

Magnetic structure of Li_2CuO_2 : From *ab initio* calculations to macroscopic simulationsCoen de Graaf,^{1,*} Ibérico de P. R. Moreira,² Francesc Illas,³ Òscar Iglesias,⁴ and Amílcar Labarta⁴¹*Department de Química Física e Inorgànica and Institut d'Estudis Avançats, Universitat Rovira i Virgili, Plaça Imperial Tàrraco 1, 43005 Tarragona, Spain*²*Gruppo di Chimica Teorica, Dipartimento di Chimica Inorganica, Chimica Fisica e Chimica dei Materiali, Facoltà di Chimica, Università di Torino, Via Pietro Giuria 5, I-10125 Torino, Italy*³*Department de Química Física, Universitat de Barcelona and Centre de Recerca en Química Teòrica, Parc Científic de Barcelona C/Martí i Franquès 1, 08028 Bracelona, Spain*⁴*Department de Física Fonamental, Facultat de Física, Universitat de Barcelona, Diagonal 647, 08028 Barcelona, Spain*

(Received 11 March 2002; published 25 July 2002)

The magnetic structure of the edge-sharing cuprate compound Li_2CuO_2 has been investigated with highly correlated *ab initio* electronic structure calculations. The first- and second-neighbor in-chain magnetic interactions are calculated to be 142 and -22 K, respectively. The ratio between the two parameters is smaller than suggested previously in the literature. The interchain interactions are antiferromagnetic in nature and of the order of a few K only. Monte Carlo simulations using the *ab initio* parameters to define the spin model Hamiltonian result in a Néel temperature in good agreement with experiment. Spin population analysis situates the magnetic moment on the copper and oxygen ions between the completely localized picture derived from experiment and the more delocalized picture based on local-density calculations.

DOI: 10.1103/PhysRevB.66.014448

PACS number(s): 75.10.Dg, 75.50.Ee

I. INTRODUCTION

The impressive richness of the magnetic behavior of the different copper oxide compounds can be traced back to a large extent to the stacking of the CuO_4 plaquettes in the lattice. Corner sharing CuO_4 units give rise to large antiferromagnetic interactions, while edge sharing units normally result in rather weak ferromagnetic interactions. Depending on the number of linkages between the different CuO_4 units, spin chains are formed (neighbors in one direction only) or CuO_2 planes appear, typical of the high- T_c superconductor cuprates. The combination of edge sharing and corner sharing CuO_4 plaquettes can give rise to spin ladders (e.g., the $\text{Sr}_{n-1}\text{Cu}_n\text{O}_{2n-1}$ with $n \geq 2$ series) or zigzag spin chains (e.g., SrCuO_2). Based on these geometrical considerations, Li_2CuO_2 can be classified as a quasi-one-dimensional (1D) spin- $\frac{1}{2}$ chain formed by edge sharing CuO_4 units. Hence it is expected that the dominant magnetic interaction along the spin chain is ferromagnetic and that there exist additional weaker interchain interactions that account for the nonzero Néel temperature. The sign of the latter interactions cannot be predicted beforehand and must be derived either from interpretation of experimental data or by independent high-level theoretical treatment of the electronic structure.

The magnetic structure of Li_2CuO_2 was described by Sapiña and co-workers.¹ Their neutron-scattering experiments indicate that spin ordering sets in at approximately 9 K and consists of an antiferromagnetic (AFM) alignment along the body diagonal of ferromagnetically (FM) ordered spin chains that run along the b axis (see Fig. 1). The magnetic moment of $0.92\mu_B$ was entirely attributed to the Cu^{2+} ion. Later, Boehm and co-workers measured the dispersion of the spin-wave excitations in this compound and they interpreted the results with a Heisenberg Hamiltonian in which six different magnetic coupling parameters appear.² They classify Li_2CuO_2 as an antiferromagnetic insulator with

competing magnetic interaction based on their finding that all nearest-neighbor interactions, including the in-chain interaction, were predicted to be antiferromagnetic and of similar size. The magnitude of all these interactions was found to be rather small, less than 3 K. In addition, a significant second-neighbor in-chain interaction was reported ferromagnetic in character.

Li_2CuO_2 has also been subject of theoretical studies. Several authors performed density-functional theory (DFT) calculations within the local-density approximation (LDA) on the periodic structure.³⁻⁷ In all these studies the nonmagnetic phase has been found to be metallic and a small band gap of ~ 0.1 eV is found for the antiferromagnetic alignment of the

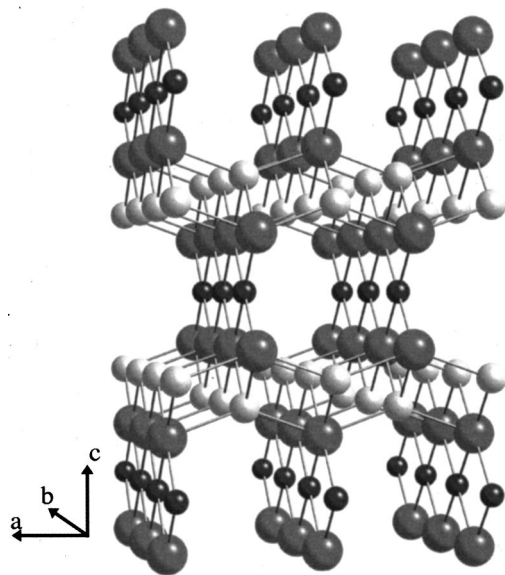


FIG. 1. Crystal structure of the quasi-1D spin-chain Li_2CuO_2 . Small dark gray spheres represent copper ions, large gray spheres depict the oxygen ions, and the light spheres the lithium ions.

spin chains.^{4,6,7} Weht and Pickett,⁴ and Neudert *et al.*³ fitted the antibonding band consisting of Cu- $3d_{xy}$ and O- $2p$ orbitals with four different hopping parameters. Both for the in-chain and interchain hopping, the fit results in second-neighbor interactions that are larger than the nearest-neighbor couplings.^{3,4} Moreover, the LDA calculations result in magnetic moments as large as $0.2\mu_B$ for the oxygen ions in the compounds, which is claimed to be larger than any experimental O moment.⁴ Similar conclusions were derived by Tanaka, Suzuki, and Motizuki,⁷ who studied the effect of the introduction of the on-site repulsion in the LDA scheme by applying the LDA+ U scheme. For $U=4$ eV, a band gap of 0.72 eV was found. The magnetic moment on oxygen is hardly sensitive to the introduction of the on-site repulsion in the calculation, it only changes from $0.22\mu_B$ for LDA to $0.21\mu_B$ for LDA+ U with $U=4$ eV.

Mizuno *et al.* analyzed the magnetic interactions in this system by diagonalizing a three band Hubbard Hamiltonian for finite copper oxide clusters.⁸ The model parameters were derived from experiment or taken from the lamellar cuprates La_2CuO_4 and $\text{Sr}_2\text{CuO}_2\text{Cl}_2$. The experimental data could be well reproduced by a ferromagnetic nearest-neighbor interaction of 100 K and a second-neighbor interaction of -60 K, antiferromagnetic in nature. The latter value is reduced to -40 K when interchain interactions along the body diagonal are taken into account. This interchain interaction was calculated to be -16 K.⁹

This surprisingly large second-neighbor coupling has been attributed to the short distance between oxygens on the chains which can cause a relatively large overlap between oxygens that connect second-neighbor copper ions.^{4,8,9} For comparison, the O-O distance in Li_2CuO_2 along the chains is 2.86 Å, while the interatomic distance is 3.9 Å for oxygens in corner sharing spin-chain compounds as Sr_2CuO_3 and Ca_2CuO_3 .

