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# Study of inclusive $B^-$ and $\bar{B}^0$ decays to flavor-tagged D, $D_s$ , and $\Lambda_c^+$

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We report on a study of inclusive  $B^-$  and  $\bar{B}^0$  meson decays to  $D^0X$ ,  $\bar{D}^0X$ ,  $D^+X$ ,  $D^-X$ ,  $D_s^+X$ ,  $D_s^-X$ ,  $A_c^+X$ ,  $\bar{A}_c^-X$ , based on a sample of  $231\times 10^6$   $B\bar{B}$  events recorded with the BABAR detector at the Y(4S) resonance. Events are selected by completely reconstructing one B and searching for a reconstructed charm particle in the rest of the event. From the measured branching fractions of these decays, we infer the number of charm and anticharm particles per  $\bar{B}$  decay, separately for charged and neutral parents. We derive the total charm yield per  $B^-$  decay,  $n_c^- = 1.208 \pm 0.023 \pm 0.040^{+0.035}_{-0.029}$ , and per  $\bar{B}^0$  decay,  $n_c^0 = 1.203 \pm 0.030 \pm 0.034^{+0.044}_{-0.035}$  where the first uncertainty is statistical, the second is systematic, and the third reflects the charm branching-fraction uncertainties. We also present the charm momentum distributions measured in the  $\bar{B}$  rest frame.

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### I. INTRODUCTION

The dominant process for the decay of a b quark is  $b \rightarrow cW^{*-}$  [1], resulting in a (flavor) correlated c quark and a virtual W. Thus the average number  $N_c$  of correlated charm hadrons produced per b decay is expected to be close to 1 while so far, only 48% (38%) of exclusive  $B^+$  ( $B^0$ ) decays to correlated charmed particles have been measured [2]. In the decay of the W, the production of a  $\bar{u}d$  or a  $\bar{c}s$  pair are

both Cabibbo-allowed and should be approximately equal, the latter being suppressed by a phase-space factor. The first process dominates hadronic b decays. The second can be easily distinguished as it produces a (flavor) anticorrelated  $\bar{c}$  quark and is expected to account for a large fraction of the anticorrelated charm production  $(N_{\bar{c}})$  in b decays.

Theoretically,  $N_c$ ,  $N_{\bar{c}}$  and  $n_c \equiv N_c + N_{\bar{c}}$  can be predicted [3-6]:  $N_c = 0.97 \pm 0.01$ ,  $N_{\bar{c}} = 0.24 \pm 0.05$  and  $n_c = 1.21 \pm 0.05$ , the large uncertainty on the two latter numbers being dominated by the error on the computation of the  $b \rightarrow c\bar{c}s$  partial width. While the data from  $Z \rightarrow b\bar{b}$  decays are in agreement with theoretical predictions [7], the experimental picture has remained blurred for data collected at the Y(4S) resonance [8,9]. Using a fully in-

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clusive technique Ref. [8] measures  $n_c = 1.10 \pm 0.05$ , and Ref. [9] estimates the anticorrelated production to be  $N_{\bar{c}} = 0.22 \pm 0.05$ ; these two results lead to a small value of  $N_c$  compared to 1. This situation was clarified by our previous measurement [10].

Besides the theoretical interest, the fact that anticorrelated charm particles are a background for many studies also motivates a more precise measurement of their production rates in B decays. For instance, the analysis of semileptonic B decays ( $b \rightarrow c \ell^-$ ) is sensitive to correlated and anticorrelated charm productions when the charmed particle decays semileptonically. Such processes can produce a lepton with the same sign as that of the b quark via cascade decays such  $b \rightarrow \bar{c} \rightarrow \ell^-$ . This is the case, in particular, for the measurement of the ratio  $\mathcal{B}(B^+ \rightarrow Xe^+\nu)/\mathcal{B}(B^0 \rightarrow Xe^+\nu)$  [11].

Experimentally, we investigate correlated and anticorrelated charm production through the measurement of the inclusive B-decay rates to a limited number of charm hadron species, i.e.  $D^0$ ,  $\bar{D}^0$ ,  $D^+$ ,  $D^-$ ,  $D_s^+$ ,  $D_s^-$ ,  $\Lambda_c^+$ ,  $\bar{\Lambda}_c^-$ ,  $\Xi_c$  and charmonia, because all other charm particles decay into one of the previous hadrons. The analysis presented here exploits a substantially larger data sample than the original BABAR result [10]. In addition, two major improvements significantly reduce the systematic uncertainty: a more sophisticated fitting method to extract, in a correlated manner, the number of reconstructed Bmesons and the charm hadron yields, and a better understanding of the differences between data and simulation. especially for particle identification. Other measurements [8,9,12–14] of these rates are more statistically limited and/or do not distinguish between the different parent B states.

Most of the charged and neutral D mesons produced in  $\bar{B}$  decays come from correlated production  $\bar{B} \to DX$ . However, a significant number of  $\bar{B} \to \bar{D}X$  decays are expected through  $b \to c\bar{c}s$  transitions, such as  $\bar{B} \to D^{(*)}\bar{D}^{(*)}\bar{K}^{(*)}(n\pi)$ . Although the branching fractions of the 3-body decays  $\bar{B} \to D^{(*)}\bar{D}^{(*)}\bar{K}$  have been measured [15,16], they do not saturate  $\bar{B} \to \bar{D}X$  transitions [10]. It is therefore important to improve the precision on the  $\bar{B} \to \bar{D}X$  branching fraction.

By contrast, anticorrelated  $D_s^-$  production,  $\bar{B} \to D_s^- D(n\pi)$ , is expected to dominate  $\bar{B}$  decays to  $D_s$  mesons, since correlated production needs an extra  $s\bar{s}$  pair created from the vacuum to give  $\bar{B} \to D_s^+ K^-(n\pi)$ . There is no prior published measurement for correlated  $D_s^+$  production.

