Magnetic interactions, weak ferromagnetism, and field-induced transitions in Nd$_2$NiO$_4$

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The magnetic properties of stoichiometric Nd$_2$NiO$_4$ have been investigated by means of dc- and ac-magnetic-susceptibility and isothermal-magnetization measurements. Five different magnetic phase transitions have been identified and characterized. A collinear antiferromagnetic ordering of Ni$^{2+}$ magnetic moments exists between $T_{N1} = 320$ K and $T_{c1} = 130$ K (g$_s$ mode) where an orthorhombic-to-tetragonal ($Bma2$ to P4$_{2}/nmc$) structural phase transition occurs. In this temperature range, the Nd$^{3+}$ ions behave as a paramagnet being polarized by the effect of an internal magnetic field associated with the Ni-Nd antiferromagnetic superexchange interaction. A weak ferromagnetic component appears below 130 K, which is consistent with the $g_s c_s f_s$ and $g_s + c_s f_s$ magnetic modes for Ni$^{2+}$ proposed from a neutron-powder-diffraction experiment. An additional out-of-plane component of the internal magnetic field on the Nd$^{3+}$ ions develops with this structural phase transition and strongly polarizes these ions. Two additional transitions are observed at $T_{c2} = 68$ K (very prominent) and $T_{c3} = 45$ K (very smooth), which are characterized by a sudden increase in the internal magnetic field acting on the Nd ions. This internal magnetic field is evaluated and an antiparallel ordering between the Ni and Nd weak ferromagnetic spin components is inferred. A field-induced transition has been identified. A peak on both the differential susceptibility and the real part of the ac susceptibility at $T_{x1} = 11$ K marks a long-range antiferromagnetic ordering of the Nd$^{3+}$ ions. The out-of-plane component of the Ni$^{2+}$ magnetic moments is attributed to the antisymmetric interaction $D_{3h}$, which turns out to be quite important ($D_{3h}$ $\approx -16.0$ meV) as compared to La$_2$NiO$_4$ and La$_2$CuO$_4$, probably because of a greater tilting angle of the octahedra. Finally, the magnetocrystalline anisotropy associated with Nd ions is found to be high below 20 K.

I. INTRODUCTION

The magnetic behavior of the nickelates of general formula $R_2NiO_4$ ($R = \text{La, Pr, Nd}$) has aroused considerable interest since the discovery of both $p$- and $n$-type high-$T_c$ cuprate superconductors$^1$ mainly because of the fact that the overall magnetic properties of nickelates and cuprates show strong similarities. However, no superconducting state has been clearly found in the nickelates, although some authors have claimed the occurrence of superconductivity in this system.$^2$

From a magnetic point of view, the Cu and Ni sublattices behave in rather similar ways: in both cases a long-range three-dimensional (3D) antiferromagnetic order develops below about 320 K while strong 2D antiferromagnetic fluctuations persist above the Néel temperature.$^3$ The magnetic behavior of the cuprates isomorphous to Nd$_2$CuO$_4$ appears much more complex because of $R$-Cu and $R$-$R$ magnetic interactions which lead, in some cases, to a long-range magnetic ordering of the rare earths that may even coexist with the superconducting state.$^3$ This interesting magnetic behavior is also observed in (Pr,Nd)$_2$NiO$_4$ oxides.$^5$–$^9$ However, concerning the crystal structure, while $R_2NiO_4$-type compounds remain isomorphous to La$_2$CuO$_4$ and both Ni and Cu exhibit an octahedral coordination, Nd$_2$CuO$_4$-type compounds are tetragonal with a square-planar arrangement of the Cu-O atoms. Then, an understanding of the magnetic properties of La$_2$NiO$_4$ might clarify which facts are relevant in the occurrence of high-$T_c$ superconductivity, while a parallel study on (Nd,Pr)$_2$NiO$_4$ might shed some light on the role of the rare-earth–transition-metal ($R$-$TM$) magnetic interactions.

Referring to the crystallographic structure, $R_2NiO_4$ ($R = \text{La, Pr, Nd}$) oxides display some common signatures: above a certain temperature $T_{c2}$ [La$_2$NiO$_4$: $T_{c2} \approx 770$ K,$^{10,11}$ Pr$_2$NiO$_4$: $T_{c2} \approx 1520$ K,$^8$ Nd$_2$NiO$_4$: $T_{c2} \approx 1900$ K (Ref. 6)], the crystal structure is described in the I4/mmm tetragonal space group, which is known as the $T$ structure of the $K_2NiF_4$-type compounds. Around this temperature, a second-order structural phase transition occurs and the crystal symmetry changes to orthorhombic ($Bma2$ space group). This transition is of the same kind as that observed in La$_2$CuO$_4$ at 530 K.$^{12}$ The orthorhombic distortion involves a slight rotation of the NiO$_6$ octahedra, in such a way that the tilting angle smoothly increases upon lowering temperature. Then, on reaching a critical value, the $Bma2$ structure is no longer stable and an orthorhombic-to-tetragonal ($Bma2$ to P4$_2$/nmc)
first-order structural phase transition takes place at $T_{c1}$ in order to rearrange the structure [La$_2$Ni$_4$O$_7$; $T_{c1}\approx80$ K,\cite{10,11,13,14} Pr$_2$Ni$_4$O$_7$; $T_{c1}\approx115$ K,\cite{6,9} Nd$_2$Ni$_4$O$_7$; $T_{c1}\approx130$ K (Refs. 6 and 7)]. This low-temperature structural phase transition is similar to that observed in La$_{2-x}$Ba$_x$CuO$_4$,\cite{15} although it is not detected either in La$_2$CuO$_4$ or in La$_{2-x}$Sr$_x$CuO$_4$.

Likewise, in all three oxides, the Ni sublattice orders antiferromagnetically in the $g_\perp$ magnetic mode as long as the crystallographic structure remains orthorhombic, and they have very similar Néel temperatures [La$_2$Ni$_4$O$_7$; $T_{N1}\approx330$ K,\cite{10,11,14} Pr$_2$Ni$_4$O$_7$; $T_{N1}\approx325$, K,\cite{8} Nd$_2$Ni$_4$O$_7$; $T_{N1}\approx320$ K (Ref. 6), which appear to be very close to that of stoichiometric La$_2$CuO$_4$ ($T_{N1}\approx320$ K).\cite{11,16} Below $T_{c1}$, the situation is more complex: the low-temperature tetragonal symmetry allows the existence of a weak ferromagnetic component along the c axis (out-of-plane axis). The magnetic structure may now be described either in the $g_\parallel$ or $g_\perp$ modes for both La$_2$Ni$_4$O$_7$ and Nd$_2$Ni$_4$O$_7$, while in Pr$_2$Ni$_4$O$_7$ there is a progressive spin reorientation from the $g_\parallel$ mode to the $g_\perp$ mode as temperature falls, in such a way that at 1.5 K the latter represents the total of the magnetic order of Ni$^{3+}$ ions. Finally, at some temperature below $T_{c1}$, Nd$^{3+}$ and Pr$^{3+}$ ions are strongly polarized, as evidenced by neutron powder diffraction,\cite{6,8} and this progressive ordering of the rare-earth sublattice occurs in the same magnetic mode as that of Ni. However, while Nd$^{3+}$ ions present a long-range antiferromagnetic ordering at $T_{N2}\approx11$ K, similarly to Nd$_2$CuO$_4$,\cite{17} the Pr$^{3+}$ sublattice does not achieve any long-range ordering above 1.5 K. Furthermore, some other magnetic anomalies are detected in Nd$_2$Ni$_4$O$_7$ and Pr$_2$Ni$_4$O$_7$ at some intermediate temperatures, signaling the existence of spin reorientations probably related to those observed in Nd$_2$CuO$_4$.\cite{18}

Finally, it is worth stressing that neutron-powder-diffraction (NPD) results show\cite{6,8,10,11} that (i) in La$_2$Ni$_4$O$_7$, the magnetic moment for Ni is about 1.68$\mu_B$ at 1.5 K (smaller than the spin-only value due to zero-point quantum fluctuations), while the ferromagnetic component along the c axis is too small to be detected; (ii) in Nd$_2$Ni$_4$O$_7$, the magnetic moments for Ni and Nd are, respectively, about 1.59$\mu_B$ and 3.2$\mu_B$ at 1.5 K (this last one in close agreement with the expected value from the $^4I_{9/2}$ ground state), and they subtend angles of 14.6° and 18.2° with the basal plane, respectively; (iii) in Pr$_2$Ni$_4$O$_7$, the magnetic moments for Ni and Pr are, respectively, about 1.56$\mu_B$ and 1.28$\mu_B$ at 1.5 K (this last one is much smaller than the expected value from the $^3H_4$ ground state due to the fact that this sublattice is only partially ordered), and they stand at angles of 19.3° and 42.2° with the basal plane, respectively.

