value of the whole rock.

282

283 **4. THEORETICAL CALCULATIONS**

284 *4.1 Methods*

285 Physical properties of rocks are mainly functions of their microstructure (Guéguen and
286 Palciauskas, 1994). Two important mathematical approaches are effective medium theory (EMT) and
287 percolation theory. The EMT (Kirpatrick, 1973) approximation is quite good for rocks with quasi-
288 uniform distributions where only a small degree of heterogeneity is observed, although they cannot
289 describe correctly the phenomenon of clustering (Guéguen et al., 1997) when the heterogeneity is
290 large. Moreover, the knowledge of the geometric distribution and connectivity of the minor phase is of
291 great importance. Percolation theory describes the medium in terms of probabilities of the connectivity

292 but does not provide bulk physical properties. Here, we propose a method to determine the physical
293 properties of composite materials that combines the EMT and the percolation theory. On one hand, the
294 EMT is used to calculate the bounds of the physical properties depending on the amount of the matrix
295 phase present. These limits correspond to the two extreme situations where the matrix phase is totally
296 interconnected or disconnected. On the other hand, the percolation theory is used to determine the
297 probability of having a connected or interconnected matrix phase assuming that it is distributed in a
298 single cube distribution.

299 The effective properties of composites, in particular electrical conductivity, have been studied
300 analytically for a long time for a very simple cases (i.e., Maxwell (1881) used effective medium theory
301 to derive the bulk conductivity of spheres dispersed in a continuous medium). The rocks can be
302 considered as random materials of different property phases at various length scales. To compute the
303 effective properties of such materials requires knowledge of the microstructure and require numerical
304 computation. Garboczi (1999) wrote an algorithm and the consequent FORTRAN code to compute
305 using both finite difference and finite element codes to calculate the electrical and elastic effective
306 properties of materials with different phases from digital images.

307 In this paper the program ELECFEM2D.F from Garboczi (1999) has been used to compute the
308 effective conductivity of gypsum-anhydrite rock samples. The method to calculate the electrical
309 conductivity of these rocks is to analyze thin section images in which the amount of both anhydrite
310 and gypsum proportion together with the one of the lutitic matrix is known. With this software it is
311 possible to obtain a resistivity distribution model based on a microphotograph.

312 In order to perform the theoretical calculation of photographs with the program
313 ELECFEM2D.F, the pictures must be converted from an image format file (e.g., JPG, JPEG, GIF,
314 PNG) into an ASCII file. This has been carried out with a converter which creates numerical files from
315 the pixels of the input image. Depending on the color range of these pixels, a numeric value, which is
316 related to a user defined electrical resistivity value, is assigned. As the images used display lutite,
317 gypsum and anhydrite phases; 10 , 10^3 and 10^4 $\Omega\cdot\text{m}$ electrical resistivity values have been selected

318 respectively. This selection will be discussed further in Section 4.2. The number of variables is user
319 defined and 2 variables (1 and 2) have been selected for photographs displaying 2 phases (any couple
320 of lutite-gypsum-anhydrite) and 3 variables (1, 2 and 3) when the 3 of them are present. Each image
321 was previously treated with an image processing program in order to homogenize the color ranges in
322 order to improve the detection of each phase.

323 Once the ASCII file is created, it can be used by the ELECFEM2D.F program. The program
324 divides the surface into 8400 (150×56) cells with an electrical resistivity value assigned to each one,
325 and calculates the current intensity remaining after crossing the system in the x or y direction. Both
326 directions and the arithmetic mean value have been calculated; the differences are related to the
327 anisotropic distribution of the phases. The selected potential gradient was set to 1 V/m.

328 4.2 *Mixing models for two and three phase systems*

329 Many mixing models have been published in order to predict the bulk conductivity of a porous
330 medium (Glover et al. 2000). In the case of sulphate rocks there is no porosity; hence, the resistivity
331 (or conductivity) of the bulk rock depends on the fraction (γ) and the electrical resistivity value (ρ) of
332 each component and on the connectivity and geometrical distribution of the matrix (which has the role
333 of a conducting fluid in a saturated porous medium). Different mixing models (Parallel, Perpendicular,
334 Random, Modified Archie's law and Hashin Shtrickman bounds) have been calculated for the case of
335 two-phase sulphate rocks (gypsum-lutite and anhydrite-lutite) with different proportions of sulphate
336 and matrix. The electrical resistivity values selected for gypsum and lutite phases have been 10^3 and
337 $10 \text{ } \Omega\cdot\text{m}$, respectively (Guinea et al., 2010b). The electrical resistivity value selected for pure anhydrite
338 phase has been $10^4 \text{ } \Omega\cdot\text{m}$, in accordance with the maximum value measured in field examples and the
339 bibliography (Table 2).

340 Parallel and Perpendicular mixing models (Table 3A and B; Somerton, 1992; Guéguen and
341 Palciauskas, 1994) describe the conductivity of a layered distribution of phases with a constant
342 arbitrary thickness arranged axially or normally (in each case) to the current flow. The random model

343 (Table 3C; Warren and Price, 1961; Shankland and Waff, 1977) describes the bulk conductivity of a
344 material with randomly distributed arbitrary volumes of the conductive phase. Glover (2000)
345 described a mixing model (Table 3D) derived from Archie's law (Archie, 1942), considering the
346 boundary conditions implied by geometrical constraints. To calculate this model, the cementation
347 exponent m has to be defined for each phase. This variable depends on the connectedness of the phases
348 and, as long as in the present case there is no information about this connectedness, it is considered
349 that $m_1=m_2=1$. Hashin and Shtrikman (1963) defined the electrical resistivity value bounds (HS
350 bounds) of a bulk rock from effective medium considerations. These bounds represent the theoretical
351 maximum (upper bound; Table 3E) and minimum (lower bound; Table 3F) electrical resistivity value
352 that any material formed of two different phases with a certain fraction can display.

353 The mentioned mixing models are displayed in the Figure 6 for both gypsum-lutite (Figure
354 6A) and anhydrite-lutite (Figure 6B) systems. The modified Archie's law model has the same trend
355 that is calculated for the case of parallel model; this is because the cementation exponent m is
356 considered 1 for every phase. Additionally to the theoretical trends of the mixing models, the
357 resistivities calculated in the laboratory measurements are displayed. The pill samples with a fraction
358 of sulphate phases of 50% or below show a similar trend to the one displayed by the HS⁻ model. This
359 is also shown in the field data in the profiles in which the sulphate formations have a high quantity of
360 matrix within. In the other hand, the resistivity of the pills with a sulphate fraction of 70% or above is
361 closer to the perpendicular or HS⁺ models. In the case of the anhydrite pills with high sulphate
362 fraction, they fit better to the random model; but this can be related to the fact that the anhydrite pills
363 are slightly watered during their elaboration. The field data obtained in anhydrite rocks also indicate
364 that the observed resistivity ranges fit better to the perpendicular or HS⁺ models. The values obtained
365 for the pills with 60% in sulphate fraction are transitional, which represents the percolation threshold.
366 Theoretically the percolation threshold occurs in a single phase fraction but in the case of real rocks
367 transitional values are displayed in this range of composition.