Correlated  $\Lambda_c^+$  are produced in decays like  $\bar{B} \to \Lambda_c^+ \bar{p} \pi^-(\pi)$ , while anticorrelated  $\bar{\Lambda}_c^-$  should originate predominantly from  $\bar{B} \to \Xi_c \bar{\Lambda}_c^-(\pi)$ . The decay  $\bar{B} \to \Xi_c \bar{\Lambda}_c^-$  has recently been observed [17], confirming the hypothesis of associated  $\Xi_c \bar{\Lambda}_c^-$  production. Another possibility for anticorrelated  $\bar{\Lambda}_c^-$  production is  $\bar{B} \to \Lambda_c^+ \bar{\Lambda}_c^- K$ , the baryonic analogue of the  $D\bar{D}K$  decay.

This analysis uses  $Y(4S) \to B\bar{B}$  events in which either a  $B^+$  or a  $B^0$  meson (hereafter denoted  $B_{\rm rec'd}$ ) decays into a hadronic final state and is fully reconstructed. We then reconstruct D,  $D_s$  and  $\Lambda_c^+$  from the decay products of the recoiling  $B^-(\bar{B}^0)$  meson and compare the flavor of the charm hadron with that of the reconstructed B (taking into account  $B^0$ - $\bar{B}^0$  mixing). This allows separate measurements of the  $B^-(\bar{B}^0) \to D^0 X$ ,  $D^+ X$ ,  $D_s^+ X$ ,  $\Lambda_c^+ X$  and  $B^-(\bar{B}^0) \to \bar{D}^0 X$ ,  $D^- X$ ,  $D_s^- X$ ,  $\bar{\Lambda}_c^- X$  branching fractions.

We then compute the average number of correlated (anticorrelated) charm particles per  $B^-$  decay,  $N_c^-$  ( $N_{\bar{c}}^-$ ) as

$$N_c^- = \sum_C \mathcal{B}(B^- \to CX),\tag{1}$$

$$N_{\bar{c}}^{-} = \sum_{\bar{C}} \mathcal{B}(B^{-} \to \bar{C}X), \tag{2}$$

where the sum is performed over  $C \equiv \{D^0, D^+, D_s^+, \Lambda_c^+, \Xi_c, (c\bar{c})\}$  or  $\bar{C} \equiv \{\bar{D}^0, D^-, D_s^-, \bar{\Lambda}_c^-, (c\bar{c})\}$ , and  $(c\bar{c})$  refers to all charmonium states collectively. We neglect anticorrelated  $\bar{\Xi}_c$  production, as it requires both a  $\bar{c}s$  and an  $s\bar{s}$  pair in the decay to give  $\bar{\Xi}_c\Omega_c$ . We then sum  $N_c^-$  and  $N_c^-$  to obtain the average number of charm plus anticharm quarks per  $B^-$  decay,  $n_c^- = N_c^- + N_{\bar{c}}^-$ . We similarly define  $N_c^0$ ,  $N_c^0$  and  $n_c^0$  for  $\bar{B}^0$  decays.

The above method also lends itself to a measurement of the momentum distribution of each charm species directly in the rest frame of the parent meson, because the four-momentum of each recoiling  $\bar{B}$  is fully determined from those of the Y(4S) and of the reconstructed B. The resulting charm spectra can then be compared to theoretical predictions in the same frame [18]. This avoids the significant smearing due to the Lorentz boost from the parent- $\bar{B}$  frame to the Y(4S) frame affecting earlier measurements, such as those reported in [8]. These spectra might also show indications of four-quark states [19].

# II. BABAR DETECTOR AND DATA SAMPLE

The measurements presented here are based on a sample of  $231 \times 10^6$   $B\bar{B}$  pairs  $(210~{\rm fb^{-1}})$  recorded at the Y(4S) resonance with the BABAR detector at the PEP-II asymmetric-energy B factory at SLAC. The BABAR detector is described in detail elsewhere [20]. Charged-particle trajectories are measured by a 5-layer double-sided silicon vertex tracker and a 40-layer drift chamber, both operating in a 1.5-T solenoidal magnetic field. Charged-particle identification is provided by the average energy loss (dE/dx) in the tracking devices and by an internally reflecting ring-imaging Cherenkov detector. Photons are detected by a CsI(Tl) electromagnetic calorimeter. We use Monte Carlo simulations of the BABAR detector based on GEANT4 [21] to optimize selection criteria and determine selection efficiencies.

# III. B MESON RECONSTRUCTION

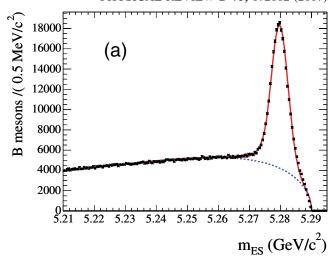
We reconstruct  $B^+$  and  $B^0$  decays  $(B_{\rm rec'd})$  in the modes  $B^+ \to \bar{D}^{(*)0}\pi^+$ ,  $\bar{D}^{(*)0}\rho^+$ ,  $\bar{D}^{(*)0}a_1^+$  and  $B^0 \to D^{(*)-}\pi^+$ ,  $D^{(*)-}\rho^+$ ,  $D^{(*)-}a_1^+$ .  $\bar{D}^0$  candidates are reconstructed in the  $K^+\pi^-$ ,  $K^+\pi^-\pi^0$ ,  $K^+\pi^-\pi^+\pi^-$  and  $K_S^0\pi^+\pi^-(K_S^0\to\pi^+\pi^-)$  decay channels, while  $D^-$  are reconstructed in the  $K^+\pi^-\pi^-$  and  $K_S^0\pi^-$  modes.  $D^*$  candidates are reconstructed in the  $D^{*-}\to \bar{D}^0\pi^-$  and  $\bar{D}^{*0}\to \bar{D}^0\pi^0$  decay modes.