In a previous study\cite{7} some of us reported preliminary macroscopic magnetization measurements on stoichiometric Nd$_2$Ni$_4$O$_7$ identifying up to five different magnetic phase transitions, related either to cooperative long-range magnetic orderings (Ni and Nd ions) or to spin reorientations associated with the orthorhombic-tetragonal structural phase transition or with other unexplained mechanisms. We report here experimental data that strongly support our first analysis, both in the ferromagneticlike character of the magnetic properties of this oxide and in the evaluation of the internal magnetic field acting on the Nd ions below ($T<T_{c1}$) and above ($T>T_{c1}$) the weak ferromagnetic regime. We have identified a metamagneticlike field-induced transition having a very different character from that observed in La$_2$CuO$_4$,\cite{19,20} which allows us to determine the superexchange isotropic coupling constant among the Ni and Nd sublattices. Finally, we discuss the appearance of the weak ferromagnetism in terms of the antisymmetric Ni-Ni superexchange interaction $D_{Ni-Ni}$ and the magneto-crystalline anisotropy associated with Nd ions.

II. EXPERIMENTAL

Stoichiometric Nd$_2$Ni$_4$O$_7$ polycrystalline samples were obtained by the reduction of the oxidized precursor at 350°C under a dry hydrogen atmosphere and careful monitoring of the reduction process by thermogravimetry. The oxidized precursor sample was prepared by the ceramic method from stoichiometric amounts of Nd$_2$O$_3$ and NiO, which were intimately homogenized and fired at temperatures up to 1450°C in air and several intermediate grindings with an accumulated firing time of about 300 hours.\cite{7,11,21} This long annealing was performed in order to yield very good crystallinity. This is an important point in this system because after the low-temperature structural phase transition very severe strains appear in the crystallites and these seem to be enhanced by the preexisting defects. The yield of the chemical reaction was followed by both x-ray and neutron diffraction and no impurity was observed within the detection limit of these techniques. Neutron powder diffraction showed much narrower Bragg lines than those previously observed.\cite{6} No Ni$^{3+}$ ions could be detected by iodometric titration.

Low-field dc and ac magnetic susceptibilities were measured by means of a Faraday balance (temperature range 14–300 K) and an ac susceptometer (temperature range 4–300 K), respectively. Isothermal magnetization measurements were performed both with a Quantum Design SQUID magnetometer (up to 5 T) and with the axial extraction technique (up to 20 T) of the Service National des Champs Intenses at Grenoble. These magnetic measurements showed that a tiny amount of metallic Ni existed in our sample, which was probably formed during the hydrogen reduction step. We evaluate the amount of metallic Ni in our sample to be smaller than 0.1% in weight.

III. RESULTS

A. ac and dc magnetic susceptibility

The temperature dependence of the low-field dc magnetic susceptibility was first studied in order to identify the different transitions observed in the neutron diffraction patterns. [Fig. 1(a)]. A clear susceptibility upturn becomes prominent at $T_{c1}=130$ K. This temperature corresponds exactly to that at which the
orthorhombic-tetragonal phase transition occurs and thus implies that the change of the NiO$_6$ octahedra tilting axis associated with this structural phase transition also brings about a reorientation of the Ni magnetic moments. We will further discuss this first transition in the light of the magnetic field dependence of the magnetization and of the magnetic structure determined by neutron powder diffraction.

Above $T_{c1}$ and up to room temperature, the dc magnetic susceptibility displays a typical Curie-Weiss behavior [Fig. 1(b)]. In this temperature range, the magnetic moments of the Ni$^{2+}$ ions are ordered ($T_{N1}=320$ K) and their contribution to the magnetic susceptibility and basically temperature-independent, while the Nd$^{3+}$ ions should behave like a paramagnet being polarized by the effect of temperature.

Previous experimental data on Nd$_3$CuO$_4$ reported by Saez-Puche et al.\textsuperscript{22} and Seaman et al.,\textsuperscript{17} and more recently by Oseroff et al.,\textsuperscript{23} show that no crystal-field effect is observed on Nd$^{3+}$ ions above around 30 K and the magnetic moment derived from the inverse of the magnetic susceptibility corresponds exactly to that of Nd$^{3+}$ ions [$\mu$(Nd$^{3+}$) = 3.62$\mu_B$, ground state \( ^{7}S_{2/2} \)]. In this sense, we expected to find the same result in Nd$_3$NiO$_4$. Nevertheless, when fitting the Curie-Weiss law to our experimental data, we obtain a magnetic moment which is roughly double. Later on, we will discuss this fact in the light of the internal magnetic field acting on Nd$^{3+}$ ions as a result of the long-range magnetic ordering of the Ni sublattice.

On lowering temperature below $T_{c1}$, the dc magnetic susceptibility deviates from the linear law, signaling the appearance of the weak ferromagnetic component. As can be seen in Fig. 1(a), at about $T \approx 80$ K, a strong low-temperature polarization occurs which needs a thorough analysis. Two further transitions at $T_{c3} \approx 68$ K and $T_{c5} \approx 45$ K are observed in Fig. 1(a) which match the anomalies observed in the intensity of some magnetic Bragg reflections.\textsuperscript{6} These anomalies are superimposed on the strong low-temperature magnetic polarization of the Nd$^{3+}$ ions.

The real part of the ac magnetic susceptibility $\chi'$ is represented in Fig. 2(a). Two prominent peaks and a smooth change of the curvature are well established; the first peak appears at $T_{N2} \approx 11$ K and may be related to the long-range order of the Nd ions. The second anomaly is found at $T_{c2} \approx 68$ K and it is more of an abrupt discontinuity rather than a peak. Finally, a smooth change of the curvature is seen around $T_{c3} \approx 45$ K, while no special effect is observed on crossing the orthorhombic-to-tetragonal structural phase transition at $T_{c1}$. All these findings have been clearly confirmed by both NPD and dc magnetic susceptibility. It is also worth pointing out that the inverse of the real part of the ac susceptibility also displays a Curie-Weiss behavior above $T_{c1}$, as indicated by the dc measurements [Fig. 2(a), inset].

The imaginary part of the ac magnetic susceptibility $\chi''$ is displayed in Fig. 2(b), and it clearly shows a discontinuity at $T_{c2}$, signaling that some kind of first-order transition occurs at this temperature. In our opinion, this transition should have something to do with the competition between magnetocrystalline anisotropy and magnetic exchange: the faster temperature dependence of the former might account for a spin reorientation occurring on lowering the temperature below $T_{c2}$. Finally, a broad absorption peak is observed at low temperature around 25 K, while no special effect is detected at $T_{c3} \approx 45$ K. We believe that this latter transition might also be due to some kind of spin reorientation.

We have also studied the imaginary part of the ac susceptibility $\chi''$ as a function of both frequency and intensity of the applied ac magnetic field. Concerning the absorption peak at 25 K, the out-of-phase component of the susceptibility indicates some kind of relaxation process.

**FIG. 1.** (a) Low-field dc magnetic susceptibility ($H_{dc}=1.56$ kOe) of stoichiometric Nd$_3$NiO$_4$ in the temperature range 14–300 K. Inset: detail of the curve showing the structural phase transition at $T_{c1}=130$ K. (b) Inverse of the dc magnetic susceptibility ($H_{dc}=1.56$ kOe) in the temperature range 80–300 K.
For example, in paramagnets, the study of both $\chi'$ and $\chi''$ as a function of frequency allows one to determine the time constants of the relaxation processes involved, thus leading to a standard way of dealing with this kind of phenomena. In magnetically ordered systems, this technique is a direct method to analyze domain-wall relaxation with typical time constants of the order of $10^{-3}$ s, which dominates in the low-temperature regime. In our case, the broad peak appearing at 25 K disappears for values of the external ac magnetic field lower than 0.1 Oe, which is consistent with the fact that the motion of a domain wall requires some minimum energy. The fact that the absorption peak is above $T_{N_2}$ ≈ 11 K gives further confidence to the idea that it is basically related to a domain-wall relaxation process.