In this paper, we apply the well-established computational methods of quantum chemistry as an alternative to the above-mentioned approaches to obtain insight in the complex magnetic structure of Li_2CuO_2 . As an extension of a preliminary study,¹⁰ attention will not only be focused on the accurate determination of the in-chain magnetic parameters, but also on the interchain magnetic interactions and the hopping parameters. The *ab initio* quantum chemical schemes provide a sound hierarchy of increasing accuracy and can be applied both within a periodic and a local (or cluster model) representation of the material. Results obtained over the last decade show that quantum chemical methods, which will be introduced in some more detail in the next section, are capable of reproducing the nature and the absolute magnitude of magnetic interactions in quantitative agreement with experiment.^{11,12} For the present material, experimental data about the magnetic coupling parameters is less clear and the validity of the *ab initio* microscopic electronic structure parameters must be established in a different way. For this purpose, we perform several checks, internal and external, to the computational schemes applied. In the first place, we validate the cluster model comparing the results with periodic calculations performed at the same level of approximation. Second, the cluster size and basis set dependence of the pa-

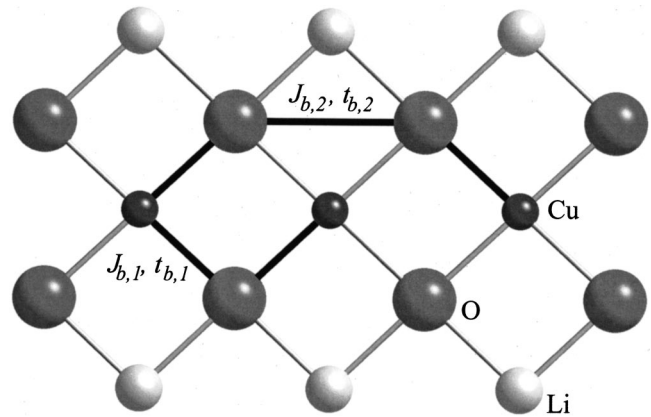


FIG. 2. Interaction pathways (marked by black lines) for the in-chain magnetic coupling and hopping parameters.

rameters is investigated. However, the most important check is provided by the determination of several thermodynamic equilibrium quantities through Monte Carlo simulations using the *ab initio* microscopic electronic structure parameters to define the effective magnetic Hamiltonian. These macroscopic quantities can easily be compared with experiment and provide us with a rigorous check on the consistency of the parameters.

II. QUANTUM CHEMICAL DETERMINATION OF J AND t

Figures 2 and 3 illustrate the pathways for the magnetic interactions and hopping processes considered in the present study. In the first place, we focus our attention on the relative magnitude of the in-chain interactions to clarify the uncertainty about the importance of second-neighbor interactions

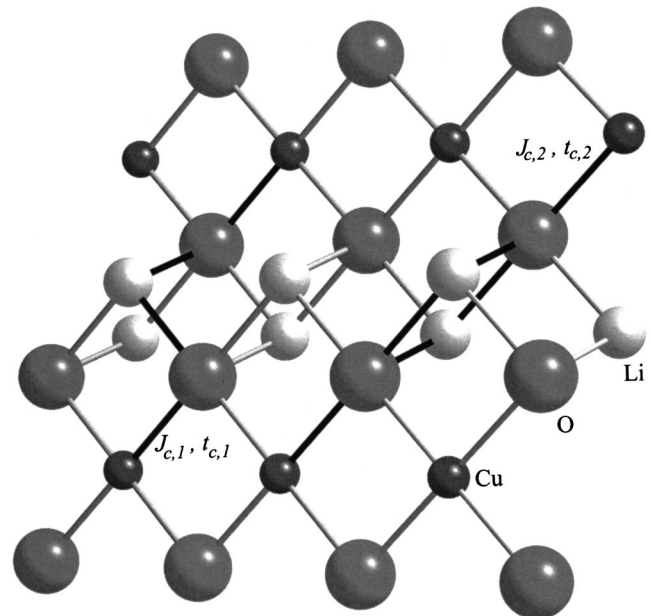


FIG. 3. Interaction pathways (marked by black lines) for the interchain magnetic coupling and hopping parameters between chains located in different a - b planes. For the nearest-neighbor interactions ($J_{c,1}$ and $t_{c,1}$) six equivalent pathways can be defined.

($J_{b,2}$ and $t_{b,2}$) and the nature of the first-neighbor interactions ($J_{b,1}$ and $t_{b,1}$), for which $J_{b,1}$ has been claimed to be antiferromagnetic^{1,2} in spite of the almost rectangular nature of the Cu-O-Cu bond and in contradiction to the Goodenough-Kanamori-Anderson rules.¹³⁻¹⁵ Second, we derive *ab initio* estimates of the interchain interactions. Beside the nearest-neighbor interactions along the a axis ($J_{a,1}$ and $t_{a,1}$, not shown in the figures) and the body diagonal ($J_{c,1}$ and $t_{c,1}$), we also consider the next-nearest-neighbor interaction along the body diagonal ($J_{c,2}$ and $t_{c,2}$). The latter interaction has been claimed to be as important as the nearest-neighbor interaction by Mizuno *et al.*⁹ Although the copper ions involved in this interaction are more separated than for $J_{c,1}$, the magnetic pathway is identical (Cu-O-Li-O-Cu) for both interactions. From geometrical considerations, it can even be expected that the next-nearest-neighbor pathway is more favorable (see Fig. 3).

A. Computational methods and material model

Two requisites must be fulfilled for an accurate determination of the electronic structure parameters with a finite representation of the material. In the first place, the cluster model must be chosen such that no serious artifacts are introduced. Once the material model is fixed, the appropriate N -electron eigenfunctions of the resulting exact (nonrelativistic) cluster Hamiltonian must be approximated in a very accurate way. *Ab initio* cluster model studies performed over the last ten years established a successful computational strategy to meet both criteria.^{11,12,16-24}

The cluster model is constructed by including the magnetic centers and its direct neighbors in the quantum cluster region, which is treated at an all-electron level. These atoms are embedded in a set of total ion potentials (TIP's) that represent the cations surrounding the quantum region.²⁵ Thereafter, optimized point charges are added to account for the long-range electrostatic interactions of the quantum region with the rest of the crystal. The TIP's account for the short-range interaction between cluster atoms and surroundings (Coulomb and exchange interaction) and avoid the spurious delocalization of the charge distribution of the oxygens towards the bare positive point charges. The basic unit to study the in-chain magnetic interactions ($J_{b,1}$ and $J_{b,2}$) is the $\text{Cu}_3\text{O}_8\text{Li}_6$ cluster embedded in two Cu^{2+} TIP's plus point charges. The small number of electrons associated with the Li^+ ions permits us to add these ions to the quantum region instead of treating them (more approximately) with TIP's. Similar considerations lead to the following quantum regions for the interchain interactions: $\text{Cu}_2\text{O}_8\text{Li}_4$ for $J_{a,1}$ and $t_{a,1}$, $\text{Cu}_2\text{O}_8\text{Li}_4$ for $J_{c,1}$ and $t_{c,1}$, and $\text{Cu}_2\text{O}_8\text{Li}_2$ for $J_{c,2}$ and $t_{c,2}$. Again, all these cluster models are completed by adding TIP's and optimized point charges. Because no simple relation exists to extract the hopping parameters from a three center cluster,²⁶ the in-chain hopping parameters $t_{b,1}$ and $t_{b,2}$ are extracted from a $\text{Cu}_2\text{O}_6\text{Li}_4$ and a $\text{Cu}_2\text{O}_8\text{Li}_6$ cluster, respectively. The latter cluster is identical to that used to calculate $J_{b,1}$ and $J_{b,2}$ but for the Cu^{2+} ion in the center of the cluster which is replaced by a $2+$ point charge. This modified cluster has been applied before by Mizuno *et al.* to de-

rive $J_{b,2}$ and Sec. II F will show that the modification does not seriously affect the results.

The Heisenberg Hamiltonian reduces to $\hat{H} = -J\hat{S}_1\hat{S}_2$ for the two center clusters and the magnetic coupling constant is obtained from the energy difference of the singlet and triplet coupled spin states. Positive J 's correspond to ferromagnetic interactions and a negative J indicates that antiferromagnetic coupling is preferred. The hopping integral t can be defined as the matrix element of the Hamiltonian between the states in which the hole is localized on center a and center b . In a symmetry adapted description of the electronic structure, this matrix element corresponds to half the energy difference between the states with the hole in the magnetic orbital of gerade symmetry [$g = (1/\sqrt{2})(a+b)$] and ungerade symmetry [$u = (1/\sqrt{2})(a-b)$].^{27,28} The three center cluster allows a simultaneous calculation of $J_{b,1}$ and $J_{b,2}$ using the relations between the spin eigenstates of the Heisenberg Hamiltonian $\hat{H} = -J_1(\hat{S}_1\hat{S}_2 + \hat{S}_2\hat{S}_3) - J_2\hat{S}_1\hat{S}_3$ and the electronic eigenstates of the cluster Hamiltonian. From the mapping we obtain $J_{b,1} = \frac{2}{3}[E(D_u) - E(Q_u)]$ and $J_{b,2} = J_{b,1} - [E(D_u) - E(D_g)]$,²⁹ where Q_u is the quartet coupled spin state of ungerade symmetry, and D_u and D_g the doublet states of ungerade and gerade symmetry, respectively.

The methods to compute the electronic structure have been applied before to many related transition-metal compounds in the study of magnetic coupling constants and hopping parameters. Here, we will only briefly review the main point of the methods; for a more detailed description the reader is referred to previous work (Refs. 20, 21, 23, and references therein). The simplest yet physically meaningful approximation of the N -electron wave function is a complete active space (CAS) wave function constructed by distributing the unpaired electrons in all possible ways over the magnetic orbitals. This corresponds to the unscreened Anderson model of superexchange and will be used here as the reference wave function for more elaborate treatments of the electronic structure that include a much larger part of the electron correlation. In the first place, we apply the difference dedicated configuration interaction (DDCI) scheme, which is specially designed to obtain accurate energy differences.³⁰⁻³² The method excludes those determinants from the CI wave function that up to second-order perturbation theory do not contribute to the energy difference of the electronic states under study. These are exactly the determinants connected to double replacements from the inactive (or doubly occupied) orbitals into the virtual (or empty) orbitals. Since these determinants are most numerous, the DDCI selection largely reduces the computational cost with almost no loss of accuracy. Moreover, the method has a much smaller size-consistency error than the complete singles-doubles CI.