Two independent variables are defined to separate the Bsignal from the combinatorial background reconstructed-B The samples. first  $\sqrt{(s/2 + \mathbf{p}_i \cdot \mathbf{p}_B)^2/E_i^2 - \mathbf{p}_B^2}$ , where  $\mathbf{p}_B$  is the  $B_{\text{rec'd}}$  momentum,  $(E_i, \mathbf{p}_i)$  is the four-momentum of the initial  $e^+e^$ system, both measured in the laboratory frame, and  $\sqrt{s}$  is the invariant mass of the  $e^+e^-$  system. The signal yield  $N_R$ of reconstructed B mesons is extracted from a fit to the  $m_{\rm ES}$ spectrum of the  $B_{rec'd}$  samples (Fig. 1). The B signal is modeled by a Crystal Ball function  $\Gamma_{CB}$  [22] which is a Gaussian peaking at the B meson mass modified by an exponential low-mass tail that accounts for photon energy loss. The B combinatorial background is modeled using the empirical ARGUS phase-space threshold function  $\Gamma_{ARG}$ [23]. All the signal and background parameters of these functions are extracted from a fit to the data.

The second variable used to ensure a reasonable purity of the B sample is  $\Delta E = E_B^* - \sqrt{s}/2$ , where  $E_B^*$  is the energy of the reconstructed B candidate in the  $e^+e^-$  center-of-mass frame. Quantitatively, the purity is defined as the fitted yield of signal B with  $m_{\rm ES} > 5.27~{\rm GeV}/c^2$ , normalized to the total number of reconstructed  $B^+$  ( $B^0$ ) candidates in the same interval. This is measured in the data, separately for each reconstructed-B mode. To reach a minimal purity of 40%, we apply a cut  $|\Delta E| < n\sigma_{\Delta E}$ , using the resolution  $\sigma_{\Delta E}$  measured in data for each decay mode, with n=2 or 3 depending on the decay channel. If an event contains several  $B^+$  ( $B^0$ ) candidates, only the highest-purity B-decay mode is retained.

The  $m_{\rm ES}$  spectra of the full charged and neutral reconstructed B samples are shown on Fig. 1. The signal yields of  $B^+$  and  $B^0$  mesons are  $N_{B^+} = 200359 \pm 705$  and  $N_{B^0} = 110735 \pm 424$ , where the errors reflect the statistical uncertainty in the number of combinatorial background events. These numbers provide the normalization for all the branching fractions reported below.

The contamination of misreconstructed  $B^0$  events in the  $B^+$  signal (and vice-versa) induces a background which peaks near the B mass. From the Monte Carlo simulation, the fraction of  $B^0$  events in the reconstructed  $B^+$  signal sample is found to be  $c_0 = 0.038 \pm 0.009 (\text{syst})$ , and the fraction of  $B^+$  events in the reconstructed  $B^0$  signal sample  $c_+ = 0.028 \pm 0.007 (\text{syst})$ . The systematic uncertainties take into account possible differences in reconstructing real and simulated events, as well as branching-fraction



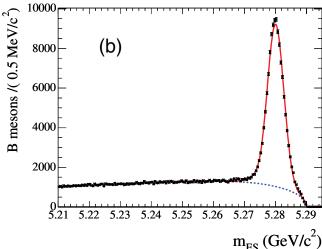


FIG. 1 (color online).  $m_{\rm ES}$  spectra of reconstructed (a)  $B^+$  and (b)  $B^0$  candidates. The solid curve is the sum of the fitted signal and background whereas the dashed curve is the background component only.

uncertainties for those B decay modes contributing to the wrong-charge contamination.

# IV. INCLUSIVE CHARM BRANCHING FRACTIONS

We now turn to the analysis of inclusive D,  $\bar{D}$ ,  $D_s^-$ ,  $D_s^+$ ,  $\Lambda_c^+$ ,  $\bar{\Lambda}_c^-$  production in the decays of the  $\bar{B}$  mesons that recoil against the reconstructed B. Charm particles C are distinguished from anticharm particles  $\bar{C}$ . They are reconstructed from charged tracks that do not belong to the reconstructed B. The decay modes considered are listed in Table I along with their branching fractions. Those are taken from Ref. [24] except for the  $D_s^+ \to \phi \pi^+$  channel [25] where we use the more precise measurement reported in Ref. [2].

### A. Charm particle yields

The numbers of charm (anticharm) particles are extracted from an unbinned maximum likelihood fit to the

TABLE I. Charm-particle decay modes and branching fractions.

$C \rightarrow f$	$\mathcal{B}(C \to f) \ (\%)$
$D^0 \to K^- \pi^+$	$3.80 \pm 0.09$
$D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$	$7.48 \pm 0.31$
$D^+ \rightarrow K^- \pi^+ \pi^+$	$9.1 \pm 0.7$
$D_s^+ \to \phi \pi^+ (\phi \to K^+ K^-)$	$4.40 \pm 0.60 (49.3 \pm 1.0\%)$
$D_s^+ \to \bar{K}\bar{K}^{*0}K^+(\bar{K}^{*0} \to K^-\pi^+)$	$4.18 \pm 0.72(66.51 \pm 0.01\%)$
$D_s^+ \to K_S^0 K^+ (K_S^0 \to \pi^+ \pi^-)$	$2.22 \pm 0.46 (68.95 \pm 0.14\%)$
$\Lambda_c^+ \to p K^- \pi^+$	$5.0 \pm 1.3$

two-dimensional distribution  $[m_{\rm ES}, m_{C(\bar C)}]$ , where  $m_{\rm ES}$  is the beam-energy substituted mass of the reconstructed B and  $m_{C(\bar C)}$  is the mass of the charm (anticharm) particle found among the recoil products. Figs. 2–5 show the results of these fits, projected onto the  $m_{C(\bar C)}$  axis, for events in the  $m_{\rm ES}$  signal region ( $m_{\rm ES} > 5.270~{\rm GeV}/c^2$ ). The probability density function used to fit the  $[m_{\rm ES}, m_{C(\bar C)}]$  distributions is the sum of four components :