We have tried to determine the characteristic time constant for this process by measuring $\chi''$ at different frequencies (from 10 Hz to 1000 Hz), but even at the maximum frequency accessible for our equipment (Lake-Shore Susceptometer) we were not able to reach the maximum of the Argand diagram at 25 K. We were only able to assert that the relaxation time $\tau = 1/2\pi\nu^*$ is less than $10^{-4}$ s, where $\nu^*$ is the frequency at which the ratio $\chi''/\chi'$ at a fixed temperature reaches its maximum. This value is smaller than the typical $10^{-3}$ s (Ref. 26) characteristic of the domain relaxation process, but it is still very far from other kinds of relaxation mechanisms, such as spin-spin (10$^{-1}$ s) and spin-lattice (10$^{-6}$ s) relaxation.

In order to explain this fact, we should bear in mind that we are dealing with a material of strong anisotropy, as we will point out when the magnetic field is inverted (see Fig. 4). This is a characteristic feature of ferromagnets with narrow domain walls that easily become pinned by structural defects. In this sense, the narrower the domain walls, the higher the energy associated with them, which leads to the decrease in the relaxation time, so we find smaller values of $\tau$ than those typically associated with domain wall relaxation mechanisms.

**B. Isothermal magnetization curves $M(H)$**

A much deeper insight into the microscopic mechanisms of the complex magnetic behavior of Nd$_2$NiO$_4$ may be gained from the isothermal magnetization curves. In Fig. 3 we show some results, as a function of tem-

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**FIG. 2.** (a) Real part of the ac magnetic susceptibility ($H_{ac} = 5$ Oe) at $\nu = 111.1$ Hz in the temperature range 4.2–300 K. Inset: inverse of the curve in the temperature range 80–300 K. (b) Imaginary part of the ac magnetic susceptibility ($H_{ac} = 5$ Oe) at $\nu = 111.1$ Hz in the temperature range 4.2–300 K.

**FIG. 3.** Isothermal magnetization curves $M(H)$ (maximum applied field $H_{max} = 1$ T), as a function of temperature in the temperature range (a) 4.2–70 K and (b) 70–300 K.
perature, obtained on decreasing the magnetic field from $H = 1$ T, while in Fig. 4 a full hysteresis loop is displayed with a maximum magnetic field of $H = 5$ T. From these curves, the typical ferromagnetic-like appearance of the magnetic properties of this oxide is very clear.

It should first be noted that the observed magnetization values are strongly dependent on the maximum previously applied field. This is an indication of ferromagnetic domains which cannot be completely reversed even with the application of magnetic fields up to 5 T, thus implying that the magnetic anisotropy of Nd$_2$NiO$_4$ should be high. This is further corroborated by the observation of anomalous drops in the hysteresis loop when the magnetic field is inverted (Fig. 4), which is also a typical feature of ferromagnets with narrow domain walls (strong anisotropy) which easily become pinned by structural defects.

The unusually high coercive field observed is also remarkable ($H_c = 1.1$ T at $T = 4.2$ K), which is consistent with a large magnetic anisotropy at low temperature. This is clearly singular as compared to (La,Nd,Gd)$_2$CuO$_4$ and La$_2$NiO$_4$ oxides which have either null or very small coercive fields. Furthermore, the coercive field of Nd$_2$NiO$_4$ is highly temperature dependent (for instance, $H_c = 1200$ Oe at $T = 70$ K), thus signaling that the magnetic anisotropy rapidly decreases with temperature, and becomes practically zero when $T > T_c$, which reinforces the idea of the development of the ferromagnetic component below this temperature (Fig. 5).

It should also be mentioned that these isothermal magnetization curves do not display, up to maximum applied field of 5 T, any magnetically induced phase transition, in contrast to La$_2$CuO$_4$. In the latter, this field-induced transition was caused by a metamagnetic-like transition of the weak ferromagnetic component which orders antiferromagnetically ($g_x g_y$ representation). The nonobservance of this sudden transition in Nd$_2$NiO$_4$, but a progressive domain-wall inversion of the ferromagnetic components, is consistent with the magnetic representations obtained by the neutron diffraction study of Nd$_2$NiO$_4$ (Ref. 6) ($g_x g_y$ or $g_x + g_y$ representations below $T_c = 130$ K). These magnetic modes indicate the existence of a ferromagnetic component along the c axis, instead of the antiferromagnetic one observed in La$_2$CuO$_4$.

In Fig. 6, we represent the $M(H)$ curve at $T = 4.2$ K, measured on decreasing the magnetic field from $H_{\text{max}} = 20$ T. In Fig. 7 we display the magnetization values at different fields ($H = 0, 1,$ and $5$ T), as a function of the maximum previously applied magnetic field (up to $20$ T). These new data are of the greatest importance in order to clarify our basic experimental framework: Fig. 6 clearly shows that some kind of field-induced transition occurs. This transition is smooth (it takes place in the field range 3.5–6 T), since our sample is polycrystalline.

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**FIG. 4.** Hysteresis curve at 4.2 K ($H_{\text{max}} = 5$ T).

**FIG. 5.** Coercive field $H_c$ as a function of temperature ($H_{\text{max}} = 5$ T).

**FIG. 6.** (a) Isothermal magnetization curves at 4.2 K, with a maximum applied field of $H_{\text{max}} = 20$ T. Inset: derivative of the magnetization with respect to the applied field, as a function of the magnetic field, showing the critical field $H_{cr} = 5.2(2)$ T.
FIG. 7. Magnetization as a function of the maximum applied field \( T = 4.2 \) K, for different magnetic fields: (1) \( H = 0 \) (remanence), (2) \( H = 1 \) T, and (3) \( H = 5 \) T.

Figure 7 evidences that the magnetic domains only disappear above \( H \approx 8 \) T.

We have evaluated the critical field \( H_{cr} \) at which the jump occurs from the inflection point of the curve (inset of Fig. 6) and we find that \( H_{cr} = 5.2(2) \) T at \( T = 4.2 \) K, which is neither dependent on the maximum previously applied field nor very far from that reported in La$_2$CuO$_4$ (Ref. 26) \( H_{cr} = 5.3(3) T \) when \( T = 0 \). The value of \( H_{cr} \) derived in this way indicates that the effects of the domain wall inversion are also superimposed in the field region where the magnetization jump takes place.

Then, this full analysis of the experimental characteristics of the \( M(H) \) curves reveals that in stoichiometric Nd$_3$NiO$_4$ a magnetic domain structure (which is not present in La$_2$CuO$_4$) coexists with a metamagnetic-like field-induced transition. Later on in this work we will explain the reasons for the occurrence of these effects at the same time.

When looking to the overall character of the \( M(H) \) curves (Fig. 3) below the critical field, it is easy to conclude that they may be represented in a wide temperature range by the equation

\[
M(H, T) = M_0(T) + \chi_d H_d,
\]

where \( \chi_d \) is a high-field differential susceptibility, \( H_d \) is the applied magnetic field, and \( M_0(T) \) is the magnetization extrapolated at zero magnetic field from the linear high-field regime. This \( M_0(T) \) is strongly temperature dependent and it is very near to the remanence because of the nearly linear character of the isothermal magnetization curves. The temperature dependence of the differential susceptibility \( \chi_d \) and the zero-field extrapolated magnetization \( M_0(T) \) are displayed in Figs. 8 and 9, respectively.