Because the computational demands are still quite elevated for the DDCI method, we explore the basis set and cluster size dependency of the electronic structure parameters with an alternative method, namely the complete active space second-order perturbation theory (CASPT2).^{33,34} This method considers the effect of all single and double replacements but treats them only by second-order perturbation theory. The method has recently been shown to reproduce

rather accurately magnetic coupling parameters.²¹ Details about the one-electron basis set can be found in the Appendix.

B. Validation of the material model

The most rigorous modelization of a crystal is obtained by imposing periodic boundary conditions on a small building block, typically the unit cell. This way of representing the crystal leads to band-structure theory for which various implementations exist. The simplest version is the well-known tight-binding method, which is mainly used for qualitative reasoning. Among the quantitative band-structure methods, one of the most popular variants is based on DFT within the local-density approximation. The expression of the exchange-correlation part of the functional is based on the noninteracting electron gas. This functional can be improved by adding gradient corrections or mixing in an arbitrary amount of the exact Fock exchange (the so-called hybrid functionals). Here, we validate our—at first sight somewhat rough—modelization of the crystal by comparing periodic unrestricted Hartree-Fock (UHF) calculations with similar calculations applied to the cluster model. UHF uses the exact nonlocal Fock exchange, but ignores the dynamical electron correlation effects. To a large extent, UHF is the spin unrestricted equivalent of the complete active space self-consistent field (CASSCF) computational scheme mentioned before, i.e., it basically describes the unscreened Anderson model, normally results in the correct sign of the interactions, but largely underestimates the experimental values because only nondynamical electron correlation effects are considered. We apply the linear combination of atomic orbitals (LCAO) approximation to construct the one-electron basis functions in the periodic calculations.

The magnetic coupling parameters are extracted from periodic calculations by comparing the energy per unit cell of different spin alignments.^{22,35,36} However, the difference of the FM and AFM spin alignment in the simple unit cell only gives us information about $J_{c,1}$. To obtain estimates for the interactions corresponding to the five closest Cu-Cu distances, we have considered the following double and triple supercells in addition to the simplest one. Doubling along the a axis gives us two different antiferromagnetic spin alignments [AFM2 a (0) and AFM2 a (1), the S_z quantum number of the supercell is given in parentheses] related to $J_{a,1}$ and $J_{a,2}$. Doubling along the b axis gives us two other antiferromagnetic alignments [AFM2 b (0) and AFM2 b (1)] and provides a way to extract $J_{b,1}$. Finally, the triplication of the unit cell along the b axis [AFM3 b (0)] allows us to extract $J_{b,2}$. The calculation of $J_{c,2}$ requires a fourfold supercell and has not been considered because of the very high computational demand. An overview of the computational details of the periodic calculations can also be found in the Appendix.

Table I reports the UHF energies per unit cell of the different supercells with respect to the simple FM cell. It also lists the relations between these energies and the magnetic coupling parameters obtained by a mapping onto the Ising Hamiltonian.^{22,37,38} For spin unrestricted calculations, one has to rely on the Ising Hamiltonian because the different

TABLE I. UHF relative energies per formula unit of different spin settings in simple (AFM and FM), double [AFM2 a (0), AFM2 a (1), AFM2 b (1), and AFM2 b (0)] and triple [AFM3 b (0)] cells. The relations resulting from a mapping onto the Ising Hamiltonian are also given.

Supercell	Relation	Relative energy (in K)
AFM2 a (0)	$4J_{a,2} + 4J_{c,1}$	-3.474
AFM2 a (1)	$J_{a,1} + 2J_{a,2} + 4J_{c,1}$	-1.895
AFM	$8J_{c,1}$	-1.263
FM	0	0.000
AFM2 b (1)	$J_{b,1} + 2J_{a,2} + 4J_{c,1}$	125.994
AFM3 b (0)	$2J_{b,1} + 4J_{a,2} + 4J_{c,1} + 2J_{b,2}$	241.412
AFM2 b (0)	$2J_{b,1} + 4J_{a,2} + 4J_{c,1}$	252.303

spin settings are in general not eigenfunctions of the Heisenberg Hamiltonian.^{22,23} Solving the set of linear equations given in Table I results in the following magnetic interaction parameters: $J_{b,1} = 127.9$ K, $J_{b,2} = -5.5$ K, $J_{a,1} = 0.2$ K, $J_{a,2} = -0.7$ K, and $J_{c,1} = -0.2$ K. Although the numerical precision of the computational methods applied is better than 0.1 K, the smallness of the interchain interactions makes them less suitable to validate the cluster model. Nevertheless, the in-chain interactions are clearly larger and can be used to make a comparison with the results obtained from a local point of view. Hence we have used the three center cluster described in the previous section and calculated the UHF energies of the high-spin state [$\alpha(1)\alpha(2)\alpha(3)$, corresponding to a ferromagnetic alignment of the spins on the three copper ions], and two broken symmetry states [$\alpha(1)\alpha(2)\beta(3)$ and $\alpha(1)\beta(2)\alpha(3)$]. From the energy differences, we obtain $J_1 = 127.0$ K and $J_2 = -6.7$ K, in good agreement with the periodic calculations. This comparison validates the modelization of the crystal with an embedded cluster model to extract local electronic structure parameters with more sophisticated quantum chemical schemes than the UHF method used in the periodic calculations. This observation is not unique for Li₂CuO₂, and has been reported before for a large series of transition-metal oxides and fluorides.^{20,22,35,39-42}

The validation of the embedded-cluster model approach for the calculation of t cannot be achieved in the same way. Extremely large supercells are needed to obtain a realistic hole concentration to directly calculate the hopping integral in a periodic approach. There exist, however, some indirect support for the suitability of the cluster model approach to calculate t 's. In the first place the cluster model satisfactorily reproduces the generally accepted value of t for La₂CuO₄.²⁶ Moreover, the LDA hopping parameters of Sr₂CuO₃ and Ca₂CuO₃ obtained from the cluster model and deduced from periodic LDA calculations⁴³ are almost identical.²⁰

C. Magnetic interactions

The first cluster model, Cu₃O₈Li₆, allows us to calculate both $J_{b,1}$ and $J_{b,2}$. The ferromagnetic character of $J_{b,1}$ found with all three computational methods applied (cf. Table II) is in agreement with the Goodenough-Kanamori-Anderson (GKA) rules.¹³⁻¹⁵ Although the Cu-O-Cu angle is not strictly

TABLE II. Magnetic coupling parameters (in K) and hopping integrals (in meV) for Li_2CuO_2 . CASSCF represents the unscreened Anderson model, whereas CASPT2 and DDCI include external electron correlation effects. $J_{b,1}$ and $J_{b,2}$ parametrize the nearest- and next-nearest-neighbor in-chain magnetic interaction, respectively. $J_{a,1}$ stands for the interchain interaction along the a axis. $J_{c,1}$ and $J_{c,2}$ are the nearest- and next-nearest-neighbor interchain interactions along the c axis. For t , analogous nomenclature is applied. See also Figs. 2 and 3.

Method	$J_{b,1}$	$J_{b,2}$	$J_{a,1}$	$J_{c,1}$	$J_{c,2}$
CASSCF	45	-3	0.0	0.0	-0.4
CASPT2	150	-21	-10.2	-12.8	-13.9
DDCI	142	-22	-1.4	0.0	-3.6
	$t_{b,1}$	$t_{b,2}$	$t_{a,1}$	$t_{c,1}$	$t_{c,2}$
CASSCF	179	125	-9	28	-53
CASPT2	322	267	-12	67	-115
DDCI	143	120	-8	28	-52

90° , it is close enough to the ideal situation so that the ferromagnetic contribution to the Cu-Cu interaction is still dominant. To give a more firm basis to the ferromagnetic nature of $J_{b,1}$, we have investigated at what angle the antiferromagnetic contribution becomes dominant and the interaction changes sign. To this purpose, we have varied the Cu-O-Cu angle in a $\text{Cu}_2\text{O}_6\text{Li}_4$ cluster model maintaining the Cu-O distance fixed at the experimental value of 1.956 Å, all other cluster atoms and the embedding remained unchanged. The outcome of this computational experiment shows that the nearest-neighbor interaction reaches a maximum around 97° and remains ferromagnetic up to angles as large as 104° . For angles smaller than 90° , the interaction becomes antiferromagnetic around 80° . The structure is, however, very stressed at these small angles and the results might be affected by this stress. Nevertheless, the results show that the experimental Cu-O-Cu angle of 94° lies in the middle of the ferromagnetic range and hence the suggestion of an antiferromagnetic nearest-neighbor interaction is not supported.