- (i)  $P_{B\text{sig}}^{C\text{sig}}$ : reconstructed charm (anticharm) signal in the recoil of reconstructed B signal,
- (ii)  $P_{Bbkg}^{Csig}$ : reconstructed charm (anticharm) signal in the recoil of combinatorial B background,
- (iii)  $P_{B ext{sig}}^{C ext{bkg}}$ : combinatorial charm (anticharm) background in the recoil of reconstructed B signal,
- (iv)  $P_{Bbkg}^{Cbkg}$ : combinatorial charm (anticharm) background in the recoil of combinatorial B background,

These four components are modeled as follows:

$$\begin{split} P_{B\text{sig}}^{C\text{sig}}(m_{\text{ES}}, m_C) &\equiv \Gamma_{CB}(m_{\text{ES}}) \times \rho_S(m_C), \\ P_{B\text{bkg}}^{C\text{sig}}(m_{\text{ES}}, m_C) &\equiv \Gamma_{\text{ARG}}(m_{\text{ES}} \times \rho_S(m_C), \\ P_{B\text{sig}}^{C\text{bkg}}(m_{\text{ES}}, m_C) &\equiv \Gamma_{CB}(m_{\text{ES}}) \times \rho_{\text{comb}}(m_C), \\ P_{B\text{bkg}}^{C\text{bkg}}(m_{\text{ES}}, m_C) &\equiv \Gamma_{\text{ARG}}(m_{\text{ES}}) \times \rho_{\text{comb}}(m_C). \end{split}$$
(3)

The function  $\Gamma_{CB}$  with all its parameters fixed from the fit detailed in Sec. III is used to model the reconstructed B signal. The combinatorial background is described by an ARGUS function  $\Gamma_{ARG}$  (see Sec. III) whose shape parameter is floated in the fit to allow for a possible charm decaymode dependence of this background. A Gaussian function  $\rho_S(m_{C(\bar{C})})$  describes the mass shape of the reconstructed charm signal. Its mean is fixed from the data using charm particles recoiling against either  $B^-$  or  $\bar{B}^0$  mesons. Its resolution is fixed from the simulation in order to remain insensitive to statistical fluctuations, particularly for the modes with a small branching fraction. For all charm modes, the Monte Carlo resolution is consistent with that measured in the data; the difference is accounted for in the systematic uncertainty. The combinatorial background distribution is fitted with a linear function  $\rho_{\text{comb}}(m_{C(\bar{C})})$  (except for the  $D^0 \to K^-\pi^+\pi^-\pi^+$  for which a quadratic dependence is assumed); all its parameters are floated in the fit [26].

The reconstruction efficiencies for each charm final state  $C \to f$  (Table II) are computed from the simulation as a function of  $p^*$ , the charm-particle momentum in the  $\bar{B}$  rest frame, and applied event-by-event to obtain the efficiency-corrected charm and anticharm signal yields. These are denoted, respectively, by  $N^-(C \to f)$  ( $N^0(C \to f)$ ) and  $N^-(\bar{C} \to \bar{f})$  ( $N^0(\bar{C} \to \bar{f})$ ) and are listed in Table III. We then determine the charm and anticharm fractional production rates  $\mathcal{B}_c^{-(0)}$  and  $\bar{\mathcal{B}}_c^{-(0)}$ , defined as

$$\mathcal{B}_{c}^{-(0)} = N^{-(0)}(C \to f) / [N_{B^{+}(B^{0})} \times \mathcal{B}(C \to f)],$$
 
$$\bar{\mathcal{B}}_{c}^{-(0)} = N^{-(0)}(\bar{C} \to \bar{f}) / [N_{B^{+}(B^{0})} \times \mathcal{B}(C \to f)],$$
 (4)

where  $N_{B^+}$  ( $N_{B^0}$ ) is the number of reconstructed  $B^+$  ( $B^0$ ) mesons, and  $\mathcal{B}(C \to f)$  is the  $C \to f$  branching fraction reported in Table I.  $\mathcal{B}_c^-$ ,  $\bar{\mathcal{B}}_c^-$ ,  $\mathcal{B}_c^0$  and  $\bar{\mathcal{B}}_c^0$  are listed in Table III.

# B. Correlated and anticorrelated charm branching fractions

For charged *B*, the branching fractions for correlated and anticorrelated *C* production are given by

$$\mathcal{B}(B^- \to CX) = \mathcal{B}_c^- - c_0 \mathcal{B}_1^0,$$
  

$$\mathcal{B}(B^- \to \bar{C}X) = \bar{\mathcal{B}}_c^- - c_0 \mathcal{B}_2^0.$$
(5)

The correlated (anticorrelated)  $B^- \to CX$  branching-fraction is equal to the charm (anticharm) fractional production rate  $\mathcal{B}_c^-$  ( $\bar{\mathcal{B}}_c^-$ ) in the recoil of reconstructed  $B^+$  mesons modified by a small correction term  $c_0\mathcal{B}_1^0$  ( $c_0\mathcal{B}_2^0$ ) that accounts for the  $B^0$  contamination in the reconstructed  $B^+$  sample. The factors  $\mathcal{B}_1^0$  and  $\mathcal{B}_2^0$  depend on the measured  $\bar{B}^0 \to CX$  and  $B^0 \to CX$  branching fractions, and on the  $B^0\bar{B}^0$  mixing parameter  $\chi_d$  [24]. Doubly Cabibbosuppressed  $D^0$  decays ( $D^0 \to K^+\pi^-$  and  $D^0 \to K^+\pi^-\pi^-$ ) are also taken into account. We combine the results from the different  $D^0$  and  $D_s$  decay modes to extract the final branching fractions listed in Table IV. The probability for the correlated  $D_s^+$  production observed in  $B^-$  decays to be due to a background fluctuation is less than  $5 \times 10^{-4}$ .