368 From the trends observed for two-phase systems, it can be considered as approximation that
369 the HS bounds define the resistivity of gypsum and anhydrite rocks depending on the quantity of

370 matrix present. When the matrix is percolating (sulphate fraction of 50% or below), the resistivity of
371 the sulphate rocks is bounded to the HS- model. In the case of non percolating matrix (sulphate
372 fraction of 70% or above), the resistivity is bounded to the HS⁺ model. A general form of the bounds
373 for n-phases was given by Berriman (1995). With his formula it is possible to construct a ternary
374 graphic for 3-phased rocks (Ledo and Jones, 2005). The gypsum-Anhydrite-Lutite (GAL) system has
375 been calculated for both upper (Table 3G) and lower (Table 3H) HS bounds. In the case of lower
376 bound (Figure 7A), the system is clearly dominated by the lutitic component; the iso-resistivity lines
377 are parallel between them showing no appreciable variation in the gypsum-anhydrite axis but when the
378 lutite fraction is less than 10%. The values of resistivity are very low in general, showing less than 100
379 $\Omega\cdot\text{m}$ for a sulphate fraction of 70%. The upper bound (Figure 7B) displays a very different trend
380 dominated by the anhydrite fraction, but in this case the 3 components affect the bulk resistivity value
381 of the rock. The electrical resistivity values are much larger than in the case of lower bound achieving
382 1000 $\Omega\cdot\text{m}$ with only 40% of anhydrite. As it has been previously shown, the electrical behavior of the
383 rocks is the one of lower HS bound when the quantity of sulphate is of 50% or below and the one of
384 upper bound when is of 70% or above. Thus it is expected that the real distribution of the electrical
385 resistivity for the GAL system should be a combination between the upper and lower HS bounds
386 (Figure 7C).

387 *4.3 Results and discussion*

388 In order to check the accurateness of this GAL diagram, the theoretical electrical resistivity
389 value of real thin section rock photographs (Figure 8) has been calculated with ELECFEM2D
390 program. Lutitic matrix display brownish coloring while both anhydrite and gypsum have are
391 transparent underplane polarized light; having anhydrite higher relief than gypsum (its bounds are well
392 marked with dark lines). With crossed polarized light, gypsum and anhydrite can be easily
393 differentiated because of the different coloring of the anhydrite (pink, green, blue, ...) in contrast with
394 the gray colors of the gypsum crystals. The standard electrical resistivity values selected for the
395 gypsum, anhydrite and lutitic matrix phases have been 10^3 , 10^4 and $10 \Omega\cdot\text{m}$ respectively, as has been
396 assigned before. The electrical resistivity of the bulk sections has been measured in both x and y

397 directions; when the distribution of the components is homogeneous these values would be considered
398 similar. For each thin section the fractions of the components are calculated by the program so it is
399 possible to obtain the electrical resistivity value corresponding to these fractions calculated with
400 different mixing models (Table 4).

401 The results show that the mean of the calculated electrical resistivity values in x and y
402 directions are in general close to HS^+ bound when the fraction of sulphate is 70% or higher (Figure 8,
403 thin sections A, D, E, F, G and H; Table 4) and to the HS^- bound when the fraction of matrix is
404 abundant (Figure 8, B and I; Table 4). There is a good match between the corresponding position of
405 each sample in the figure 7C, according to their components percentages, and the calculated resistivity
406 values. In the case of thin sections C and J there is abundant matrix (58 and 52% respectively);
407 nevertheless, the calculated resistivity values are slightly larger than that expected for such mixture.
408 This is due to that the phases are not scattered and randomly distributed within the samples but
409 forming compact and pure areas. This represents large heterogeneities which change the percolating
410 behavior (we have considered it only for regular distributions of the phases as in the case of the pills)
411 of the bulk rock and makes the transition zone larger. In any case the values are always much closer to
412 the lower bound than to the upper one. The parallel/Modified Archie's law and perpendicular (serie)
413 models does not fit well to the calculated resistivities. The random model fits well in many cases but
414 in samples with large fraction of anhydrite, calculated resistivity is too high (especially in C thin
415 section).

416 At larger scale (as in the ERT profiles) the rocks are in general more homogeneous and should
417 fit to the HS lower bound for compositions of 0-60% in lutitic matrix. The microscopic anisotropies do
418 not affect to the electrical conductivity of the bulk deposit if we increase the scale. In any case, it is
419 possible to observe cases of heterogeneities at metric scale. When these heterogeneities are large, they
420 can be considered as different rocks (for example a gypsum-rich lutite body within a larger pure
421 gypsum host-rock). In any case, heterogeneities below the detection limit of the method will be
422 considered as a single rock. Another possible case is a layered deposit in which every layer has
423 different purity in the sulphate phase. If the difference among grades is low, which is the most

424 common case, the whole sequence can be considered as a single member with a mean grade. Rarely
425 sulphate deposits have great variations of grade from layer to layer forming a heterogeneous sequence.
426 Sudden variations in the grade exist, but are normally associated with the limit of a sequence or a
427 stable change in the depositional conditions. In the case of having layering between almost pure matrix
428 and highly pure sulphates, the transitional values of resistivity will increase their range as happens in
429 the case of the microphotographs.

430

431 **5 GEOELECTRICAL CLASSIFICATION OF CALCIUM SULPHATE ROCKS**

432 With the GAL diagram obtained combining both HS^+ and HS^- boundaries for a gypsum
433 anhydrite-lutite system (Figure 7C) a geoelectrical classification has been elaborated differentiating 6
434 calcium sulphate rock types (Figure 9). When the lutitic matrix is connected at long range (in the case
435 of sulphate fraction of 50% or below) the system is matrix dominant and therefore there is no
436 possibility of differentiating between gypsum and anhydrite components; these rocks are classified as
437 Lutites and Gypsum/Anhydrite rich Lutites. The electrical resistivity of this groups range from 10 to
438 100 $\Omega.m$. When the sulphate grade is of 70% or above, the rock will be considered as pure Gypsum
439 when it ranges from 700 to 1000 $\Omega.m$ as was stated by Guinea et al. (2010b) for the case of gypsum-
440 lutite systems. If the sulphate mineral is mainly anhydrite (more than 90%) the rock is considered pure
441 Anhydrite and its electrical resistivity value range from 2500 to 10^4 $\Omega.m$ depending on the rock grade.
442 In the case of presence of both gypsum and anhydrite sulphate phases, the rock is considered Gypsum
443 with Anhydrite (1000 to 2000 $\Omega.m$) or Anhydrite with Gypsum (2000 to 5000 $\Omega.m$). The values of
444 pure Anhydrite and Anhydrite with Gypsum overlap; in this case it is possible to bond the electrical
445 value to Pure Anhydrite rocks when there is no evidence of rehydration and to the Anhydrite with
446 Gypsum otherwise. Between Lutites and Gypsum/Anhydrite rich Lutites and the sulphate pure rocks
447 there is a transitional area displaying transitional values from 100 to 700/2500 $\Omega.m$ (depending of the
448 sulphate composition). The lower boundary of Transitional Gypsum/Anhydrite rocks has been selected
449 as 55% in sulphate fraction instead of 60% because the measures in pills have shown that the 60%

450 values display an electrical resistivity increasing trend; the upper boundary is 70% in gypsum fraction.
451 This transitional area is displayed with a resistivity-trend calculated by interpolation between lower
452 and upper HS bounds, but the resistivity in the transition zone is uncertain and therefore the displayed
453 trend is only a reference.

454 For the microscopic scale, it has been shown that the transitional range is wider (including
455 rocks between 55 and 70% in sulphate fraction, depending of the anisotropy). For the cases of sulphate
456 fractions of 55% or below or higher than 70%, the values obtained are similar to the corresponding HS
457 bound. At larger scale, the ERT lines have shown relationships between composition and resistivity
458 values similar to the ones displayed in the classification of the Figure 9; that is, higher than 5000 $\Omega.m$
459 when the dominant phase is the anhydrite, 1500 to 5000 $\Omega.m$ for different proportions of gypsum and
460 anhydrite (with presence of little lutite) and close to 1000 $\Omega.m$ when the gypsum is the dominant
461 phase. For deposits with large amount of lutites, the obtained value has been $<60 \Omega.m$ in all cases.