Comparing the results of the three different computational schemes, we observe the usual behavior. The (almost) uncorrelated CASSCF wave function reproduces the correct sign but the inclusion of the important electron correlation effects by CASPT2 or DDCI largely enhances the interaction. The final result ($J_{b,1} = 142$ K) is of the same order of magnitude as that derived from the three band model Hamiltonian ($J_{b,1} = 100$ K),^{8,9} but much larger (and of opposite sign) than the one obtained from the fitting of the spin-wave dispersions ($J_{b,1} = -2.8$ K).²

The next-nearest-neighbor in-chain interaction, derived from the same $\text{Cu}_3\text{O}_8\text{Li}_6$ cluster, is antiferromagnetic in nature and hence introduces a frustration in the spin chain. The calculated absolute magnitude of the interaction is, however, much smaller than the predictions mentioned in the Introduction. For the CASSCF wave function, $J_{b,2}$ is about 5% of $J_{b,1}$ and can be considered negligible. On the other hand, the explicitly correlated wave functions significantly increase $J_{b,2}$ and our final estimate corresponds to -22 K and a ratio

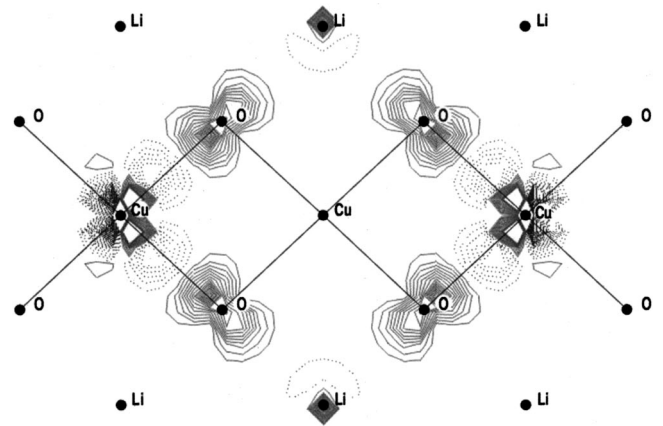


FIG. 4. Changes in the CASSCF spin density on the addition of the Li ions to the quantum cluster region. Solid contours indicate a decrease of the spin density, whereas the dotted contours enclose areas of increasing spin density.

$J_{b,2}/J_{b,1} = -0.15$. It is interesting to note that the Li ions play an important role in the ratio between $J_{b,1}$ and $J_{b,2}$. When the six lithium ions are removed from the quantum cluster region and represented as bare point charges, $J_{b,2}$ increases dramatically and becomes as large as -102 K. $J_{b,1}$ is much less affected by the removal of the lithium ions and is reduced to 123 K, leading to $J_{b,2}/J_{b,1} = -0.83$. The large change observed for $J_{b,2}$ indicates that the magnetic interaction path (Cu-O-O-Cu) for this interaction is obstructed when the Li ions around the cluster are represented by real charge distributions instead of point charges. Figure 4 represents the changes in the spin density when Li ions are removed from the quantum cluster region. It clearly illustrates how the introduction of the short-range repulsion between the Li ions and the oxygens on the $J_{b,2}$ magnetic path significantly reduces the spin density along this path to increase it on the Cu ions. Hence the overlap between the two oxygens decreases and the two copper ions involved in this magnetic interaction are disconnected magnetically.

We now turn to the interchain interactions. The magnetic pathway for these interactions is rather long and complicated (see Figs. 2 and 3) and therefore normally result in weak interactions, but they are fundamental to understand the three-dimensional magnetic structure of the crystal. The first conclusion that can be drawn from Table II is that the second-order perturbative treatment of the correlation effects is not precise enough for these very small energy differences. The CASPT2 results are much larger than those calculated with the variational DDCI method and result in too high a Néel temperature ($T_N \sim 28$ K) when the values are inserted in the mean-field expression for T_N of quasi-1D spin chains proposed by Schulz.⁴⁴ On the other hand, the DDCI values result in a T_N around 7 K, much closer to the experimental value of 9 K.^{1,45,46} Nevertheless, these values have to be taken with caution. In the first place, there is the uncertainty inherent to the mean-field character of the expression,⁴⁷⁻⁴⁹ and secondly, the five calculated interaction parameters must be converted into one effective in-chain parameter J_{\parallel} and one effective interchain parameter J_{\perp} . Because T_N is not very

sensitive to J_{\parallel} —at least not in the expression of Schulz— $J_{b,2}$ can either be neglected or the relation $J_{\parallel} = J_{b,1} - rJ_{b,2}$ can be applied with $r = 1$ or $r = 1.12$.^{43,50,51} For the interchain interaction, we follow the strategy previously adopted by other authors,^{43,52} which consists in taking the average of the interactions perpendicular to the chain as the effective J_{\perp} . For CASPT2, we have used $J_{\perp} = [J_{a,1} + 1/2(J_{c,1} + J_{c,2})]/2 = -11.8$ K, and for DDCI, $J_{\perp} = (J_{a,1} + J_{c,1})/2 = -2.5$ K.

In the second place, the DDCI results confirm the assumption of Mizuno *et al.* about the importance of the second-neighbor interchain interaction.⁹ We obtain, however, a slightly different picture of the interchain interaction along the c axis. Where Mizuno *et al.* assumed that $J_{c,1}$ and $J_{c,2}$ are equal and can be written directly as one effective J_c , Table II shows that $J_{c,1}$ is practically zero and $J_{c,2}$ is much larger. In addition, we could determine the strength of the interaction along the a axis, which is approximately half of $J_{c,2}$. We have also investigated the size of $J_{a,2}$, but this interaction turns out to be practically zero with all three computational schemes applied in this work. Therefore no further reference to this interaction will be made. The relative size of the interaction along the body diagonal ($J_{c,2}$) and in the a - b planes ($J_{a,1}$)—both antiferromagnetic in nature—is not incompatible with the experimental magnetic structure, as AFM alignment of the spin chains along the body diagonal is preferred to AFM alignment in the a - b planes.

D. Hopping parameters

The second set of calculations are devoted to the accurate determination of the different t 's, which parametrize the dynamics of the holes when the system is doped. The fact that the CuO_4 plaquettes are edge sharing has a large effect on the nearest-neighbor effective hopping parameter $t_{b,1}$. Whereas a typical value of this parameter in corner sharing cuprates is around 500 meV, it is more than three times smaller in Li_2CuO_2 ; see Table II. On the other hand, $t_{b,2}$ is of the same order of magnitude as $t_{b,1}$ and almost three times larger than the corresponding t in corner sharing cuprates,²⁶ namely the hopping integral between two copper ions separated by a linear $-\text{O}-\text{Cu}-\text{O}-$ interaction path. The interchain hopping parameters are smaller in magnitude, but not negligible relative to the in-chain parameters. As for the magnetic coupling, we observe that $t_{c,1}$ is significantly smaller than $t_{c,2}$, although the distance between the copper ion is larger for the latter process (5.2 versus 6.6 Å). On the contrary, the in-chain hopping parameters are rather similar, unlike the magnetic interactions for which $J_{b,2}$ is only a small fraction of $J_{b,1}$. This seems to indicate that the simple superexchange relation $J = 4t^2/U$ cannot be applied for Li_2CuO_2 . Whereas the DDCI parameters substituted in $U = 4t_{b,1}^2/J_{b,1}$ result in a reasonable on-site repulsion parameter of 6.7 eV, the same procedure for the next-nearest-neighbor interaction DDCI parameters lead to an unphysical $U = 26$ eV.

The comparison of the three computational methods applied in this study shows that the CASSCF and DDCI values nearly coincide, whereas the CASPT2 values are significantly larger. The first observation is in agreement with the

understanding that the hopping process is basically a one-electron property and therefore not strongly influenced by electron correlation effects. Test calculations in which we only diagonalize a subset of the full DDCI matrix give similar values and confirm the insensitivity of t to electron correlation effects. This also explains the similar values predicted with LDA. The second observation indicates that the CASPT2 method is not the best choice to obtain accurate t 's. The method also overestimates the hopping parameter for corner sharing cuprates, ~ 800 meV instead of the usual 500 meV. Nevertheless, CASPT2 perfectly reproduces the trends in the hopping parameters obtained at the more accurate DDCI level. Therefore it can be perfectly used to explore the basis set and cluster size dependency of the electronic structure parameters presented in Sec. II F.