For neutral B, charm and anticharm production rates in the recoil of reconstructed  $B^0$  mesons have to be corrected for  $B^0\bar{B}^0$  mixing to obtain the correlated and anticorrelated charm branching fractions

$$\mathcal{B}(\bar{B}^{0} \to CX) = \frac{\mathcal{B}_{c}^{0} - \chi_{d}(\mathcal{B}_{c}^{0} + \bar{\mathcal{B}}_{c}^{0})}{1 - 2\chi_{d}} - c_{+}\mathcal{B}_{1}^{+},$$

$$\mathcal{B}(\bar{B}^{0} \to \bar{C}X) = \frac{\bar{\mathcal{B}}_{c}^{0} - \chi_{d}(\bar{\mathcal{B}}_{c}^{0} + \mathcal{B}_{c}^{0})}{1 - 2\chi_{d}} - c_{+}\mathcal{B}_{2}^{+}.$$
(6)

The correction factors  $c_+\mathcal{B}_1^+$  and  $c_+\mathcal{B}_2^+$  account for  $B^+$ 

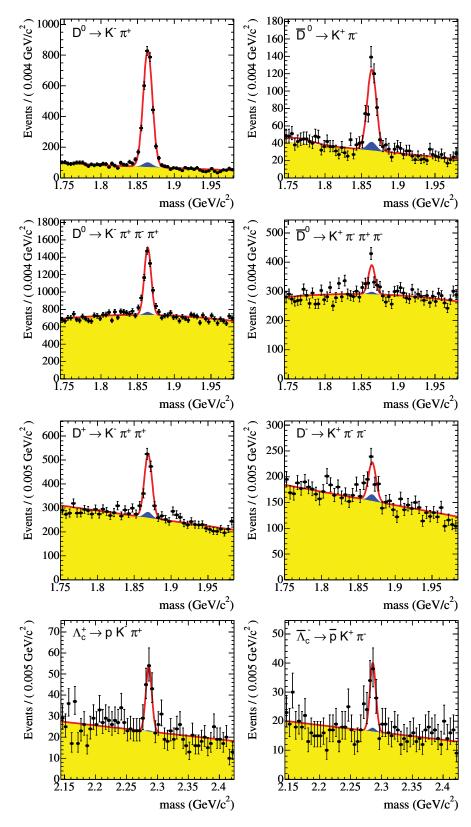


FIG. 2 (color online). Charm (left) and anticharm (right) mass spectra in the recoil of  $B^+$  candidates, for the subsample of events with  $m_{\rm ES} > 5.270~{\rm GeV}/c^2$  (B signal region). The solid curve shows the result of the two-dimensional fit. The dark shaded areas show the contribution of reconstructed D,  $\bar{D}$ ,  $\Lambda_c^+$  and  $\bar{\Lambda}_c^-$  signal in the recoil of combinatorial  $B_{\rm rec'd}^+$  background. The light shaded area corresponds to the fitted combinatorial (anti-) charm background.

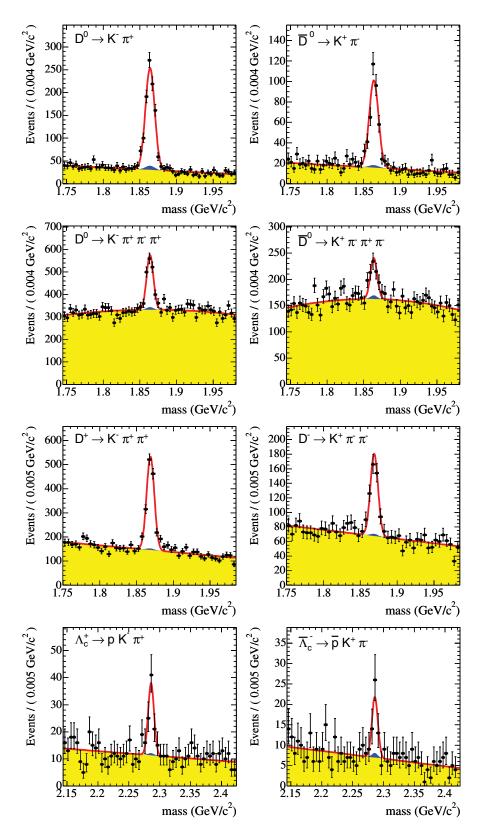


FIG. 3 (color online). Charm (left) and anticharm (right) mass spectra as for Fig. 2, but in the recoil of  $\bar{B}^0$  candidates.

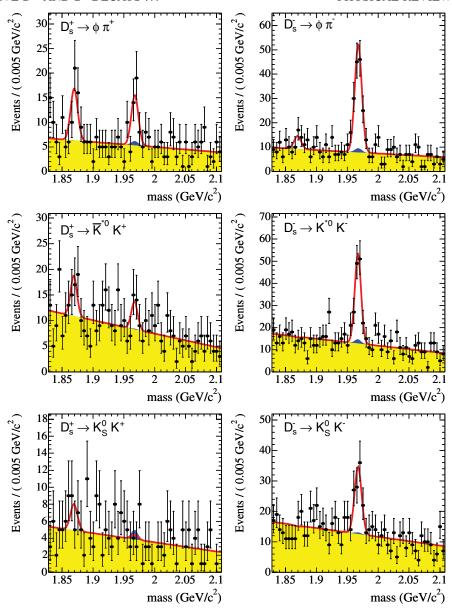


FIG. 4 (color online).  $D_s^+$  (left) and  $D_s^-$  (right) mass spectra in the recoil of  $B^+$  candidates, for the subsample of events with  $m_{\rm ES} > 5.270~{\rm GeV}/c^2$  (B signal region). The solid curve shows the result of the two-dimensional fit. The dark shaded areas show the contribution of reconstructed  $D_s^+$ ,  $D_s^-$  signal in the recoil of combinatorial  $B_{\rm rec'd}^+$  background. The light shaded area corresponds to the fitted combinatorial (anti-) charm background. The Gaussian peak at the  $D^+$  mass accounts for reconstructed  $D^+$  signal [26].

contamination in the  $B^0$  sample and depend on the  $B^- \to CX$  and  $B^+ \to CX$  branching fractions. Combining the different  $D^0$  and  $D_s$  modes, we obtain the final branching fractions listed in Table IV.