462

463 **6. CONCLUSIONS**

464 The electrical properties of calcium sulphate rocks have been widely studied at different scales
465 with microphotographs, synthetic pills and geological deposits. Laboratory tests in pills have shown
466 that the matrix of calcium sulphate rocks may be affected by the percolation phenomena and therefore,
467 when the sulphate fraction in a rock is of 55% or below, the matrix controls the resistivity of the bulk
468 rock. When the sulphate fraction is of 70% or above, the sulphate minerals control the electrical
469 resistivity of the bulk rock.

470 The electrical resistivity value of anhydrite rocks range from 10 to $10^4 \Omega.m$, being larger in the
471 purest anhydrite rocks. This value is found in the field examples where the anhydrite appears in
472 massive form. The values observed in rocks with both gypsum and anhydrite (with minor matrix) have
473 ranged between 1500 and 5000 $\Omega.m$ depending on the quantity of each other. Large quantity of matrix

474 in sulphate rocks have shown low electrical resistivity values been unable to differentiate between
475 gypsum and anhydrite.

476 When the matrix of the calcium sulphate rocks is above the percolation threshold (i.e., more
477 than 45%), the electrical resistivity value fits the value calculated with the Hashin-Shtrikman lower
478 bound (HS^-), and when is embedded in the sulphate phase (i.e., 30% of matrix or less) the resistivity
479 follows the Hashin-Shtrikman upper bound (HS^+). If there are large heterogeneities in the distribution
480 of the phases, the resistivities of rocks with a matrix quantity ranging from 30 to 45% can display
481 transitional values (more than 100 $\Omega.m$, without reaching values of the purest sulphate rocks).
482 Therefore, it is possible to calculate any combination of these 3 components and the geoelectrical
483 classification has been elaborated for calcium sulphate rocks. With this classification is possible to
484 determine the purity of the sulphates and the presence of anhydrite in gypsum rocks, which is useful
485 for the characterization of the deposit.

486

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495

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610

611 **TABLE CAPTIONS**

612 *Table 1:* Geoelectrical classification of gypsum rocks (modified after Guinea et al. 2010b).

613 *Table 2:* Electrical resistivity values for anhydrite rocks in the literature.

614 *Table 3:* Summary of the equations of the mixing models used in the present study (modified from
615 Glover et al. 2000).

616 *Table 4:* Results of the theoretical calculations of electrical resistivity of the thin section photographs
617 with ELECFEM2D software. Parallel, Serie, Random, Archie's modified law and Lower (HS^-) and
618 upper (HS^+) Hashin-Shtrikman bounds have been calculated, only considering the proportion of each
619 phase. The calculated resistivity for each sample in both x' and y' directions is listed in the right
620 column. The corresponding images of the thin sections A to J are displayed in Figure 8.

621

622 **FIGURE CAPTIONS**

623 *Figure 1:* Photographs of the areas studied with ERT, A to C are taken in the Beuda quarry while D is
624 taken in the area of Odena and E in the Zaragoza formation. A) pure gypsum-anhydrite boundary with
625 a interdigitation between them; B) sulphate layers showing less gypsum fraction than in other areas;
626 C) anhydrite blocks filled with gypsum veins and embedded in a gypsum matrix; D) massive anhydrite
627 body; E) impure sulphate layers in Montes de Torrero area.

628 *Figure 2:* Distribution of evaporite formations in the Tertiary basins northeastern Spain indicating the
629 location of the nine studied ERT profiles with black dots (modified from Ortí et al., 2010).

630 *Figure 3:* Inverted electrical resistivity tomography data for the different areas studied (the locations
631 of the profiles are shown in figure 2). Profile F modified from Guinea et al. (2010b).

632 *Figure 4:* Electrical circuit to measure the electrical resistivity of the samples. It consists of a
633 switchable laboratory power-supply (EA-PS 3032-10B), two electrodes, a voltmeter (MY-67) and a

634 micro or nanoammeter depending on the samples (Demestres, mod. 540; and Monroe, mod. 285
635 respectively).

636 *Figure 5:* Semi-logarithmic plots representing the results of the measurements of gypsum-lutite (A)
637 and anhydrite-lutite (B) pills. The symbols represent the mean of the calculated resistivities for each
638 sulphate fraction (using 2 pills and 3 different measurements on both for each fraction) and the error
639 bar represents the standard deviation. The error on the X axis is not showed because is below 1%.

640 *Figure 6:* Different mixing models calculated for the case of gypsum-lutite (A) and anhydrite-lutite
641 rocks (B). The resistivity ranges obtained in the laboratory essays (Figure 5) are superimposed for both
642 cases.

643 *Figure 7:* Ternary plots showing Hashin-Shtrikman bounds for gypsum-anhydrite-lutite (GAL)
644 system. A) lower HS bound; B) upper HS bound; C) combined diagram considering the percolation
645 phenomena.

646 *Figure 8:* Microphotographs of thin sections of calcium sulphate rocks; D, E, H and I are taken with
647 cross polarized light and the rest with plane polarized light. The different phases are indicated with
648 numbers 1 (gypsum), 2 (anhydrite) and 3 (lutite/carbonate).

649 *Figure 9:* Geoelectrical classification of calcium sulphate rocks, depending on their gypsum-
650 anhydrite-lutite fraction. The resistivity values are shown in the background (Figure 7C).

651
652
653 ANNEX

654 *Annex 1:* Results of the laboratory measurements on synthetic pills made by mixing powdered pure
655 anhydrite or gypsum with clay. G samples correspond to gypsum-lutite pills, while A samples
656 correspond to anhydrite-lutite pills. Samples with a sulphate fraction of 70% or above have been
657 measured with a nanoammeter and the rest with a microammeter. The mean resistivity for each
658 fraction and the standard deviation is showed in Figure 5.

Table 01

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	Purity in Gypsum (%)	Resistivity (ohm.m)
Lutites and Gypsum rich Lutites	0-55	10-100
Transitional Gypsum	55-75	100-700
Pure Gypsum	75-100	700-1000

Table 02

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REFERENCE	RESISTIVITY (ohm.m)	AUTHOR'S COMMENTS
Lugo et al. (2008)	1000-11500	The bodies displaying the lowest values are related to the presence of gypsum from the hydration of anhydrite while the highest ones are related to pure anhydrite.
Asfahani and Mohammad (2002)	94-1200	The values are measured by vertical electrical soundings in a gypsum and anhydrite formation.
Choteau et al. (1997)	1000	Anhydrite appears in an halite-karnalite-tachyhydrite sequence.
Robinson and Çoruh (1988)	10^9 - 10^{10}	Anhydrite appears in a summary of different mineral resistivity values
Rider (1986)	10^4 - 10^{10}	Obtained from wireline logs of different sources.
Parkhomenko (1967)	$1.0 \cdot 10^9$	Listed in a summary of different mineral and rock resistivities
Jakosky (1950)	$1.0 \cdot 10^3$ / $1.0 \cdot 10^5$	Low and High resistivity ranges obtained from laboratory measurements