E. Magnetic moments

The Mulliken spin populations provide a way to extract an estimate of the magnetic moment of the different centers from our cluster calculations. The populations of the CASSCF wave function corresponding to the ferromagnetic solution indicate that a very large part of the magnetic moment is concentrated on the Cu ions. In all clusters, we found that the Mulliken spin population of Cu is 0.93, and ~ 0.03 for oxygen. Nevertheless, the CASSCF wave function includes only a small amount of electron correlation and more accurate spin populations are needed. Recent work on magnetic moments in molecules learns that DDCI spin populations compare fairly well to experimental results.⁵³ For Li_2CuO_2 , we obtain the following DDCI spin populations: 0.76 for copper and 0.12 for oxygen, the spin density on Li is essentially zero. These values are almost independent of the cluster model and the basis set applied. The treatment of the electron correlation effects with DDCI leads to a more delocalized character of the unpaired electrons compared to the CASSCF result, although it does not become as delocalized as found in the LDA calculations.

To give further support to these cluster model results, we have determined the magnetic moments from periodic calculations applying different computational schemes (see the Appendix for computational details). In the first place, there is the already mentioned UHF calculation, which predicts the magnetic moments in excellent agreement with the CASSCF cluster results: 0.90 for Cu and 0.05 for O. Second, we performed LDA periodic and cluster calculations. As expected, the periodic LDA calculations give similar results as those previously reported:⁴ the spin populations are 0.53 and 0.20 for Cu and O, respectively. These results are accurately reproduced with the LDA cluster model calculation: 0.51 and 0.22 for Cu and O, respectively. Finally, we applied the hybrid Becke-3-Lee-Yang-Parr (B3LYP) functional, a gradient corrected functional which has 20% Fock exchange and uses the Lee-Yang-Parr expression for the correlation functional.⁵⁴ This functional is one of the most successful functionals in molecular quantum chemistry and has been claimed to reproduce spin densities with reasonable accuracy, although it has the tendency to slightly overestimate the spin density on the bridging ligand.^{55,56} Whereas the UHF

TABLE III. Basis set dependency of the magnetic interaction parameter $J_{b,1}$ (in K) and the hopping parameter $t_{b,1}$ (in meV) for Li_2CuO_2 calculated with an embedded $\text{Cu}_2\text{O}_6\text{Li}_4$ cluster. Basis A consists of the Cu ($5s$, $4p$, $3d$) basis, the bridging O ($4s$, $3p$) basis, the edge O ($3s$, $2p$) basis and a Li ($2s$) basis. Basis B augments the edge O basis to ($4s$, $3p$). Basis C augments B with a d function on all O but treats the Li ions at the frozen ion level. Basis D only differs from C in the treatment of the Li ions, namely by a ($3s$, $1p$) basis. Basis E consists of a ($6s$, $5p$, $4d$, $1f$) basis for Cu, a ($5s$, $4p$, $2d$) basis for O and a ($3s$, $1p$) basis for Li.

	$J_{b,1}$		$t_{b,1}$	
	CASSCF	CASPT2	CASSCF	CASPT2
Basis A	44	147	180	320
Basis B	45	150	179	322
Basis C	46	159	165	316
Basis D	45	150	164	330
Basis E	44	147	160	356

band gap is unphysically large (16.3 eV) and LDA results in too small a band gap (~ 0.1 eV), the periodic B3LYP calculations give a much more realistic band gap of 2.3 eV, in reasonable agreement with the theoretical estimate reported in the literature.⁸ The B3LYP spin densities are 0.65 for copper and 0.17 for oxygen, interpolate between the LDA and UHF results.

Considering the B3LYP values as an upper limit for the oxygen spin density and lower limit for the copper spin density, the results are in good agreement with the DDCI results. We must caution that the way in which the overlap population is divided over the centers—Mulliken population analysis distributes it on equal parts over the two centers involved—is somewhat arbitrary. Nevertheless, it is clear that our results situate the magnetic moments somewhere between the completely localized picture assumed in early experimental work and the more delocalized interpretation based on LDA calculations.

F. Cluster size and basis set effects

The validation of the calculated electronic structure parameters is continued with a check on the dependence of the J 's and t 's on the one-electron basis set size. In Table III, we report $J_{b,1}$ and $t_{b,1}$ calculated in the $\text{Cu}_2\text{O}_6\text{Li}_4$ cluster applying five basis sets of different quality. In this series we investigate the effect of a frozen ion description of Li, and the effect of polarization functions on the cluster atoms. The largest basis set considered consists of a ($6s$, $5p$, $4d$, $1f$) basis for Cu, ($5s$, $4p$, $2d$) for O, and ($3s$, $1p$) for Li.

The comparison of basis A, B, D, and E shows that the values listed in Table III are converged for the size of the basis set. Adding polarization functions and/or any further extension of the basis set on the cluster ions does not induce significant changes in any of the calculated values. Furthermore, basis C and D allow us to investigate the role of the Li ions, since these basis sets are equivalent except for the description of the Li ions, the former being as frozen ions not allowing for any covalent interaction with the oxygens. We

TABLE IV. Cluster size dependency of the CASPT2 in-chain magnetic coupling parameters $J_{b,1}$ and $J_{b,2}$ (in K), and the in-chain hopping integrals $t_{b,1}$ and $t_{b,2}$ (in meV). All clusters are embedded in two Cu^{2+} TIP's and point charges.

Cluster	$J_{b,1}$	$J_{b,2}$	$t_{b,1}$	$t_{b,2}$
Cu_2O_6	132		329	
$\text{Cu}_2\text{O}_6\text{Li}_4$	150		330	
$\text{Cu}_2\text{O}_6\text{Li}_{20}$	153		320	
$\text{Cu}_2\text{O}_6\text{Li}_{20}\text{O}_{16}$	156		316	
Cu_2O_8		-93		486
$\text{Cu}_2\text{O}_8\text{Li}_6$		-37		278
$\text{Cu}_2\text{O}_8\text{Li}_{26}$		-30		295
$\text{Cu}_2\text{O}_8\text{Li}_{26}\text{O}_{12}$		-33		230
Cu_3O_8	138	-99		
$\text{Cu}_3\text{O}_8\text{Li}_6$	153	-22		
$\text{Cu}_3\text{O}_8\text{Li}_{10}$	154	-22		
$\text{Cu}_3\text{O}_8\text{Li}_{26}$	167	-27		
$\text{Cu}_3\text{O}_8\text{Li}_{26}\text{O}_{12}$	163	-25		

conclude that a frozen ion description of the Li ions does not seriously affect the magnitude of the magnetic coupling parameters and that the role of the Li ions is (although essential) completely static.

The comparison between periodic and cluster model calculations reported in Sec. II B have shown that the cluster model provides a valid description of the material to derive a microscopic electronic structure parameter. An additional check of the validity of the cluster model can be found in Table IV, where we report the effect of the cluster size on the properties under study. Starting from the $\text{Cu}_2\text{O}_6\text{Li}_4$ cluster used to extract $J_{b,1}$ and $t_{b,1}$, successively more shells are added. The same strategy is applied for the two-center cluster to study the convergence of the second-neighbor interactions and the three-center cluster for the simultaneous determination of $J_{b,1}$ and $J_{b,2}$. The largest cluster we consider is $\text{Cu}_2\text{O}_6\text{Li}_{20}\text{O}_{16}\text{Cu}_2$ (the two extra Cu ions are represented by TIP's) for the two-center cluster and $\text{Cu}_x\text{O}_8\text{Li}_{26}\text{O}_{12}\text{Cu}_2$ ($x=2,3$) in the second series. Table IV lists the effects of the increase in the cluster size on the magnetic coupling parameters using basis D for the central cluster atoms ($\text{Cu}_2\text{O}_6\text{Li}_4$ and $\text{Cu}_3\text{O}_8\text{Li}_6$), and ($3s$, $2p$) and ($2s$) for the other O and Li ions, respectively.

It is readily recognized that the cluster size effect is small, $J_{b,1}$ and $J_{b,2}$ do not significantly depend on the cluster size, provided that the Li ions in the $J_{b,2}$ magnetic pathway are included. Similar considerations apply for the hopping parameters $t_{b,1}$ and $t_{b,2}$. In addition, it can be observed that $J_{b,1}$ derived from the two center cluster is virtually identical to that derived from the three center clusters. Finally, Table IV validates the use of two center clusters to calculate next-nearest-neighbor interactions. Comparing Cu_2O_8 with Cu_3O_8 , $\text{Cu}_2\text{O}_8\text{Li}_6$ with $\text{Cu}_3\text{O}_8\text{Li}_6$, and so forth, we observe that $J_{b,2}$ is practically identical in both series and that the representation of the central copper by a point charge does not affect the calculated value of $J_{b,2}$. It is assumed that the same applies for $t_{b,2}$.