We also compute the fraction of anticorrelated charm production in  $\bar{B}$  decays

$$w(\bar{C}) = \frac{\mathcal{B}(\bar{B} \to \bar{C}X)}{\mathcal{B}(\bar{B} \to CX) + \mathcal{B}(\bar{B} \to \bar{C}X)}.$$
 (7)

Here, many systematic uncertainties cancel out (tracking, K identification, D branching fractions, B counting). The results are given in Table V.

The main systematic uncertainties are associated with the track-finding efficiency, the models used to describe the  $m_{\rm ES}$  and  $m_{C(\bar{C})}$  distributions, and the particle-identification efficiency. For example, the 2.7% absolute systematic uncertainty on  $\mathcal{B}(B^- \to D^0 X)$  reflects the quadratic sum of 1.3% attributed to the track-finding efficiency, 1.6% to the description of the  $m_{\rm ES}$  distribution by the  $\Gamma_{\rm ARG}$  and  $\Gamma_{CB}$  functions, 0.8% to the description of the  $m_{C(\bar{C})}$  signal distribution by the  $\rho_S$  function, 1.4% to the particle identification, 0.5% to the Monte Carlo statistics, 0.4% to final-state radiations in  $D^0$  decays, 0.3% to  $c_0$ , and 0.1% to  $\mathcal{B}_1^0$ .

The uncertainty affecting the track-finding efficiency is estimated with two different methods. The first uses a large

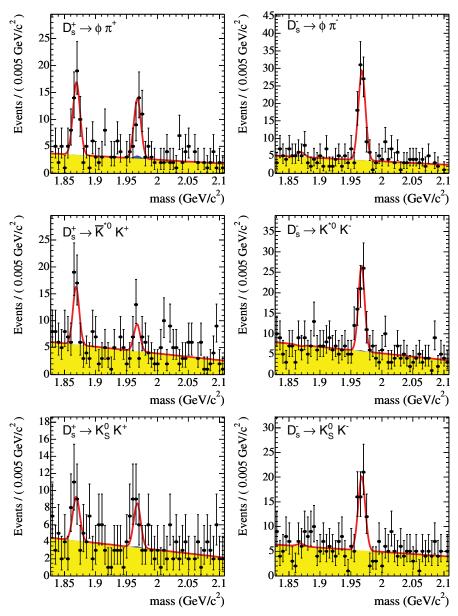


FIG. 5 (color online).  $D_s^+$  and  $D_s^-$  mass spectra as for Fig. 4, but in the recoil of  $\bar{B}^0$  candidates.

TABLE II.  $p^*$ -averaged reconstruction efficiencies  $\epsilon_C$  for each charm final state. The errors reflect the limited Monte Carlo statistics.

$C \to f$	$\epsilon_{C}$ (%)
$D^0 \to K^- \pi^+$	$50.2 \pm 0.3$
$D^0  o K^- \pi^+ \pi^- \pi^+$	$20.1 \pm 0.2$
$D^+ \rightarrow K^- \pi^+ \pi^+$	$33.7 \pm 0.2$
$D_s^+  o \phi  \pi^+$	$33.0 \pm 0.8$
$D_s^+ \to \bar{K}^{*0} K^+$	$18.0 \pm 0.5$
$D_s^+ \to K_S^0 K^+$	$31.1 \pm 0.8$
$\Lambda_c^+ \to p K^- \pi^+$	$26.7 \pm 0.9$

inclusive sample of tracks with a minimum number of hits in the silicon vertex detector. The second relies on an  $e^+e^- \rightarrow \tau^+\tau^-$  control sample. From these, we derive a relative systematic uncertainty of 0.8% per track.

The modeling of the  $m_{\rm ES}$  distribution by the  $\Gamma_{CB}$  and the  $\Gamma_{\rm ARG}$  functions affects, in a correlated manner, both the charm signal yields and the numbers of reconstructed B mesons used in normalizing the branching fractions. As a consequence, the measured branching fractions become largely insensitive to the model parameters. The remaining uncertainty is conservatively estimated by varying the lower edge of the  $m_{\rm ES}$  fit range from 5.195 to 5.225 GeV/ $c^2$ . This yields a variation in the branching fraction that is taken as systematic uncertainty. This range was chosen such that the branching fractions measured in

TABLE III. Charm and anticharm efficiency-corrected signal yields and fractional production rates. The uncertainties are statistical only.