Table 03
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Name	Conducting phases	Equation
a) Parallel model	1+	$\sigma_{\text{eff}} = \sum_{i=1}^N \chi_i \sigma_i$
b) Perpendicular model	1+	$\frac{1}{\sigma_{\text{eff}}} = \sum_{i=1}^N \frac{\chi_i}{\sigma_i}$
c) Random model	1+	$\sigma_{\text{eff}} \prod_{i=1}^N \sigma_i^{\chi_i}$
d) Modified Archie's law	1-2	$\sigma_{\text{eff}} = \sigma_1(1-\chi_2)^p + \sigma_2\chi_2^m \text{ where } p = \frac{\log(1-\chi_2^m)}{\log(1-\chi_2)}$
e) Hashin-Shtrikman upper bound	2	$\sigma_{\text{eff}+} = \sigma_2 \left(1 - \frac{3(1-\chi_2)(\sigma_2 - \sigma_1)}{3\sigma_2 - \chi_2(\sigma_2 - \sigma_1)} \right)$
f) Hashin-Shtrikman lower bound	2	$\sigma_{\text{eff}-} = \sigma_1 \left(1 + \frac{3\chi_2(\sigma_2 - \sigma_1)}{3\sigma_1 + (1-\chi_2)(\sigma_2 - \sigma_1)} \right)$
g) Hashin-Shtrikman upper bound	3	$\sigma_{\text{eff}+} = \frac{1}{\left(\frac{\chi_1}{\sigma_1 + 2\sigma_2} \right) + \left(\frac{\chi_2}{3\sigma_2} \right) + \left(\frac{\chi_3}{\sigma_3 + 2\sigma_2} \right)} - \sigma_2$
h) Hashin-Shtrikman lower bound	3	$\sigma_{\text{eff}-} = \frac{1}{\left(\frac{\chi_1}{\sigma_1 + 2\sigma_3} \right) + \left(\frac{\chi_2}{\sigma_2 + 2\sigma_3} \right) + \left(\frac{\chi_3}{3\sigma_3} \right)} - 2\sigma_3$

Table 04

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Thin section	COMPOSITION (%)			MIXING MODEL ($\Omega.m$)					CALCULATED ($\Omega.m$)	
	Gy	Anh	Lut	Parallel	Series	Random	HS-	HS+	X	Y
A	95	0	5	168	951	794	365	928	862	844
B	17	0	83	12	178	22	16	129	16	16
C	0	42	58	17	4206	2630	32	1091	214	126
D	0	83	17	59	8302	3090	154	4504	3087	3157
E	29	71	0	2770	7390	5129	4417	6684	5070	6024
F	68	32	0	1404	3880	2089	1947	3230	1622	2265
G	26	51	23	43	5361	1122	105	2105	1102	2474
H	53	34	13	74	3931	1202	185	1708	1129	1940
I	35	6	59	17	956	76	30	408	33	82
J	38	10	52	19	1385	115	36	540	65	210

Sample	Sulphate fraction (%)	Thickness (cm)	Voltage 1 (mV)	Voltage 2 (mV)	Voltage 3 (mV)	Current 1 (μ A)	Current 2 (μ A)	Current 3 (μ A)	Resistivity 1 (Ω .m)	Resistivity 2 (Ω .m)	Resistivity 3 (Ω .m)
G1	0	0.49	12	11	13	90	90	95	5	4	5
G1'	0	0.49	15	23	11	74	96	78	7	9	5
G2	10	0.49	22	14	12	70	64	28	11	8	15
G2'	10	0.49	14	12	23	60	56	73	8	8	11
G3	20	0.50	11	15	14	28	35	37	13	15	13
G3'	20	0.50	15	12	12	42	40	14	12	11	30
G4	30	0.49	16	31	21	28	48	74	20	23	10
G4'	30	0.50	18	14	12	36	24	49	18	21	9
G5	40	0.52	33	30	35	37	37	78	30	28	16
G5'	40	0.50	34	42	45	21	50	38	57	30	40
G6	50	0.51	41	19	36	20	23	39	71	29	32
G6'	50	0.50	43	40	42	12	14	21	126	101	71
G7	60	0.52	26	30	29	10	12	8	88	85	123
G7'	60	0.51	32	41	21	6	9	4	185	158	182
G8	70	0.51	3	2	3	0.120	0.096	0.144	866	722	722
G8'	70	0.50	2	3	4	0.070	0.132	0.139	1009	803	1017
G9	80	0.52	3	3	2	0.092	0.067	0.095	1108	1522	715
G9'	80	0.52	4	3	3	0.126	0.132	0.067	1078	772	1522
G10	90	0.51	3	2	1	0.070	0.050	0.036	1484	1386	962
G10'	90	0.51	2	4	2	0.082	0.088	0.040	845	1575	1732
G11	100	0.52	1	1	1	0.013	0.016	0.012	2613	2124	2832
G11'	100	0.53	2	1	1	0.040	0.022	0.030	1667	1515	1111
A1	0	0.49	16	15	14	97	93	94	6	6	5
A1'	0	0.48	13	17	11	89	92	88	5	7	5
A2	10	0.49	15	18	19	55	60	57	10	11	12
A2'	10	0.50	18	22	12	62	67	67	10	12	6
A3	20	0.50	17	26	18	40	43	37	15	21	17
A3'	20	0.50	20	19	22	42	44	45	17	15	17
A4	30	0.50	18	22	25	33	40	35	20	20	26
A4'	30	0.51	23	24	32	26	28	26	31	30	43
A5	40	0.50	36	23	43	33	24	58	37	13	25
A5'	40	0.50	32	32	56	66	62	71	17	18	28
A6	50	0.52	29	44	44	41	42	50	25	36	30
A6'	50	0.50	35	37	50	32	33	30	39	40	59
A7	60	0.52	43	55	39	2	3	2	731	623	663
A7'	60	0.53	31	43	43	1	1	1	1074	1490	1490
A8	70	0.51	2	1	1	0.035	0.028	0.022	1980	1237	1575
A8'	70	0.52	1	2	2	0.023	0.026	0.033	1537	2718	2142
A9	80	0.53	2	1	2	0.021	0.013	0.021	3236	2614	3236
A9'	80	0.52	2	2	1	0.033	0.037	0.019	2059	1837	1788
A10	90	0.52	1	1	1	0.007	0.009	0.010	4950	3850	3465
A10'	90	0.53	1	1	1	0.009	0.004	0.007	3850	8662	4950
A11	100	0.52	1	1	1	0.004	0.005	0.008	8495	6796	4248
A11'	100	0.52	1	1	1	0.005	0.003	0.004	6668	11113	8335