III. MONTE CARLO SIMULATIONS

The objectives of our Monte Carlo simulations are two-fold. In the first place, we determine the Néel temperature T_N for AFM ordering between the FM chains using the *ab initio* magnetic coupling parameters derived in the previous section. Second, we study the dependency of the interchain interactions and the ratio $J_{b,2}/J_{b,1}$ on T_N .

A. Definition of the model

In order to reproduce the crystallographic structure of the material and the magnetic interactions between the atoms, we have divided the lattice into two sublattices, each formed by next-nearest-neighboring *a-b* planes. This allows us to separate the contribution of Cu chains to the equilibrium properties from that of the whole system. Therefore inter-plane interactions are represented by interactions between *A* and *B* sublattices. Experimental results^{45,57,58} show that there is a strong uniaxial anisotropy along the *a* axis and therefore we have represented the Cu ions by Ising spins $S_{i,j,k}^\alpha = \pm \frac{1}{2}$, where α labels the sublattices *A* and *B* and *i, j, k* represent the vector coordinates in each sublattice. Taking into account the above-mentioned comments, the effective spin-model Hamiltonian used in the simulations can be written as

$$\hat{H} = -S^2 \sum_{\alpha=A,B} \sum_{i,j,k=1}^N S_{i,j,k}^\alpha [J_{b,1} S_{i,(j+1),k}^\alpha + J_{b,2} S_{i,(j+2),k}^\alpha + J_{a,1} S_{(i+1),j,k}^\alpha + J_{c,2} S_{i,j,(k+1)}^{\alpha+1}],$$

where N is the number of unit cells considered in the simulation and $J_{c,1}$, being essentially zero, has been omitted. Moreover, since the *ab initio* calculations indicate that the interchain interactions along the *a* axis and the *c* axis are of the same order, we set $J_\perp = (J_{a,1} + J_{c,2})/2$. This reduces the number of parameters in the simulations to 2, namely $J_{b,2}/J_{b,1}$ and $J_\perp/J_{b,1}$.

With this spin Hamiltonian at hand, we have studied several thermodynamic equilibrium quantities through Monte Carlo (MC) simulations. MC techniques have been proven to be very useful for the study of magnetic phase transitions and nature of magnetic order in a wide range of solid-state compounds.⁵⁹ It has the advantage that it allows us to follow many of the experimentally measured quantities as a function of the temperature or external magnetic fields while keeping track of the microscopic spin configuration not directly accessible by commonly used experimental techniques. In particular, Ising spin lattices with competing ferromagnetic and antiferromagnetic interactions⁶⁰ or topologically frustrated lattices⁶¹ have been the object of recent simulation studies aiming at the elucidation of the phase diagram of the different possible magnetic order.

We have used periodic boundary conditions and treated systems with linear size up to $N=20$ in order to minimize the finite-size effects on the thermodynamical properties. The procedure followed in the MC simulation is the so-called simulated thermal annealing method.^{62,63} This method starts with a random spin configuration at very high temperature, which is slowly decreased by a constant factor δT . We start

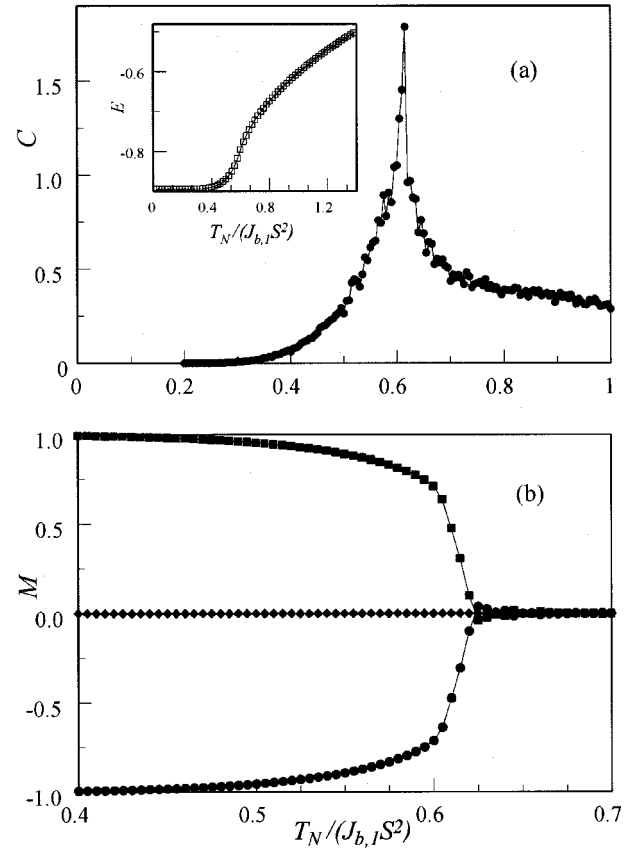


FIG. 5. (a) Thermal variation of the specific heat C as obtained from MC simulation applying the *ab initio* calculated J 's. The position of the peak in C marks the Néel temperature \bar{T}_N for antiferromagnetic ordering. Inset: thermal dependence of the magnetic energy E . (b) Thermal variation of sublattice magnetizations M_A and M_B , and total magnetization of the system M_{Total} . $M_\alpha = \pm 1$ corresponds to complete FM order along the chains.

at a dimensionless temperature \bar{T} of 4 ($\bar{T} = T/J_{b,1}S^2$) and use a reduction factor of -0.005 . At each temperature step, the system is brought to thermal equilibrium by evolving the system during a large number of MC steps, normally between 2000 and 5000. The quantities measured after each MC step are the energy E , the specific heat C , the sublattice magnetizations M_A and M_B , and the total magnetization M_{Total} .

B. Simulation results

Figure 5(a) and inset present the thermal variation of the specific heat C and the energy E during a thermal annealing process for the magnetic coupling parameters derived in Sec. II C. Setting $J_{b,1} = 1$, ferromagnetic in nature, the simulation parameters are $J_{b,2}/J_{b,1} = -1.549 \times 10^{-1}$ and $J_\perp/J_{b,1} = -1.761 \times 10^{-2}$. The sharp peak in C at $\bar{T}_N = 0.61 \pm 0.1$ signals a transition from a paramagnetic phase to antiferromagnetic ordering of the spins. Converting \bar{T}_N in physical units, we obtain $T_N = 10.8 \pm 0.2$ K in good agreement with the experimental value of 9.4 K.^{1,45,46} The calculated T_N is stable against a further increase of the system size; no sig-

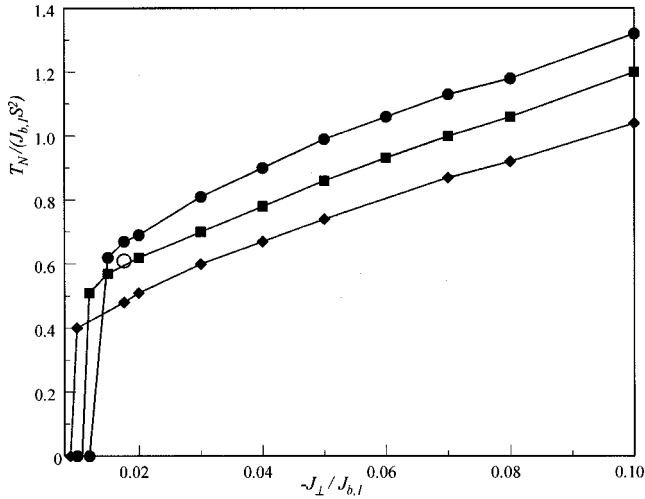


FIG. 6. Dimensionless Néel temperature \bar{T}_N as function of the ratio $J_{\perp}/J_{b,1}$ for three $J_{b,2}$ to $J_{b,1}$ ratios. Circles correspond to $J_{b,2}/J_{b,1} = -8.000 \times 10^{-2}$, squares to $J_{b,2}/J_{b,1} = -1.549 \times 10^{-1}$, and triangles give $J_{b,2}/J_{b,1} = -2.500 \times 10^{-1}$. \bar{T}_N corresponding to the *ab initio* values derived in Sec. II C is marked by an empty circle.

nificant changes have been observed for $N > 10$. The nature of the low-temperature phase can be understood by looking at the thermal variation of the magnetizations in Fig. 5(b). The sublattice magnetizations M_{α} ($\alpha = A, B$) acquire non-zero values at T_N that rapidly saturate to ± 1 at lower T . This observation clearly shows that ferromagnetic order in the chains sets in at T_N , while the different signs of M_A and M_B indicate that these chains are antiferromagnetically ordered along the c axis. This is completely in agreement with the magnetic structure proposed by Sapiña and co-workers.¹

To study the effect of the second-neighbor in-chain and interchain magnetic interaction parameters on T_N , we have run simulations varying the $J_{\perp}/J_{b,1}$ ratio from 0 to 0.10 for three different $J_{b,2}/J_{b,1}$ ratios: -8.000×10^{-2} , -1.549×10^{-1} , and -2.500×10^{-1} . The results are given in Fig. 6. In the first place, we observe that T_N vanishes below a certain value of $J_{\perp}/J_{b,1}$, indicating that a finite value of the interchain interaction is necessary to induce AFM order. As expected from the AFM nature of the interchain interactions, T_N increases with increasing interchain interaction. On the other hand, the increase in $J_{b,2}$ results in a decrease of the Néel temperature because of the increasing frustration in the spin chain.