We note first that the ferromagnetic component develops at \( T_c = 130 \) K (both \( M_0 \) and \( \chi_d \) exhibit a jump at this temperature), i.e., at the structural phase transition. The first-order character of this phase transition may be evidenced by the existence of some magnetization hysteresis when cycling the temperature. Only a very small magnetic hysteresis remained above \( T_c \), which we attribute to a tiny amount of metallic Ni formed during the high-temperature hydrogen reduction step. The residual saturation magnetization of 0.05 emu/g at 300 K that we have found in the magnetization measurements lead us to evaluate the amount of metallic Ni in our sample to be smaller than 0.1% in weight. In any case, there is no doubt about the increase of the weak ferromagnetic component at \( T_c \), thus giving full support to the group-theoretical arguments which show that no weak ferromagnetic component is possible within the space group \( Bmab \) in connection with the g mode.\(^6\)

We should also take into account that this weak ferromagnetic component of the Ni magnetic moments lies at the origin of the magnetic anomaly observed in stoichiometric La$_2$NiO$_4$,\(^{13}\) where the structural phase

FIG. 8. (a) High-field differential susceptibility \( \chi_d \) as a function of temperature. Inset: detail of the curve in the temperature range 4.2–50 K. (b) Detail of the inverse of the high-field differential susceptibility in the temperature range 20–80 K.
transition occurs at 80 K. This is also the temperature at which it was claimed that minor phase high-temperature superconductivity develops in La$_2$NiO$_4$ and so we would like to stress that extreme care should be taken when observing magnetic anomalies around this temperature.

The existence of further spin reorientations at $T_{c2}\approx 68$ K and $T_{c3}\approx 45$ K may be clearly stated from the anomalies observed in either the high-field magnetic susceptibility or the saturation magnetization (Figs. 1,2,8,9). The observation of these anomalies in the region where the Nd ions are becoming progressively polarized by an internal magnetic field points to the existence of sudden increases in the c-axis component of this field.

It is not possible from our present macroscopic measurements on polycrystalline samples to undertake a complete analysis of these spin-reorientation transitions. It is very likely, however, that these anomalies involve some kind of spin reorientations, similar to those observed in Nd$_3$CuO$_4$ and there is probably competition between magnetocrystalline anisotropy and magnetic exchange effects.

Finally, a sharp peak at $T_{N_2}\approx 11$ K is clearly observed in the the $\chi_c(T)$ curve [Fig. 8(a)], which is also evidenced by the ac magnetic susceptibility [Fig. 2(a)], signaling a long-range magnetic ordering of the Nd ions. It is straightforward to note that this transition is hardly seen in the $M_0(T)$ curve, thus implying that the c-axis component of the internal magnetic field acting on the Nd ions is not modified by the long-range order of these ions. This observation is in sharp contrast with the behavior of $T_{c1}$ cuprates such as Gd$_3$CuO$_4$ where the internal magnetic field falls to zero when the Gd ions order magnetically. It is also important to note that the long-range order transition identified here occurs at much higher temperatures than those observed in Nd$_3$CuO$_4$ ($T_N = 1.5$ K), even if in both cases a strong polarization of Nd ions magnetic moments is induced by the Ni or Cu sublattice.

IV. DISCUSSION

A. $T_{N_1} > T > T_{c1}$

In this temperature range, the crystal symmetry ($Bmab$ orthorhombic space group) in connection with the $g$-mode does not allow the existence of a ferromagnetic component of the Ni$^{2+}$ magnetic moments along the c axis; thus they are restricted to the a-b plane. Then, the in-plane ordered Ni$^{2+}$ magnetic moments will cause a net in-plane staggered exchange internal field $H_{\text{i-a-b}}$ acting on the Nd ions. Nevertheless, since $H_{\text{i-a-b}}$ is antiferromagnetically staggered (due to the AF ordering of the Ni sublattice) no net magnetization in the Nd sublattice should be observed and Nd ions should follow a paramagnetic-like behavior, which is proved by the Curie-Weiss-like law evidenced by both dc and ac magnetic susceptibility above $T_{c1}$.

However, the external applied field $H_0$ will induce a net magnetization of Ni$^{2+}$ ions (which is not staggered but aligned along the magnetic field axis), which, at the same time, will polarize Nd$^{3+}$ ions through an internal magnetic field $H_i$. What makes this argument appealing is the fact that the Nd ions are now being polarized by the effect both of the external applied field $H_0$ and the internal induced magnetic field $H_i$. This means that the magnetic susceptibility may be expressed (assuming that above $T_{c1}$ no crystal-field effects are expected on Nd$^{3+}$ ions) as

$$\chi = C^* / T - \theta + \chi_0,$$  \hspace{1cm} (2)

where $\chi_0$ accounts for the temperature-independent contributions to the susceptibility, such as, for example, the core diamagnetism and the contribution arising from the antiferromagnetically ordered Ni sublattice (we assume this latter because the magnetic susceptibility of stoichiometric La$_2$NiO$_4$ is basically temperature-independent above 150 K [Ref. 13]).

As we can see, the effective Curie constant $C^* = C_{\text{Nd}}(1 + H_i/H_0)$ is greater than the expected $C_{\text{nd}}$ (= 1.64 emu K/mol) by a factor $H_i/H_0$. For example, we have found experimentally by means of dc susceptibility [Fig. 1(b)] that $C^* = 6.0(2)$ emu K/mol when $H_0 = 1.56$ kOe (which is of course much greater than the
expected value for Nd\(^{3+}\) ions). This means that the induced internal magnetic field acting on Nd ions is about \(H_i \approx 4.1(3)\) kOe.

Further support to our argument can be achieved as follows: in the scope of the mean-field approximation and assuming the Nd-Ni superexchange \(J_{\text{Nd-Ni}}\) interaction to be isotropic, the induced internal magnetic field \(H_i\) acting on Nd ions and arising from the field induced magnetization of Ni ions may be written

\[
H_i = (2ZJ_{\text{Nd-Ni}}/\mathcal{N}_{\text{Nd}}g_{\text{Nd}}N_{\text{H}})M_{\text{Ni}},
\]

(3)

where \(Z\) is the number of nearest neighbors, \(g_{\text{Nd}} = \frac{8}{3}\), and \(M_{\text{Ni}}\) stands for the Ni sublattice magnetization. Expressing \(M_{\text{Ni}} = \chi_{\text{Ni}}N_{\text{H}}\), Eq. (3) becomes

\[
H_i = AM_{\text{Ni}} = A\chi_{\text{Ni}}H_a,
\]

(4)

where \(A\) represents the molecular field constant characteristic of the mean-field approximation, thus suggesting that the effective Curie constant \(C^*\) should be temperature independent \([C^* = C_{\text{Nd}}(1 + A\chi_{\text{Ni}})]\). From our experimental data \([H_i \approx 4.1(3)\) kOe and \(H_a = 1.56\) kOe], and assuming that the Ni sublattice magnetic susceptibility \(\chi_{\text{Ni}}\) should be of the same order of magnitude as the value we have obtained for stoichiometric La\(_2\)NiO\(_4\) (Ref. 13) \([\chi(300 K) \approx 1.6 \times 10^{-6}\) emu/g, \(\chi(150 K) \approx 1.5 \times 10^{-6}\) emu/g], we derive that \(J_{\text{Nd-Ni}} \approx 0.75(1)\) meV, which is in close agreement with the value we determine in the next section of this paper, where we derive that the Nd and Ni magnetic moments are antiparallel and \(J_{\text{Nd-Ni}} \approx -0.6(2)\) meV.

**B. \(T_{c1} > T > T_{N2}\)**

Below \(T_{c1}\), the new crystal symmetry (\(P4_2/nmc\) tetragonal space group) allows the appearance of a weak ferromagnetic component of Ni\(^{2+}\) magnetic moments along the \(c\) axis, which develops an out-of-plane component of the internal field that further polarizes the Nd\(^{3+}\) ions and this is on the basis of the strong contribution of these ions to the magnetic susceptibility, mainly below 80 K [Figs. 1(a) and 2(a)]. The total internal field acting on Nd ions will basically be a consequence of the Nd-Ni exchange interaction and may be expressed as

\[
H_i = H_i^0 + A\chi_{\text{Nd}}H_a,
\]

(5)

where \(A\chi_{\text{Nd}}H_a\) stands for the internal magnetic field arising from the field-induced magnetization of Ni ions [see Eq. (4)]. This contribution tends to zero with the applied field, while the term \(H_i^0\) accounts for the internal field induced by the weak ferromagnetic component of the Ni\(^{2+}\) magnetic moments, which is not field dependent.