Figure 01
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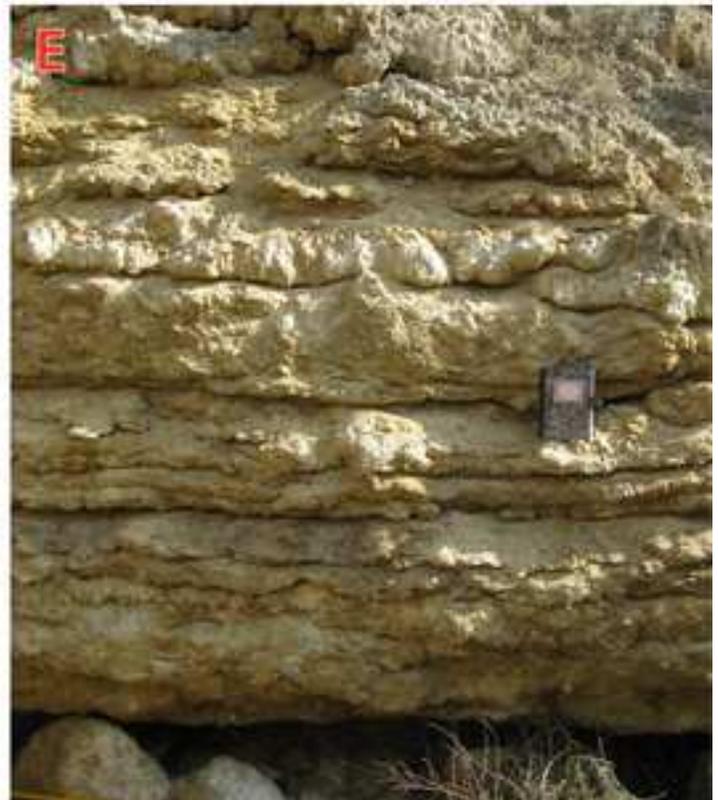
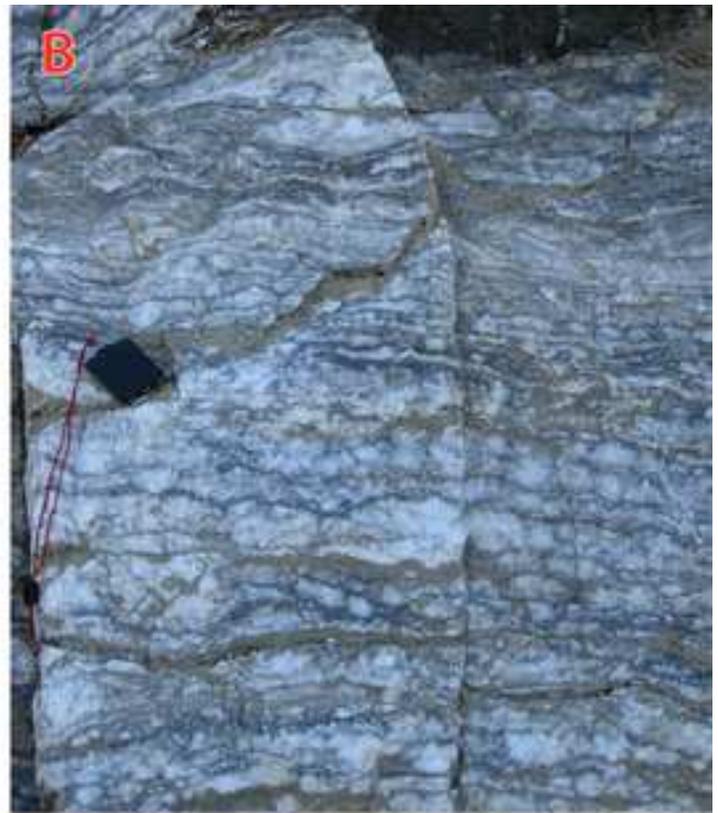