IV. SUMMARY AND CONCLUSIONS

An extended t - J Hamiltonian of the quasi-1D spin chain compound Li_2CuO_2 has been parametrized by means of state-of-the-art *ab initio* quantum chemistry calculations. We have established the ferromagnetic nature of the first-neighbor in-chain magnetic interaction (142 K), and observed that the second-neighbor in-chain magnetic interaction is antiferromagnetic in nature and about 15% of the first-neighbor interaction. These results indicate that the frustration in the spin chain is significantly smaller than sug-

gested by other authors. At first sight this could be incompatible with the small T_N observed for Li_2CuO_2 and a way to assess the 3D magnetic structure of the compound (more specifically, T_N) was opened by completing the model Hamiltonian with interchain interactions. These antiferromagnetic interactions are weak (-3.6 K for the interaction along the c axis and -1.4 along the a axis) and suggest a very low AFM ordering temperature T_N . The hopping parameters show a very similar pattern, with the exception of the ratio between the first- and second-neighbor in-chain hopping parameters, which is much larger than the ratio of the corresponding magnetic interactions.

The validity of the parameters has been checked with three different approaches. In the first place we compare our cluster model results with band-structure calculations carried out at the same level of electronic structure theory. The comparison at the UHF level shows that the magnetic interactions parameters are essentially identical in the two representations of the model, e.g., the $J_{b,2}/J_{b,1}$ ratio obtained in the periodic UHF calculations is 0.04, in very good agreement with the UHF cluster model result. This validates our representation of the material with a finite cluster model. In the second place, we study the cluster size and basis set dependency of the electronic structure parameters. Neither for the cluster size nor for the basis set do we observe significant changes, once a reasonable choice has been made. Finally, and most importantly, we use our *ab initio* parameters to define an effective spin Hamiltonian that permits us to perform Monte Carlo simulations of the magnetic system. The resulting Néel temperature of 10.8 K is in good agreement with the experimental value, showing that a small $J_{b,2}/J_{b,1}$ ratio does not necessarily lead to high ordering temperatures. Moreover, the Monte Carlo simulations suggest that the system is rather close to a situation for which three-dimensional magnetic ordering no longer occurs.

ACKNOWLEDGMENTS

Financial support was provided by the “Comisión Interministerial de Ciencia y Tecnología” under CICYT Project No. PB98-1216-CO2-01, by SEEUID through Project No. MAT2000-0858, and by the “Generalitat de Catalunya” under Project Nos. 2000SGR00025 and 2001SGR00043. We acknowledge CESCA and CEPBA under coordination of C⁴ for the computer facilities. I. de P. R. M. thanks the European Community for a Marie Curie postdoctoral Fellowship under Project No. HPMF-CT-2000-00812.

APPENDIX

The results listed in Table II have been obtained using one-electron basis sets of the atomic natural orbital type. The Cu basis set is a general contraction of the (21s, 15p, 10d) primitive set to [5s, 4p, 3d] Gaussian-type functions. We use a (14s, 9p)/(4s, 3p) basis set for O and a (14s)/(2s) basis set for Li.^{64,65} This corresponds to basis B in Table III and results in 212 basis functions for the $\text{Cu}_3\text{O}_8\text{Li}_6$ cluster model. Both in the DDCI and the CASPT2 calculations, the deep-core electrons (Cu 1s², 2s², 2p⁶, and O 1s²) were

kept frozen. The DDCI and CASSCF/CASPT2 calculations have been performed with the CASDI and MOLCAS 5.2 codes,^{66,67} respectively. The LDA and UHF cluster model calculations have been performed with the GAUSSIAN98 program,⁶⁸ applying the following segmented basis sets: 6-3111+*G* for Cu, 6-31*G** for O and STO-3*G* for Li. The DDCI calculations have been performed with a molecular-orbital basis optimized for the spin state with maximum spin multiplicity, triplet and quartet for the two- and three-center clusters, respectively.

The CRYSTAL98 program⁶⁹ has been used for all periodic electronic structure calculations reported here. Standard basis sets have been used in the periodic calculations,⁷⁰ i.e.,

(20*s*, 12*p*, 5*d*)/[5*s*, 4*p*, 2*d*] for Cu, (14*s*, 6*p*)/[4*s*, 3*p*] for O, and (7*s*, 1*p*)/(2*s*, 1*p*) for Li, where a segmented contraction scheme is applied. The cutoff parameters for the Coulomb and exchange integral evaluation (ITOL 1-5 of the CRYSTAL98 code) have been set to 7, 7, 7, 7, 14. The *k*-space grid parameter is 6 for the double supercells and 4 for the triple supercells, yielding 67 and 27 *k* points in the first irreducible Brillouin zone, respectively. This parameter choice is taken from previous applications^{20,35,39} and results in an energy difference per cell smaller than 10⁻⁶ hartree for the FM alignment in the single and triple unit cells and even better for the difference between single and double unit cells.

*Author to whom correspondence should be addressed. Electronic address: coen@correu.urv.es

¹F. Sapiña, J. Rodríguez-Carvajal, M. J. Sanchis, R. Ibáñez, A. Beltrán, and D. Beltrán, *Solid State Commun.* **74**, 779 (1990).

²M. Boehm, S. Coad, B. Roessli, A. Zheludev, M. Zolliker, P. Böni, D. M. Paul, H. Eisaki, N. Motoyama, and S. Uchida, *Europhys. Lett.* **43**, 77 (1998).

³R. Neudert, H. Rosner, S.-L. Drechsler, M. Kielwein, M. Sing, Z. Hu, M. Knupfer, M. S. Golden, J. Fink, N. Nücker, M. Merz, S. Schuppler, N. Motoyama, H. Eisaki, S. Uchida, M. Domke, and G. Kaindl, *Phys. Rev. B* **60**, 13 413 (1999).

⁴R. Weht and W. E. Pickett, *Phys. Rev. Lett.* **81**, 2502 (1998).

⁵H. Rosner, R. Hayn, and S.-L. Drechsler, *Physica B* **259–261**, 1001 (1999).

⁶N. Tanaka, M. Suzuki, and K. Motizuki, *J. Phys. Soc. Jpn.* **68**, 1684 (1999).

⁷N. Tanaka, M. Suzuki, and K. Motizuki, *Physica B* **284–288**, 1388 (2000).

⁸Y. Mizuno, T. Tohyama, S. Maekawa, T. Osafune, N. Motoyama, H. Eisaki, and S. Uchida, *Phys. Rev. B* **57**, 5326 (1998).

⁹Y. Mizuno, T. Tohyama, and S. Maekawa, *Phys. Rev. B* **60**, 6230 (1999).

¹⁰C. de Graaf, I. de P. R. Moreira, and F. Illas, *Int. J. Mol. Sci.* **1**, 28 (2000).

¹¹I. de P. R. Moreira, F. Illas, C. J. Calzado, J. F. Sanz, J.-P. Malrieu, N. Ben Amor, and D. Maynau, *Phys. Rev. B* **59**, 6593 (1999).

¹²D. Muñoz, F. Illas, and I. de P. R. Moreira, *Phys. Rev. Lett.* **84**, 1579 (2000).

¹³J. B. Goodenough, *Phys. Rev.* **100**, 564 (1955).

¹⁴J. Kanamori, *J. Phys. Chem. Solids* **10**, 87 (1959).

¹⁵P. W. Anderson, *Theory of Magnetic Exchange Interaction: Exchange in Insulators and Semiconductors*, *Solid State Physics* Vol. 14 (Academic, New York, 1963).

¹⁶F. Illas, J. Casanovas, M. A. Garcia-Bach, R. Caballol, and O. Castell, *Phys. Rev. Lett.* **71**, 3549 (1993).

¹⁷J. Casanovas, J. Rubio, and F. Illas, *Phys. Rev. B* **53**, 945 (1996).

¹⁸C. de Graaf, R. Broer, and W. C. Nieuwpoort, *Chem. Phys. Lett.* **271**, 372 (1997).

¹⁹C. Wang, K. Fink, and V. Staemmler, *Chem. Phys.* **192**, 25 (1995).

²⁰C. de Graaf and F. Illas, *Phys. Rev. B* **63**, 014404 (2001).

²¹C. de Graaf, C. Sousa, I. de P. R. Moreira, and F. Illas, *J. Phys. Chem. A* **105**, 11 371 (2001).