C decay mode	C in recoi		$\bar{C}$ in recoi		C in reco	il of $B_{\text{rec'd}}^0$	$\bar{C}$ in recoi	
	$N^-(C \to f)$	$\mathcal{B}_{c}^{-}$ (%)	$N^-(\bar{C} \to \bar{f})$	$\mathcal{B}_{c}^{-}$ (%)	$N^0(C \to f)$	$\mathcal{B}_{c}^{0}\left(\% ight)$	$N^0(\bar{C} \to \bar{f})$	$\mathcal{B}_{c}^{0}\left(\% ight)$
$D^0 \rightarrow K^- \pi^+$	$5898 \pm 126$	$77.5 \pm 1.6$	$691 \pm 52$	$9.1 \pm 0.7$	$1713 \pm 70$	$41.1 \pm 1.7$	$669 \pm 44$	$15.9 \pm 1.0$
$\rightarrow K^-\pi^+\pi^-\pi^+$	$11010 \pm 383$	$73.4 \pm 2.6$	$1378 \pm 214$	$9.2 \pm 1.4$	$3418 \pm 239$	$41.2 \pm 2.9$	$1065 \pm 159$	$12.8 \pm 1.9$
$D^+ \to K^- \pi^+ \pi^+$	$1970 \pm 131$	$10.8 \pm 0.7$	$513 \pm 89$	$2.8 \pm 0.5$	$3044 \pm 122$	$30.2 \pm 1.2$	$869 \pm 74$	$8.6 \pm 0.7$
$D_s^+  o \phi  \pi^+$	$85 \pm 24$	$2.0 \pm 0.5$	$385 \pm 42$	$8.9 \pm 1.0$	$97 \pm 21$	$4.0 \pm 0.9$	$227 \pm 30$	$9.5 \pm 1.3$
$ ightarrow ar{K}^{*0}K^+$	$78 \pm 39$	$1.4 \pm 0.7$	$567 \pm 72$	$10.2 \pm 1.3$	$78 \pm 28$	$2.5 \pm 0.9$	$306 \pm 50$	$9.9 \pm 1.6$
$\rightarrow K_S^0 K^+$	$0 \pm 16$	$0.0 \pm 0.5$	$212 \pm 39$	$7.2 \pm 1.3$	$48 \pm 19$	$3.0 \pm 1.2$	$148 \pm 29$	$9.1 \pm 1.7$
$\Lambda_c^+ \to p K^- \pi^+$	$288 \pm 52$	$2.9 \pm 0.5$	$210 \pm 45$	$2.1 \pm 0.5$	$240 \pm 41$	$4.3 \pm 0.7$	$124 \pm 30$	$2.2 \pm 0.5$

TABLE IV.  $\bar{B}$  branching fractions. The first uncertainty is statistical, the second is systematic, and the third reflects charm branching-fraction uncertainties [2,24].

	Corre	elated	Antico	orrelated
C	$\mathcal{B}(B^-\to CX)\ (\%)$	$\mathcal{B}(\bar{B}^0 \to CX) \ (\%)$	$\mathcal{B}(B^- \to \bar{C}X) \ (\%)$	$\mathcal{B}(\bar{B}^0 \to \bar{C}X) \ (\%)$
$\overline{D^0}$	$78.6 \pm 1.6 \pm 2.7^{+2.0}_{-1.9}$	$47.4 \pm 2.0 \pm 1.5^{+1.3}_{-1.2}$	$8.6 \pm 0.6 \pm 0.3^{+0.2}_{-0.2}$	$8.1 \pm 1.4 \pm 0.5^{+0.2}_{-0.2}$
$D^{+}$	$9.9 \pm 0.8 \pm 0.5^{+0.8}_{-0.7}$	$36.9 \pm 1.6 \pm 1.4^{+2.6}_{-2.3}$	$2.5 \pm 0.5 \pm 0.1^{+0.2}_{-0.2}$	$2.3 \pm 1.1 \pm 0.3^{+0.2}_{-0.1}$
				<3.9 at 90% CL
$D_s^+$	$1.2^{+0.4}_{-0.3} \pm 0.1^{+0.2}_{-0.1}$	$1.6 \pm 0.9 \pm 0.1^{+0.2}_{-0.2}$	$8.6 \pm 0.7 \pm 0.4^{+1.3}_{-1.0}$	$11.2 \pm 1.3 \pm 0.4^{+1.7}_{-1.3}$
		<2.8 at 90% CL		
$\Lambda_c^+$	$2.8 \pm 0.5 \pm 0.3^{+1.0}_{-0.6}$	$5.0 \pm 1.0 \pm 0.5^{+1.8}_{-1.0}$	$2.1 \pm 0.5 \pm 0.2^{+0.8}_{-0.4}$	$1.6 \pm 0.9 \pm 0.2^{+0.6}_{-0.3}$
	***	**	***	<3.1 at 90% CL

the simulation remain stable within their statistical uncertainty.

The uncertainty associated with the description of the charm signal mass shape by the  $\rho_S$  function translates into an uncertainty on the charm reconstruction efficiency. It is estimated by fitting the simulated charm signal with a double instead of a single Gaussian.

The systematic uncertainties affecting the proton and charged kaon particle-identification efficiency are estimated using  $D^0 \to K^-\pi^+$  and  $\Lambda^0 \to p\pi^-$  samples recoiling against reconstructed  $B^+$  and  $B^0$  mesons. The  $D^0$  or  $\Lambda^0$  signal yields are extracted in a manner similar to that described in Sec. IVA, both with and without applying

TABLE V. Fraction of anticorrelated charm as defined in Eq. (7).

Mode	$B^-$ decays	$\bar{B}^0$ decays
$\bar{D}^0 X$	$0.098 \pm 0.007 \pm 0.001$	$0.146 \pm 0.022 \pm 0.006$
$D^-X$	$0.204 \pm 0.035 \pm 0.001$	$0.058 \pm 0.028 \pm 0.006$
		<0.098 at 90% CL
$D_s^- X$	$0.884 \pm 0.038 \pm 0.002$	$0.879 \pm 0.066 \pm 0.005$
_		>0.791 at 90% CL
$\bar{\Lambda}_c^- X$	$0.427 \pm 0.071 \pm 0.001$	$0.243^{+0.119}_{-0.121} \pm 0.003$
		<0.403 at 90% CL

the proton or kaon particle-identification requirements. The ratio of these yields on real and simulated samples is proportional to the particle-identification efficiency in the data and the simulation, respectively. The difference between these two efficiencies is then taken as an estimate of the corresponding systematic uncertainty (1.7% relative uncertainty per kaon and 1.3% per proton).

The statistical and systematic uncertainties in Table IV and V are computed separately for each charm decay mode; correlated errors are taken into account when averaging over  $D^0$  and  $D_s$  final states.