Figure 02
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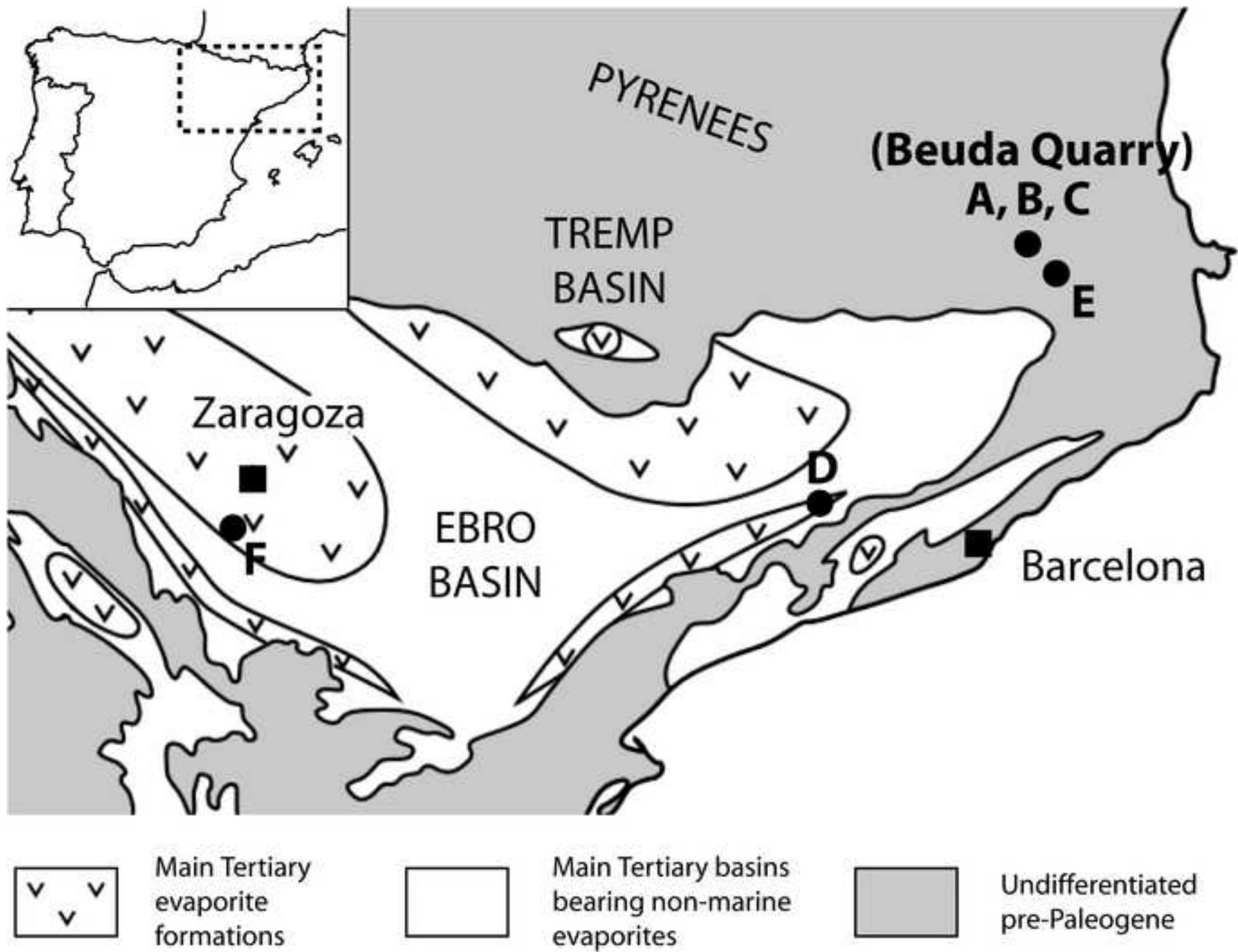
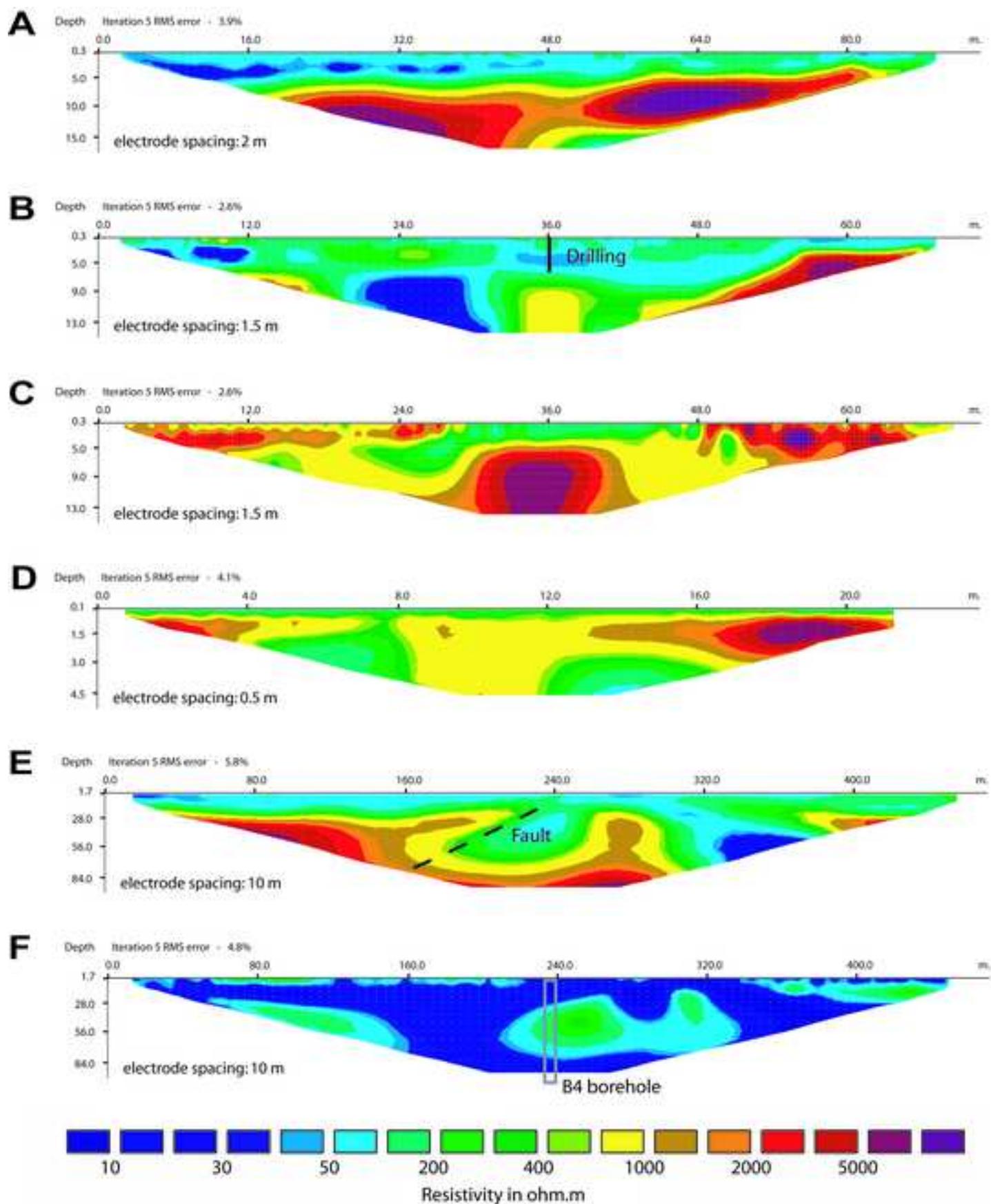
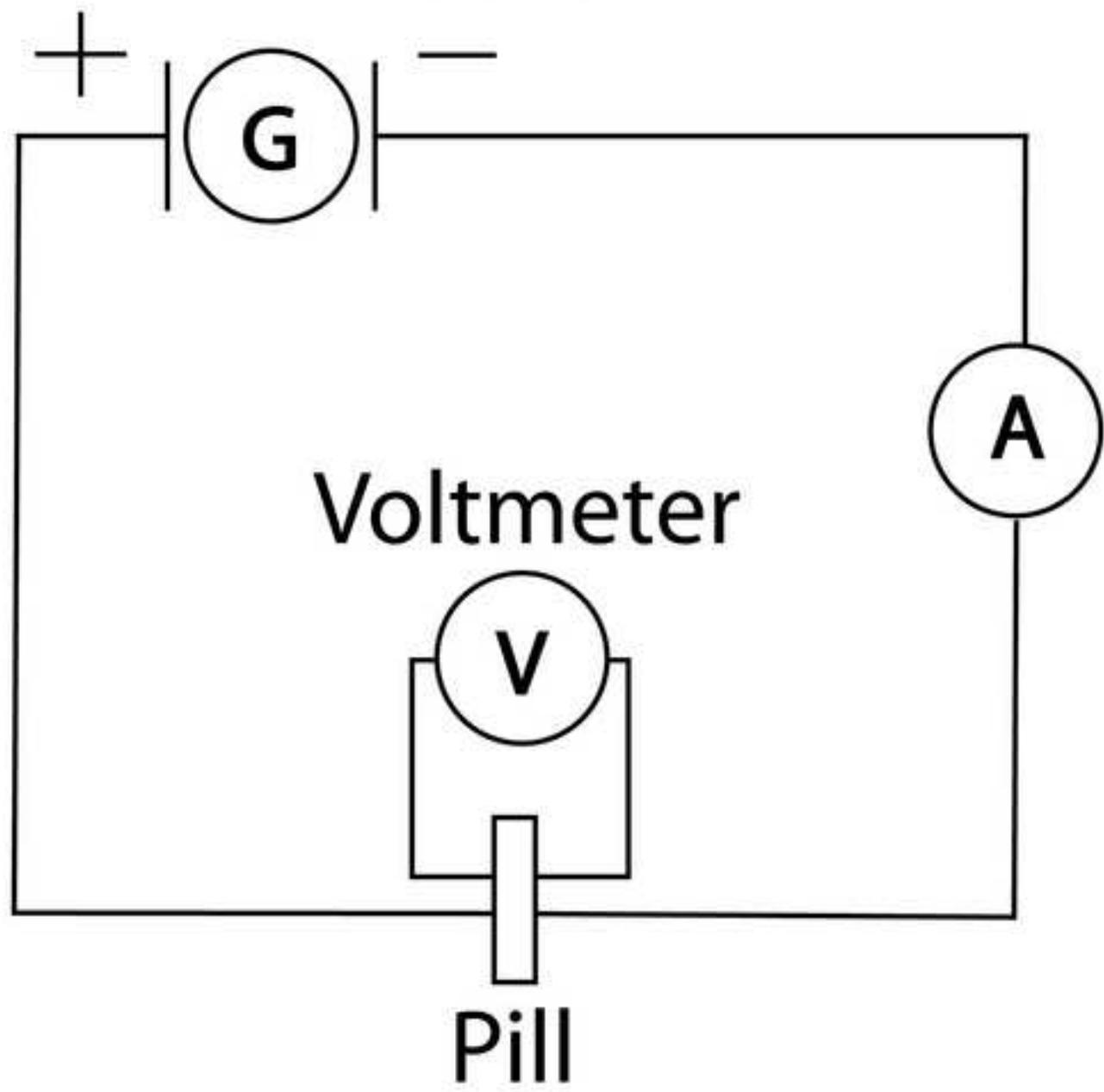