²²I. de P. R. Moreira and F. Illas, *Phys. Rev. B* **55**, 4129 (1997).

²³F. Illas, I. de P. R. Moreira, C. de Graaf, and V. Barone, *Theor. Chem. Acc.* **104**, 265 (2000).

²⁴A. B. van Oosten, R. Broer, and W. C. Nieuwpoort, *Chem. Phys. Lett.* **257**, 207 (1996).

²⁵N. W. Winter, R. M. Pitzer, and D. K. Temple, *J. Chem. Phys.* **86**, 3549 (1987).

²⁶C. J. Calzado and J.-P. Malrieu, *Phys. Rev. B* **63**, 214520 (2001).

²⁷C. J. Calzado, J. F. Sanz, and J.-P. Malrieu, *J. Chem. Phys.* **112**, 5158 (2000).

²⁸J. F. Sanz and J.-P. Malrieu, *J. Phys. Chem.* **97**, 99 (1993).

²⁹E. Sinn, *Coord. Chem. Rev.* **5**, 313 (1970).

³⁰J. Miralles, J.-P. Daudey, and R. Caballol, *Chem. Phys. Lett.* **198**, 555 (1992).

³¹J. Miralles, O. Castell, R. Caballol, and J.-P. Malrieu, *Chem. Phys.* **172**, 33 (1993).

³²V. M. García, O. Castell, R. Caballol, and J.-P. Malrieu, *Chem. Phys. Lett.* **238**, 222 (1995).

³³K. Andersson, P.-Å. Malmqvist, B. O. Roos, A. J. Sadlej, and K. Wolinski, *J. Phys. Chem.* **94**, 5483 (1990).

³⁴K. Andersson, P.-Å. Malmqvist, and B. O. Roos, *J. Chem. Phys.* **96**, 1218 (1992).

³⁵J. M. Ricart, R. Dovesi, C. Roetti, and V. R. Saunders, *Phys. Rev. B* **52**, 2381 (1995).

³⁶M. D. Towler, N. L. Allan, N. M. Harrison, V. R. Saunders, W. C. Mackrodt, and E. Aprà, *Phys. Rev. B* **50**, 5041 (1994).

³⁷L. Noodleman and J. G. Norman, Jr., *J. Chem. Phys.* **70**, 4903 (1979).

³⁸L. Noodleman and E. R. Davidson, *Chem. Phys.* **109**, 131 (1986).

³⁹Y.-S. Su, T. A. Kaplan, S. D. Mahanti, and J. F. Harrison, *Phys. Rev. B* **59**, 10 521 (1999).

⁴⁰P. Reinhardt, M. P. Habas, R. Dovesi, I. de P. R. Moreira, and F. Illas, *Phys. Rev. B* **59**, 1016 (1999).

⁴¹P. Reinhardt, I. de P. R. Moreira, C. de Graaf, R. Dovesi, and F. Illas, *Chem. Phys. Lett.* **319**, 625 (2000).

⁴²I. de P. R. Moreira and F. Illas, *Phys. Rev. B* **60**, 5179 (1999).

⁴³H. Rosner, H. Eschrig, R. Hayn, S.-L. Drechsler, and J. Málek, *Phys. Rev. B* **56**, 3402 (1997).

⁴⁴H. J. Schulz, *Phys. Rev. Lett.* **77**, 2790 (1996).

⁴⁵K. Okuda, S. Noguchi, K. Konishi, H. Deguchi, and K. Takeda, *J. Magn. Magn. Mater.* **104–107**, 817 (1992).

⁴⁶S. Ebisu, T. Komatsu, N. Wada, T. Hashiguchi, P. Kichambare, and S. Nagata, *J. Phys. Chem. Solids* **59**, 1407 (1998).

⁴⁷S. G. Chung and Y. C. Chang, *J. Phys. A* **20**, 2875 (1987).

⁴⁸V. Y. Irkhin and A. A. Katanin, *Phys. Rev. B* **61**, 6757 (2000).

- ⁴⁹A. W. Sandvik, Phys. Rev. Lett. **83**, 3069 (1999).
- ⁵⁰A. Fledderjohann and C. Gros, Europhys. Lett. **37**, 189 (1997).
- ⁵¹D. Gottlieb, M. Lagos, K. Hallberg, and C. Balseiro, Phys. Rev. B **43**, 13 668 (1991).
- ⁵²A. B. van Oosten and F. Mila, Chem. Phys. Lett. **295**, 359 (1998).
- ⁵³J. Cabrero and R. Caballol (unpublished).
- ⁵⁴A. D. Becke, J. Chem. Phys. **98**, 5648 (1993).
- ⁵⁵E. Ruiz, J. Cano, S. Alvarez, and P. Alemany, J. Am. Chem. Soc. **120**, 11122 (1998).
- ⁵⁶C. Blanchet-Boiteux and J.-M. Mouesca, J. Am. Chem. Soc. **122**, 861 (2000).
- ⁵⁷H. Ohta, N. Yamauchi, T. Nanba, M. Motokawa, S. Kawamata, and K. Okuda, J. Phys. Soc. Jpn. **62**, 785 (1993).
- ⁵⁸R. J. Ortega, P. J. Jensen, K. V. Rao, F. Sapiña, D. Beltrán, Z. Iqbal, J. C. Cooley, and J. L. Smith, J. Appl. Phys. **83**, 6542 (1998).
- ⁵⁹K. Binder and D. W. Heermann, *Monte Carlo Methods in Statistical Physics*, Springer Series in Solid State Sciences Vol. 80 (Springer-Verlag, Berlin, 1988).
- ⁶⁰O. Iglesias and A. Labarta, Phys. Rev. B **63**, 184416 (2001).
- ⁶¹S. T. Bramwell and M.-P. Gingras, Science **294**, 1495 (2001).
- ⁶²O. Iglesias and A. Labarta, J. Magn. Magn. Mater. **221**, 149 (2000).
- ⁶³S. Kirpatrick, D. C. Gellat, and M. P. Vecchi, Science **220**, 671 (1983).
- ⁶⁴R. Pou-Amérigo, M. Merchán, I. Nebot-Gil, P.-O. Widmark, and B. O. Roos, Theor. Chim. Acta **92**, 149 (1995).
- ⁶⁵P.-O. Widmark, P.-Å. Malmqvist, and B. O. Roos, Theor. Chim. Acta **77**, 291 (1990).
- ⁶⁶D. Maynau and N. Ben Amor, CASDI suite of programs, Université Paul Sabatier, Toulouse, 1997.
- ⁶⁷K. Andersson, M. Barysz, A. Bernhardsson, M. R. A. Blomberg, D. L. Cooper, T. Fleig, M. P. Fülscher, C. de Graaf, B. A. Hess, G. Karlström, R. Lindh, P.-Å. Malmqvist, P. Neogrády, J. Olsen, B. O. Roos, B. Schimmelpfennig, M. Schütz, L. Seijo, L. Serrano-Andrés, P. E. M. Siegbahn, J. Ståhring, T. Thorsteinsson, V. Veryazov, and P.-O. Widmark, MOLCAS Version 5, Lund University, Sweden, 2000.
- ⁶⁸M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, V. G. Zakrzewski, J. A. Montgomery, Jr., R. E. Stratmann, J. C. Burant, S. Dapprich, J. M. Millam, A. D. Daniels, K. N. Kudin, M. C. Strain, O. Farkas, J. Tomasi, V. Barone, M. Cossi, R. Cammi, B. Mennucci, C. Pomelli, C. Adamo, S. Clifford, J. Ochterski, G. A. Petersson, P. Y. Ayala, Q. Cui, K. Morokuma, D. K. Malick, A. D. Rabuck, K. Raghavachari, J. B. Foresman, J. Cioslowski, J. V. Ortiz, A. G. Baboul, B. B. Stefanov, G. Liu, A. Liashenko, P. Piskorz, I. Komaromi, R. Gomperts, R. L. Martin, D. J. Fox, T. Keith, M. A. Al-Laham, C. Y. Peng, A. Nanayakkara, C. Gonzalez, M. Challacombe, P. M. W. Gill, B. Johnson, W. Chen, M. W. Wong, J. L. Andres, C. Gonzalez, M. Head-Gordon, E. S. Replogle, and J. A. Pople, GAUSSIAN 98 (Revision A.7), Gaussian, Inc., Pittsburgh, PA, 1998.
- ⁶⁹V. R. Saunders, R. Dovesi, C. Roetti, M. Causà, N. M. Harrison, R. Orlando, and C. M. Zicovich-Wilson, CRYSTAL98 User's Manual, University of Torino, Torino, 1998.
- ⁷⁰Atomic basis sets are taken from the CRYSTAL web site: http://www.ch.unito.it/ifm/teorica/Basis_Sets/mendel.html and http://www.ch.unito.it/ifm/teorica/AuxB_Sets/mendel.html