Then, if we assume the Nd-Ni superexchange coupling to be isotropic, \(H_i^0\) may be written, in the scope of the mean-field approximation,

\[
H_i^0 = 2ZJ_{\text{Nd-Ni}}\langle S_{\text{Nd}}\rangle^2g_{\text{Nd}}H_B,
\]

(6)

thus meaning that the weak ferromagnetic component of the Ni\(^{2+}\) magnetic moments \(\langle S_{\text{Nd}}\rangle^2\) originates an out-of-plane component of the internal magnetic field \(H_i^0\). Then, we assume that the \(c\) component of the internal field is on the origin of the strong polarization of Nd\(^{3+}\), giving way to the strong increase in the saturation magnetization \(M_0\) mainly below 80 K (Fig. 9). It is evident that this increase of the ferromagnetic component could also be related to the magnetic anisotropy, though in the next section we show that this latter contribution is not relevant above 20 K.

Let us now undertake the evaluation of the internal field acting on Nd ions and the origin of the field-induced transition:

1. **Evaluation of internal field acting on Nd ions**

Within the weak ferromagnetic regime \((T < T_{c1})\), a nonmonotonic magnetic behavior is observed with three more transitions at \(T_{c1} \approx 68\) K, \(T_{c2} \approx 45\) K and \(T_{N2} \approx 11\) K (Figs. 1, 2, 8, and 9). If we concentrate on the \(T_{c2} > T > T_{N2}\) temperature range, we may associate the two intermediate transitions \(T_{c2}\) and \(T_{c3}\) to some kind of spins reorientations coming from competition among magnetocrystalline anisotropy and magnetic exchange, leading to an increase in the saturation magnetization (Fig. 9).

If we now examine the magnetic behavior below \(T_{c2}\), we see that the high-field magnetic susceptibility \(\chi_d\) follows a Curie-Weiss law in two definite temperature ranges; from \(T_{c2}\) to \(T_{c3}\) and from \(T_{c3}\) down to \(T \approx 20\) K [Fig. 8(b)]. This fact suggest that, although the internal magnetic field acting on the Nd ions remains constant in each temperature interval, there exists some discontinuity on crossing \(T_{c3}\).

On the other hand, our experimental data suggest that the 3D long-range magnetic ordering for Nd ions takes place around \(T_{N3} \approx 11\) K. Therefore, we may consider that below \(T_{c2}\) \((T < 68\) K), and down to \(T \approx 20\) K (temperature range where Nd ions are strongly polarized in the internal magnetic field created by the Ni ions), the Nd-Nd interaction is not relevant in comparison with the dominant Nd-Ni one, which bring us to a simple evaluation of the \(c\) axis component of the exchange internal field \(H_i^0\).

Let us first assume that both the Ni\(^{2+}\) ferromagnetic component \(M_{\text{Ni}}^0\) and \(H_i^0\) are temperature independent in each interval 20 K–\(T_{c3}\) and \(T_{c3}–T_{c2}\). We also assume that the high-field magnetic susceptibility is basically related to the contribution of the Nd ions. For instance, in stoichiometric La\(_2\)NiO\(_4\), \(\chi_d(T = 4.2\) K\) = 3 and \(\chi_d(T_{c1} = 75\) K\) = 1.4 (all values are given in \(10^{-6}\) emu/g), while in stoichiometric Nd\(_2\)NiO\(_4\), \(\chi_d(T = 4.2\) K\) = 118 and \(\chi_d(T_{c1} = 130\) K\) = 50. Taking into account all these hypotheses and Eq. (5), Eq. (1) may be written

\[
M(H_a, T) = M_{\text{Ni}}^0 + \chi_d(H_i^0 + A\chi_{\text{Nd}}H_a + H_a),
\]

(7)

where only \(\chi_d\) has an explicit dependence on temperature and we have ignored the anisotropy field \(H_a\) associated with the Nd ions (see Sec. V). Consequently, the zero-field extrapolation of Eq. (7) leads us to a new equation:
\[ M_0(T) = M_{\text{Ni}}^0 + \chi_d H_i^0. \]  

\( M_0(T) \) vs \( \chi_d(T) \) is displayed in Fig. 10, which clearly shows four different magnetic behaviors as a function of temperature:

(a) The observed linearity between \( M_0(T) \) and \( \chi_d(T) \) in the temperature range 20 K–\( T_{c3} \) gives full support to our assumption of constant \( H_i^0 \) and allows one to derive that \( M_{\text{Ni}}^0 = -0.36(7) \mu_B / \text{f.u.}, \) i.e., \( \theta = 13.1(1) ^\circ, \) and \( H_i^0 = 5.2(6) \) T. \( M_0 \) is in close agreement with the value obtained from neutron powder diffraction [\( M_{\text{Ni}}^0 = 0.4(2) \mu_B / \text{f.u.}. \) Moreover, it is also evident that in the temperature range \( T_{c3} - T_{c2}, M_0(T) \) vs \( \chi_d(T) \) also follows a linear law, though the weak ferromagnetic component of the Ni\(^{2+}\) magnetic moments \( M_{\text{Ni}}^0 \) (defined as the crossing point with the y axis) and the internal magnetic field \( H_i^0 \) (defined as the slope of the linear law) have been drastically reduced with respect to the former interval 20 K–\( T_{c3} \). Then, we understand that at \( T_{c3} \approx 45 \) K some kind of sudden spin reorientation of the Ni\(^{2+}\) magnetic moments takes place, leading, below this temperature, to a sharp increase in both the weak ferromagnetic component and the canting angle \( \theta \), which provokes a marked increase in the internal field acting on Ni ions.

(b) On the other hand, when \( T > T_{c2} \approx 68 \) K, the extrapolated behavior of \( M_0(T) \) vs \( \chi_d(T) \) shows that \( M_{\text{Ni}}^0 \approx 0 \), while the internal magnetic field has been even more drastically reduced, thus signaling that the weak ferromagnetic component of the Ni\(^{2+}\) magnetic moments develops below \( T_{c2} \) and that some kind of spin reorientation, which should be similar in principle to that observed at \( T_{c3} \), occurs at this temperature.

(c) Finally, below 20 K and down to \( T_{N2} \approx 11 \) K, \( M_0 \) clearly increases. This fact should not be taken as a proof of a consequent increase in the internal field acting on Ni ions due to the Nd-Ni superexchange interaction, but rather as the contribution of the magnetocrystalline anisotropy associated with Nd ions, which develops exactly at this temperature (see Sec. V).

We should remark that (i) A NQR investigation on stoichiometric La\(_2\)NiO\(_4\) (Ref. 20) demonstrates that the out-of-plane component of the internal field acting on the La sites (\( H_i \approx 1.97 \) T, which is quite similar to the value we have found in Nd\(_2\)NiO\(_4\)) is much stronger than that observed in stoichiometric La\(_2\)CuO\(_4\) [\( H_i = 0.1 \) T (Ref. 30)], while a simple calculation shows that this relative increase cannot be due to the dipolar interaction thus meaning that the superexchange interaction should be invoked. This is quite understandable if we consider that the Ni-O(2) (apical oxygen) distance is smaller than that of Cu-O(2) [Nd\(_2\)NiO\(_4\): \( d(\text{Ni-O2}) = 2.19 \) Å; La\(_2\)NiO\(_4\): \( d(\text{Ni-O2}) = 2.24 \) Å; La\(_2\)CuO\(_4\): \( d(\text{Cu-O}) = 2.39 \) Å].

(ii) The c component of the internal magnetic field acting on Nd ions at low temperature (20 K–\( T_{c3} \)) is much higher than that observed in the \( T' \) compounds [Gd\(_2\)CuO\(_4\): \( H_i = 0.074 \) T (Ref. 27)]. This difference is probably mainly related to the differences in the topology between the K\(_2\)NiFe\(_2\) and the Nd\(_2\)CuO\(_4\) crystal structures. In both the \( T \) and \( T' \) structures, the TM sublattice is antiferromagnetically aligned and the four nearest-neighbor interactions at the R site cancel by symmetry, in such a way that the net TM-R superexchange coupling arises from next-nearest-neighbor. However, in the \( T \) structure there is one additional nearest-neighbor superexchange interaction which is not canceled by symmetry (that connecting the rare-earth and Ni ions through the apical oxygen of the NiO\(_6\) octahedron), while in the \( T' \) structure this interaction is absent because of the planar coordination of Cu ions.