Figure 03
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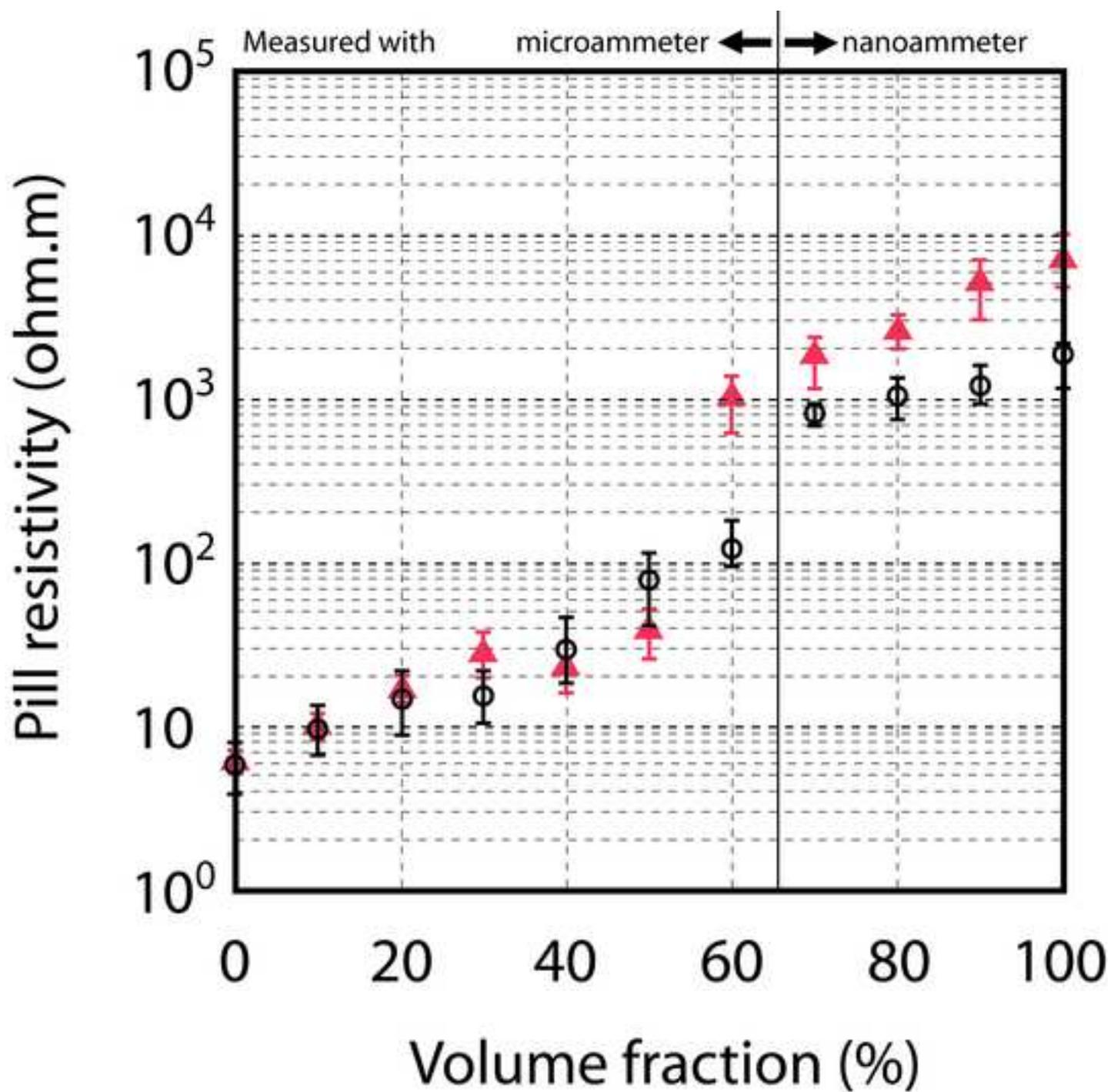
Current Supply



Micro/nano-ammeter

Figure 05

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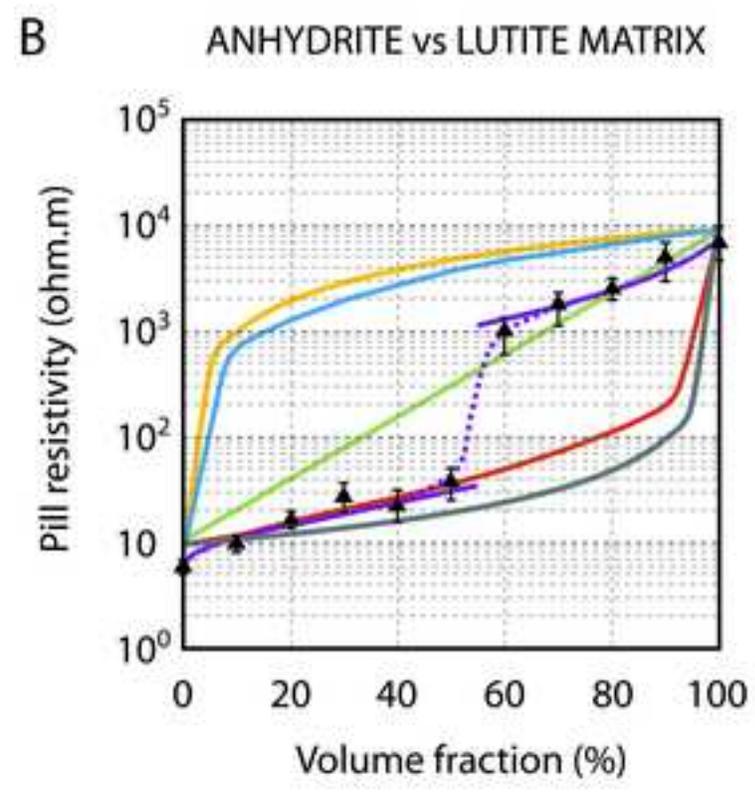
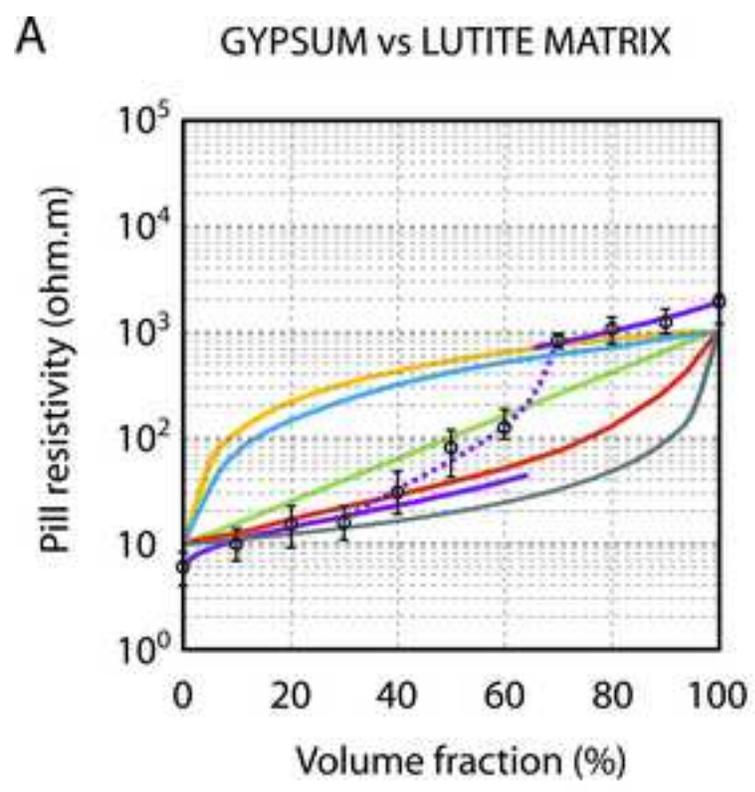


▲ Anhydrite pills

⊕ Gypsum pills

Figure 06

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- ▲ Anhydrite pills ○ Gypsum pills
- HS⁻ — Parallel
- HS⁺ — Serie
- Random — Modified Archie's law

Figure 07

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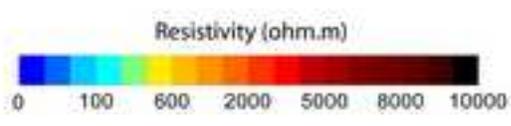
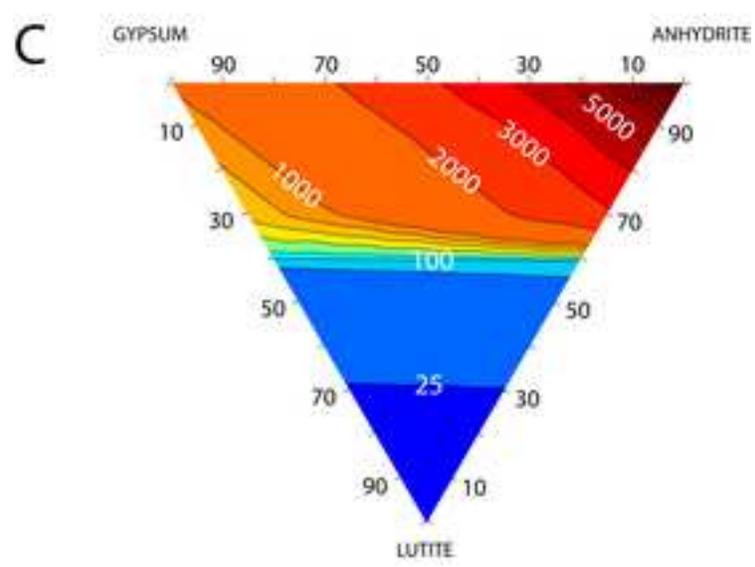
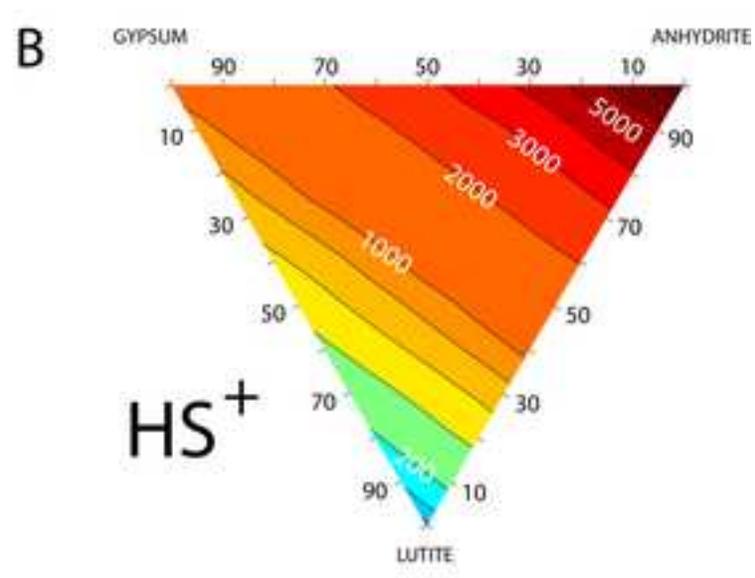
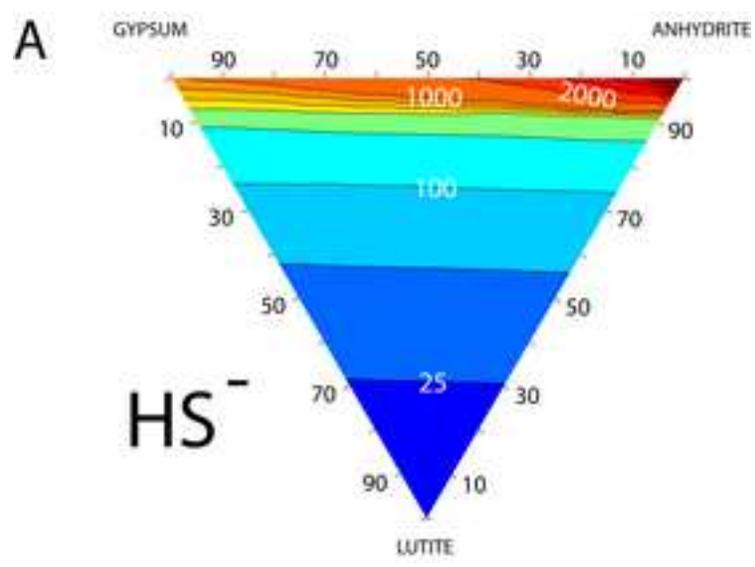
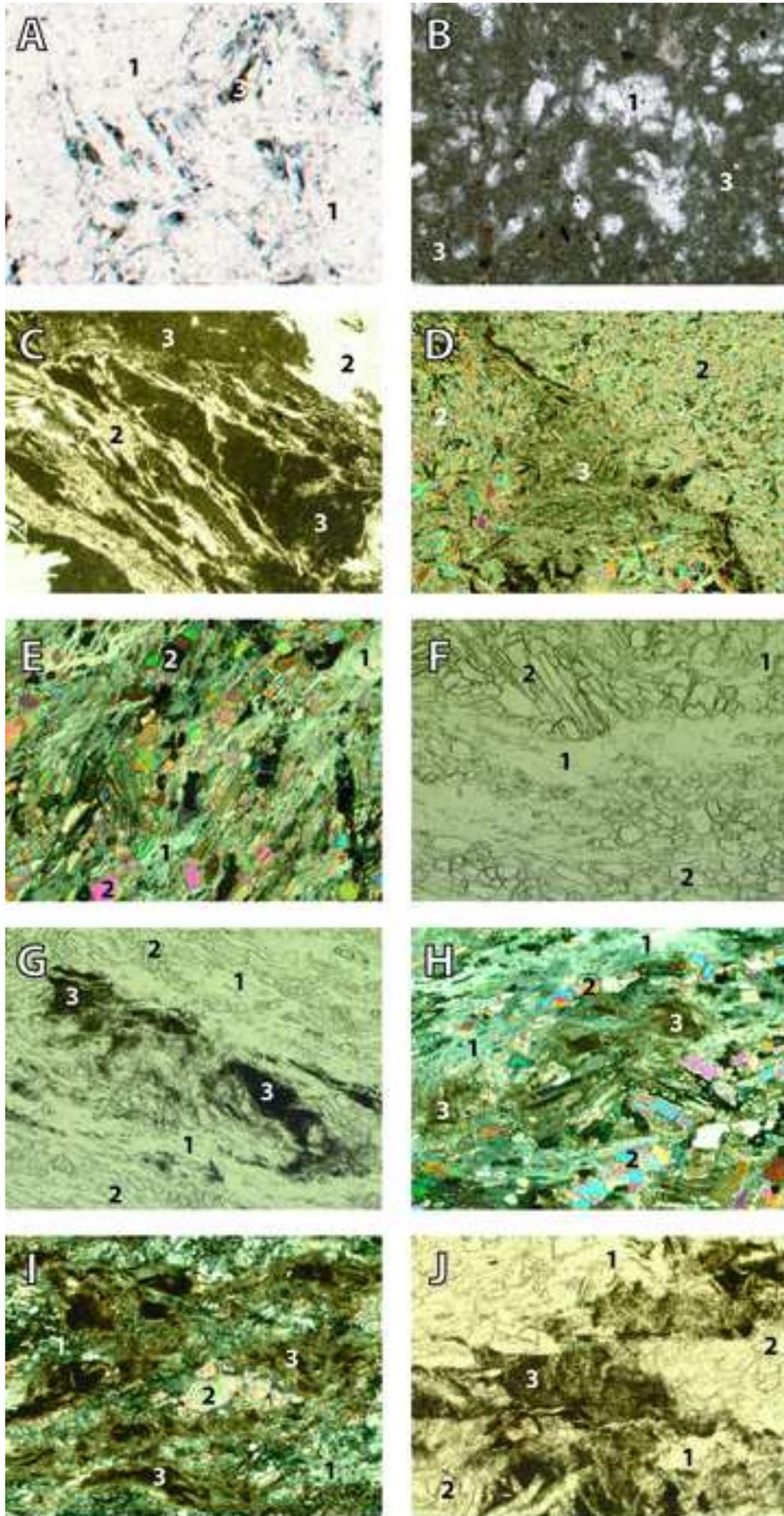


Figure 08

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500 µm

Figure 09
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