(iii) Further, the value of the Ni canting angle \( \theta \) is not far from that reduced for the Nd and Ni ions from neutron diffraction (\( \theta = 18.2^\circ \) and 14.6\(^\circ \), respectively, at 1.5 K). This slight difference should not be taken as a proof of a noncollinear magnetic structure among Nd and Ni ions. In fact, within the magnetic field range investigated here, \( M_0 \) is still increasing, thus indicating that the magnetic domains have not completely disappeared (the domain-wall inversion is not fully accomplished up to \( H \approx 8 \) T) and so our \( \theta \) value is only a lower limit.

(iv) Referring to the origin of the spin reorientations at \( T_{c3} \) and \( T_{c2} \), we can argue that NPD is unable to distinguish between the two in-plane magnetic modes allowed by the crystallographic symmetry \(( g_x + c_y \) and \( g_x c_y )\) since the low-temperature phase is tetragonal. In this sense, a hypothetic spin reorientation of the Ni\(^{2+}\) magnetic moments from the [110] direction to the [100] direction (or vice versa) would not be detected. However, this reorientation might have some effects on the ferromagnetic component \(( f_x )\) mode, due to the fact that, in both magnetic modes, the relative arrangement of the Ni\(^{2+}\) magnetic moments with respect to the tilting axis of the NiO\(_6\) octahedra is different. Although the origin of these spin reorientations is not very clear, it might be related to a change in the local easy magnetization axis associated with the magnetocrystalline anisotropy of Ni ions, leading to the mentioned upturn of the saturation magnetiza-
2. Origin of the field-induced transition

The negative sign of $M_0^{N_{i}}$ indicates that the Nd-Ni interaction is antiferromagnetic. This result suggests a possible interpretation of the field-induced transition observed in the magnetization curves.

NPD experiments\(^6\) demonstrate that below $T_{c1} \approx 130$ K a ferromagnetic long-range order of the out-of-plane component of Nd$^{3+}$ magnetic moment appears, standing at an angle of 18.2° with respect to the basal plane at $T = 1.5$ K, thus meaning a value of 1.0(2)$µ_B$/Nd atom (the total fitted magnetic moment is 3.2$µ_B$/Nd atom), while the out-of-plane component of the Ni$^{2+}$ magnetic moment is about 0.42(2)$µ_B$/f.u. which implies that $θ \approx 14.6°$ (the total fitted magnetic moment is 1.59$µ_B$/f.u.). On the other hand, since the magnetic domains completely disappear about 8 T, we derive the total saturation magnetization $M_0$ at $T = 4.2$ K from the magnetization curve $M(H)$ with a maximum applied field of 20 T (Fig. 6) and we obtain that $M_0 = 2.25µ_B$/f.u.

On the basis of this framework, the origin of the field-induced transition may be viewed as follows: when the applied field equals the critical field $H_{cr} = 5.2(2)$ T, the ferromagnetic component of Ni$^{2+}$ ions, which lay antiparallel to that of Nd$^{3+}$ ions, undergoes a metamagnetic-like transition, and both out-of-plane components become parallel (Fig. 11). Then, we observe a jump in the $M(H)$ curve, which is not abrupt but smooth, due to the fact that our sample is polycrystalline. Then, when $H_o > H_{cr}$ we may write the total saturation magnetization as

$$M_0 = 2M_0^{Nd} + M_0^{Ni}.$$  \hspace{1cm} (9)

From our data [$M_0 = 2.25µ_B$/f.u. at $T = 4.2$ K and $M_0^{Ni} = 0.36(7)µ_B$/f.u., independent of temperature], we find that $M_0^{Nd} = 0.95(14)µ_B$/Nd at $T = 4.2$ K, which is comparable with that derived from NPD at $T = 1.5$ K ($M_0^{Nd} = 1.0(2)µ_B$/Nd).

The fact that both the critical field (at which the metamagnetic transition takes place) and the internal magnetic field (that reflects the net superexchange coupling Nd-Ni) are equal within the experimental error, gives full support to our assumption of the origin of the field-induced transition. Let us consider an uniaxial antiferromagnet where the applied field is parallel to the easy magnetization axis. When the anisotropy is high, which is in fact the case since the coercive field is enormous and the domain wall inversion is not fully accomplished till 8 T, the antiferromagnetic ordering is stable up to $H_o < H^0_{cr}$, in such a way that when $H_o > H^0_{cr}$ the magnetic moments become ferromagnetically ordered.\(^3\) Then, the out-of-plane components of both Ni and Nd ions lie antiparallel exactly until the applied field equal the internal field.

C. $T < T_{N2}$

It seems experimentally well established that the Nd$^{3+}$ ions become antiferromagnetically ordered at $T_{N2} = 11$ K, although no specific-heat results have been reported up to now. On lowering temperature below $T_{N2}$, no abrupt change is observed in $M_0(T)$, though this magnitude smoothly tends to the saturation regime [Fig. 9(b)]. Then, if the out-of-plane component of the Ni$^{2+}$ magnetic moments $M_0^{Ni}$ does not significantly vary from that value we have obtained in the paramagnetic phase of the $R(T > T_{N2})$, $M_0(T)$ is basically governed by the behavior of the out-of-plane component of the Nd$^{3+}$ ions. Then, the $c$ axis component of the internal field acting on these ions is not modified by their long-range ordering of Nd ions and $M_0$ smoothly increases since Nd ions are not yet saturated. This leads to the conclusion that both the $J_{Nd-Ni}$ and $J_{Nd-Nd}$ superexchange interactions do not compete with each other, which is consistent with the reported magnetic structure if the $J_{Nd-Nd}$ interaction is antiferromagnetic.

Finally, the high-field magnetic susceptibility $\chi_d$ [Fig. 8(a)] displays a sharp peak at $T_{N2}$, reflecting an antiferromagnetic ordering of the in-plane component of Nd ions, and tends to zero when $T \rightarrow 0$. This might be due to the crystal-field energy-level splitting of Nd ions at low temperature arising from the crystallographic symmetry.

V. MAGNETIC INTERACTIONS

Let us assume that the magnetic Hamiltonian describing the magnetic interactions in Nd$_2$NiO$_4$ may be written as follows:

$$H = J_{Ni-Ni} \sum_{NN} S_{Ni}^i \cdot S_{Ni}^j + J_{Ni-Nd} \sum_{NN} S_{Ni}^i \cdot S_{Nd}^j + D_{Ni-Ni} \sum_{NN} S_{Ni}^i \times S_{Ni}^j + J_{Nd-Ni} \sum_{NN} S_{Nd}^i \cdot S_{Ni}^j + K_{Nd} \sum_{i} (n_i \cdot s_i)^2,$$  \hspace{1cm} (10)

where all the sums are extended to nearest neighbors, except for the second one which is extended to next-nearest neighbors, and the last one which is extended to all the
Nd ions in the sample. \(J_{\text{Ni-Ni}}\) and \(D_{\text{Ni-Ni}} = (0, D_{\text{Ni-Ni}}, 0)\) stand respectively for the in-plane symmetric and antisymmetric parts of the antiferromagnetic Ni-Ni superexchange interaction, while \(J'_{\text{Nd-Ni}}\) stands for the magnetic interactions between two adjacent NiO\(_2\) planes. \(J_{\text{Nd-Ni}}\) is the isotropic symmetric antiferromagnetic Nd-Ni superexchange coupling constant. Moreover, in Eq. (10) we have assumed the magnetocrystalline anisotropy of Nd ions to be uniaxial, thus meaning that \(n\) and \(s\) stand for, respectively, the unitary vectors along the \(c\) axis and along the direction defined by the Nd magnetic moments. Then, \(K^{\text{Nd}}\) represents the anisotropy energy per Nd spin, and is related to the first anisotropy constant \(K^{\text{Nd}}\) through

\[
K^{\text{Nd}}_1 = K^{\text{Nd}}(z'/v_{\text{uc}}),
\]

where \(z'\) is the number of Nd ions per unit cell and \(v_{\text{uc}}\) is the volume of the unit cell. In Eq. (10), we have ignored for simplicity the antisymmetric Ni-Nd superexchange interaction \(D_{\text{Nd-Ni}}\) and the symmetric Nd-Nd \(J_{\text{Nd-Nd}}\). In this sense, it is obvious that our magnetic Hamiltonian is not able to take into account the long-range magnetic ordering of Nd\(^{3+}\) ions.

Labeling \(\theta\) and \(\theta'\) as the canting angles, respectively, of the Ni and Nd magnetic moments with the \(a\)-\(b\) plane and minimizing the system energy with respect to \(\theta\) and \(\theta'\), the equilibrium state will be reached when

\[
-4J_{\text{Ni-Ni}}S_{\text{Ni}}^zS_{\text{Ni}}^z\sin(2\theta) - 8J'_{\text{Ni-Ni}}S_{\text{Ni}}^zS_{\text{Ni}}^z\sin(2\theta) + 4D_{\text{Ni-Ni}}S_{\text{Ni}}^zS_{\text{Ni}}^z\cos(2\theta)
\]

\[-10J_{\text{Nd-Ni}}S_{\text{Nd}}^zS_{\text{Nd}}^z\sin(\theta + \theta') = 0,
\]

\[-5J_{\text{Nd-Ni}}S_{\text{Nd}}^zS_{\text{Nd}}^z\sin(\theta + \theta') - 4K^{\text{Nd}}\sin\theta'\cos\theta' = 0,
\]

and knowledge of the magnetic interactions \((J_{\text{Ni-Ni}}, D_{\text{Ni-Ni}}, J'_{\text{Ni-Ni}}, J_{\text{Nd-Ni}}, K^{\text{Nd}})\) will lead us to the determination of the magnetic structure, which is parametrized by \((\theta', \theta)\).

### A. Magnetic interactions at 0 K

Concerning \(J_{\text{Ni-Ni}}\), Aeppli et al.\(^4\) found that \(J_{\text{Ni-Ni}} \approx -20\) meV in La\(_2\)NiO\(_4\). When moving from La\(_2\)NiO\(_4\) to Nd\(_2\)NiO\(_4\), the superexchange angle \(\varphi\) decreases, due to the fact that the tilting angle of the NiO\(_6\) octahedra increases, and the in-plane superexchange distance \(d = O(1)-\text{Ni-O}(1)\) increases\(^6,11\) in such a way that both effects tend to reduce the in-plane magnetic interaction. Assuming the well-known dependences of the superexchange coupling constant \(J\) with respect to \(\varphi\) (Ref. 32) and \(d\),\(^11\)

\[
J(\varphi) = J_0\cos^2\varphi, \quad J(d) = J_0d^{-12}
\]

and taking into account those values of the superexchange angles and distances determined by NPD,\(^6,11\) we expect to obtain a relative decrease of about 5% in the in-plane antiferromagnetic exchange interaction \(J_{\text{Ni-Ni}}\) when moving from La\(_2\)NiO\(_4\) to Nd\(_2\)NiO\(_4\), thus meaning that \(J_{\text{Ni-Ni}}(\text{Nd}_2\text{NiO}_4) \approx -19\) meV.

On the other hand, let us assume that the strong bidimensionality of the crystallographic structure makes Nd\(_2\)NiO\(_4\) a good example of the two-dimensional antiferromagnetic Heisenberg model.\(^3,18\) We may also assume that the 3D long-range antiferromagnetic ordering appears because of the intraplane interaction \(J_{\text{Ni-Ni}}\). It is worth noting that \(J'_{\text{Nd-Ni}}\) is a super-supercoupling term that cancels by symmetry at nearest neighbors when the structure is tetragonal type K\(_2\)NiF\(_4\). In this basic framework, the two-dimensional in-plane antiferromagnetic correlation length \(\xi\) increases upon lowering temperature, and when the effective interplane interaction \([J(T)/a]^2J_{\text{Nd-Ni}}\) (\(a\) stands for the in-plane cell parameter) becomes comparable to the thermal energy \(K_B T\), a 3D ordering occurs. Then, at the Néel temperature, we can write\(^3,18\)

\[
(M_s/M_0)\xi(J(T)/a)^2J'_{\text{Nd-Ni}} \approx K_B T\],
\]

where the factor \(M_s/M_0\) accounts for the relative importance of the zero-point quantum fluctuations,\(^3,18\) which are enhanced in the 2D Heisenberg antiferromagnetic systems. In Nd\(_2\)NiO\(_4\), the \(S = 1\) spin reduction is about 20% \((M_s \approx 1.59\mu_B, M_0 \approx 2\mu_B)\). Equation (15) shows that knowledge of the in-plane correlation length at the Néel temperature \(l(T_N)\) is necessary in order to determine the interplane interaction \(J'_{\text{Nd-Ni}}\). Chakravarty, Halperin, and Nelson\(^3,18\) have recently developed a quantitative theory (CHN theory) to account for the temperature-dependence of the instantaneous spin-spin antiferromagnetic in-plane correlation length in the 2D Heisenberg models, which may be written as follows

\[
S = 1: l/a = C \exp[2\pi\rho_s/(K_B T)/(1 + K_B T/2\pi\rho_s)],
\]

where \(C = 0.17\) and \(\rho_s\) is the spin stiffness constant.\(^3,18\) From our data \((J_{\text{Ni-Ni}} \approx -19\) meV and \(T_N = 320\) K, Eq. (16) leads to \(l(T_N)/a \approx 4.5\). Then, we derive \(J_{\text{Ni-Ni}} \approx -2.2\) meV from Eq. (15). It is remarkable that, as compared to La\(_2\)NiO\(_4\), the effective in-plane correlation length has been reduced by a factor 0.75, while the interplane interaction has been multiplied by a factor of 2 \([\text{La}_2\text{NiO}_4]: l(T_N)/a \approx 6.1; J'_{\text{Nd-Ni}} \approx -1.1\) meV (Ref. 13)]. We believe that the former is caused by the relative reduction in the intraplane superexchange interaction \(J_{\text{Ni-Ni}}(\text{La}_2\text{NiO}_4) \approx -20\) meV; \(\text{Nd}_2\text{NiO}_4: J_{\text{Ni-Ni}} \approx -19\) meV), while the latter is due to the relative decrease of the apical distance Ni-O(2) of the NiO\(_2\) octahedra, through which the interplane superexchange interaction proceeds \([\text{La}_2\text{NiO}_4]: d(\text{Ni-O}(2)) = 2.24\) Å;\(^11\) \(\text{Nd}_2\text{NiO}_4: d(\text{Ni-O}(2)) = 2.19\) Å (Ref. 6). Finally, Eq. (8) has led us to determine the weak ferromagnetic component of the Ni magnetic moment \([H_{\text{Ni}}^0 = -0.36(7)\mu_B/T, \text{e.g., } \theta = 13.1(1)\text{°}\) and the c-axis component of the internal magnetic field acting on Nd ions \([H_{\text{Ni}}^0 = 5.2(6)\text{ T}\). We should remark that both values are constant in the temperature range 20 K \(- T_{\text{C}}\) and in this evaluation we have neglected the anisotropy field acting on Nd ions. In this framework and on the scope of the mean-field approximation, the fitted \(H_{\text{Ni}}^0\) and \(M'_{\text{Ni}}\) led us to a first evaluation of an isotropic exchange coupling
\[ J_{\text{Nd-Ni}} \text{ by using the formula} \]
\[ H_0^0 = 2J_{\text{Nd-Ni}} M_{\text{Ni}}^2 / N g_{\text{Ni}} g_{\text{Nd}} \mu_B^2 \]  
(17)

from which we obtain that \( J_{\text{Nd-Ni}} \approx -0.6 \) meV. We have not found any thorough evaluation of the R-TM superexchange coupling in these kinds of oxides. For example, Dalichaouch et al.\(^{37}\) report that an abrupt upturn on the upper critical field of superconducting Sm\(_{1.15}\)Ce\(_{0.15}\)Cu\(_{0.4}\) as compared to superconducting Nd\(_{1.64}\)Ce\(_{0.15}\)Cu\(_{0.4}\), takes place as soon as the Sm sublattice orders antiferromagnetically along the c axis at \( T_{N2} \approx 4.9 \) K, and from the temperature dependence of the upper critical field they derive that the exchange interaction between the localized Sm magnetic moments, and the spin of the superconducting charge carriers is about \( J \approx 60 \) meV. However, the two values \( J_{\text{Nd-Ni}} \approx -0.6 \) meV; \( J_{\text{Nd-Ni}} \approx -0.6 \) meV; \( J_{\text{Nd-Ni}} \approx -0.6 \) meV, \( \theta \approx 13.1^\circ \), and \( \theta' \approx 18.2^\circ \), besides Eqs. (11), (12), and (13), allows us to obtain

\[ D_{\text{Ni-Ni}} \approx -16 \text{ meV} \]  
(18)

Concerning the first anisotropy constant associated with Nd ions, \( K_{\text{Nd}} \) is roughly the order of magnitude of the typical values of rare earths \( (K_{\text{Nd}} \approx 1.6 \times 10^8 \text{ erg/cm}^3 \) in a Nd\(_2\)Fe\(_4\)B single crystal,\(^{38}\) thus meaning that the anisotropy of Nd\(_2\)NiO\(_4\) is very large at low temperature.

Referring to the antisymmetric Ni-Ni superexchange interaction \( D_{\text{Ni-Ni}} \), the huge relative increase with respect to La\(_2\)NiO\(_4\) \( (D_{\text{Ni-Ni}} \approx -0.1 \) meV; La\(_2\)NdO\(_4\): \( D_{\text{Ni-Ni}} \approx -16 \) meV) is on the origin of the consequent increase of the canting angle \( \theta \) of the Ni\(^{2+}\) magnetic moments with respect to the basal plane (\( \theta \) varies from 0.14° to 13.1° on moving from La\(_2\)NdO\(_4\) to La\(_2\)NiO\(_4\)). On the other hand, the antisymmetric should be proportional to the overlap between the \( d_{2-y}^z \) orbitals of neighboring sites, which, at the same time, increases with the tilting angle of the NiO\(_6\) octahedra. This tilting angle is greater in Nd\(_2\)NiO\(_4\) (Ref. 6) than in La\(_2\)NiO\(_4\).\(^{11}\)

**B. Canting angles \( \theta \) and \( \theta' \) as a function of temperature**

In Eqs. (12) and (13), only \( K_{\text{Nd}} \) has an explicit dependence on temperature. Let us assume that the temperature dependence of first anisotropy constant for rare-earth elements may be written\(^{31}\)

\[ K_{\text{Nd}}(T) = K_{\text{Nd}}(T = 0)[M(T)/M(0)]^3 \]  
(19)

where \( M(T) \) is spontaneous magnetization at a given temperature and \( M_0 \) is the spontaneous magnetization at zero kelvin. NPD diffraction shows\(^{39}\) (i) the \( a-b \) component of the Nd ions magnetic moments is about 0.1\( \mu_B \) /Nbd atom at 68 K, and increases to 0.5\( \mu_B \) at 45 K and to 1\( \mu_B \) /Nd atom at 20 K, and (ii) the \( c \) component is below the detection level about 20 K, and it is about 0.05\( \mu_B \) /Nd atom at this temperature. From these data, Eq. (19) determines that, at 20 K, \( K_{\text{Nd}} = 5.1 \times 10^6 \text{erg/cm}^3 \) and \( K_{\text{Nd}} = 0.13 \text{ meV} \), which is about the 3% of the value at 0 K, while at 45 K \( K_{\text{Nd}} = 6.8 \times 10^6 \text{erg/cm}^3 \) and \( K_{\text{Nd}} = 0.017 \text{ meV} \), which is about the 0.4% of the value at 0 K. Then, we understand that the Nd-ion anisotropy will be high at low temperature (the large increase of the coercive field at low temperature—see Fig. 5—reinforces this assertion) and it is in no way relevant above 20 K, thus meaning that in the determination of \( H_0^0 \) [Eqs. (6)–(8)] it is not worth taking into account.

Finally, NPD shows that the Nd-ion canting angle \( \theta' \) is practically zero above 20 K, from which we believe that the origin of both the huge increase in the ferromagnetic component at low temperature shown by NPD and also the upturn of \( M_0(T) \) (Fig. 10) below 20 K should be related to the magnetic anisotropy associated with Nd ions.

On the other hand, as soon as we know the temperature dependence of \( K_{\text{Nd}} \), Eqs. (12) and (13) will allow us to ascertain the temperature dependence of the canting angle \( \theta \) and \( \theta' \). At 45 K, we derive that \( \theta = 13.4^\circ \) and \( \theta' = 0^\circ \), while at 20 K the best solution to our equation system is obtained when \( \theta = 13.5^\circ \) and \( \theta' = 0^\circ \). It is now clear that the canting angle \( \theta \) of the magnetic moments of Ni ions, and consequently the weak ferromagnetic component \( M_{\text{Ni}}^0 \) does not change in the temperature range 20 \( K-T_{c3} \), giving further support to the way we have derived \( J_{\text{Nd-Ni}} \). It is also obvious that from our proposed magnetic Hamiltonian [Eqs. (12) and (13)] we are not able to account for any discontinuous phenomena. In this sense, the spin reorientation observed at \( T_{c3} \) is beyond our goals and cannot be explained in this framework, which is nevertheless valid, in principle, when \( T < T_{c3} \).

**VI. SUMMARY AND CONCLUSIONS**

We have analyzed the complex magnetic behavior observed in stoichiometric antiferromagnetic Nd\(_2\)NiO\(_4\) oxide. It is found that the interactions associated with the Nd\(^{3+}\) ions lead to a temperature-dependent weak ferromagnetic behavior, to a magnetic structure where the Nd and Ni magnetic moments are not collinear, and finally to a magnetic-field-induced (metamagneticlike) transition. It is also stressed that the Nd magnetic moments present a long-range magnetic ordering at low temperature, which is probably mediated by the polarization effect associated with the internal field created by the Ni magnetic moments.

The leading microscopic magnetic interactions have been discussed taking into account the analysis carried out for stoichiometric La\(_2\)NiO\(_4\). The magnetic properties of the latter have been recently shown\(^{13}\) to be easily investigated in the scope of the 2D Heisenberg model proposed by Chakravartty et al.\(^{34}\) We have assumed that the essential features of this model are also valid for Nd\(_2\)NiO\(_4\) and hence we obtain a set of symmetric and antisymmetric superexchange interactions associated with Ni ions. Furthermore, the Ni-Nd exchange is also determined and it is evidenced in some experimental features,
i.e., the paramagnetic behavior in the collinear high-temperature antiferromagnetic phase, the field-induced transition, the strongly enhanced weak ferromagnetic component, etc.

Finally, several experimental results have forced us to introduce a uniaxial single-ion contribution of Nd ions to the magnetic anisotropy in the magnetic Hamiltonian describing the magnetic interactions of this oxide. We have shown that both this term and the strong enhancement of the antisymmetric $D_{xy}$ interaction, as compared to $La_2NiO_4$, allow us to explain the appearance of very large canting angles for the Ni and Nd magnetic moments.

As a final conclusion, our study shows that even if the magnetic behavior of both Nd$_2$CuO$_4$ and Nd$_2$NiO$_4$ is highly complex, some severe differences in the rare-earth transition-metal interaction exist. The $T'\uparrow$ cuprates seem to have, in some cases, a weak ferromagnetic component which appears within the a-b plane, while the ferromagnetic component in Nd$_2$NiO$_4$ is along the c axis. The origin of these ferromagnetic components in the $T'$ structure and how they interact with the rare-earth ions is still an object of discussion. From our study, it may be inferred which are those magnetic interactions that should be also taken into account in the $T'$ structure. This is a problem that now holds a strong interest in the context of understanding the relationship between high-temperature superconductivity and magnetism.$^{37-40}$

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39J. Rodriguez-Carvajel (private communication).