# C. Average charm production in $\bar{B}$ decays

To extract  $N_c$  from the results of Table IV, we still need to evaluate the  $\bar{B}\to\Xi_c X$  and  $\bar{B}\to(c\bar{c})X$  branching fractions. Because there exists no absolute measurement of the  $\Xi_c$ -decay branching fraction, the absolute rates for correlated  $\Xi_c$  production in B decays are unknown [17,27]. Therefore, following the discussion in Sec. I, we assume that  $\mathcal{B}(\bar{B}\to\Xi_c X)=\mathcal{B}(\bar{B}\to\bar{\Lambda}_c^- X)-\mathcal{B}(\bar{B}\to\Lambda_c^+ \bar{\Lambda}_c^- \bar{K}(\pi))$  [28]. A recent measurement [29] indicates that  $\bar{B}\to\Lambda_c^+ \bar{\Lambda}_c^- \bar{K}$  decays have a branching fraction of the order of  $7\times 10^{-4}$ , and thus can be neglected by comparison to  $N_c^{-/0}$  (see also [10]). We take  $\mathcal{B}(\bar{B}\to(c\bar{c})X)=(2.3\pm0.3)\%$  [7,30] and, using Eqs. (1) and (2), we obtain for charm production in  $B^-$  decays

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$$N_c^- = 0.969 \pm 0.019 \pm 0.032^{+0.026}_{-0.022}$$
  
 $N_{\bar{c}}^- = 0.239 \pm 0.012 \pm 0.008^{+0.016}_{-0.012}$   
 $n_c^- = 1.208 \pm 0.023 \pm 0.040^{+0.036}_{-0.020}$ 

and in  $\bar{B}^0$  decays :

$$N_c^0 = 0.948 \pm 0.030 \pm 0.028^{+0.035}_{-0.028},$$
  
 $N_{\tilde{c}}^0 = 0.255 \pm 0.024 \pm 0.009^{+0.019}_{-0.014},$   
 $n_c^0 = 1.203 \pm 0.030 \pm 0.034^{+0.035}_{-0.034}.$ 

These results supersede those of Ref. [10]. The threefold increase in integrated luminosity accounts for the substantial reduction in statistical error. The experimental systematic uncertainties have been similarly reduced, primarily through the use of the two-dimensional  $[m_{ES}, m_{C(\bar{C})}]$ fit, which takes correctly into account the correlation between the fitted number of reconstructed B mesons and the corresponding charm yield, and by a better description of the kaon identification in the simulation. The systematic uncertainty associated with these sources decreased by a factor of 1.7 and 1.8, respectively. The reconstructed-B selection was also somewhat tightened to improve the purity. The differences between the central values reported above and those in our original publication [10] can be traced to three factors: a more precise  $D_s^+$  branching fraction [2] assumed in interpreting the  $D_s^+ \to \phi \pi^+$  yield, a better control of systematic uncertainties, and statistical fluctuations. The consistency of our analyses was checked by splitting the present sample into two data-taking periods, one corresponding to the dataset used in Ref. [10] (81 fb<sup>-1</sup>) and another one gathering the remaining 121 fb $^{-1}$ . For the first data-taking period, the differences with the results of Ref. [10] are consistent with the systematic uncertainty ( $\approx 3.5\%$ ) arising from the differences between the two fitting methods, augmented by a statistical component associated with a more restrictive event selection adopted in this paper. A global chi-squared test of the statistical consistency between the two data-taking periods (with identical selection and analysis procedures) yields a 17% probability for the observed differences.

Our results are in agreement with theoretical predictions (as reviewed in Ref. [6])

$$N_c = 0.97 \pm 0.01,$$
  
 $N_{\bar{c}} = 0.24 \pm 0.05,$   
 $n_c = 1.21 \pm 0.05.$ 

Different theoretical results, using experimental inputs, predict  $n_c$  to lie in the range [1.09, 1.28] [6].

# D. Isospin analysis

The main source of anticorrelated  $\bar{D}$  mesons produced in  $\bar{B}$  decays is  $b \to c\bar{c}s$  transitions. In these processes isospin should be conserved, leading to the expectation that:  $\Gamma(B^- \to \bar{D}^0 X) = \Gamma(\bar{B}^0 \to D^- X)$  and  $\Gamma(B^- \to D^- X) =$ 

 $\Gamma(\bar{B}^0 \to \bar{D}^0 X)$ . However,  $\bar{D}$  mesons can also arise from  $\bar{D}^*$  mesons, whose decay does not conserve isospin since the  $\bar{D}^{*0} \to D^- \pi^+$  channel is kinematically forbidden. Thus isospin invariance actually requires

$$\Gamma_{\text{dir}}(B^{-} \to \bar{D}^{0}X) = \Gamma_{\text{dir}}(\bar{B}^{0} \to D^{-}X)$$

$$\Gamma_{\text{dir}}(B^{-} \to D^{-}X) = \Gamma_{\text{dir}}(\bar{B}^{0} \to \bar{D}^{0}X)$$

$$\Gamma(B^{-} \to \bar{D}^{*0}X) = \Gamma(\bar{B}^{0} \to D^{*-}X)$$

$$\Gamma(B^{-} \to D^{*-}X) = \Gamma(\bar{B}^{0} \to \bar{D}^{*0}X)$$
(8)

where  $\Gamma_{\rm dir}(\bar B\to \bar DX)$  refers to the partial width of  $\bar B$ -meson decays to  $\bar D$  mesons where the  $\bar D$  state is *not* reached through a  $\bar D^*$  cascade decay. Equations (8) lead to the following relations involving the measured anticorrelated  $\bar D$  branching fractions in Table IV:

$$rx^* = \mathcal{B}(B^- \to \bar{D}^0 X) - \mathcal{B}(\bar{B}^0 \to D^- X) \frac{\tau_{B^+}}{\tau_{B^0}}$$
 (9)

$$rx^* = \mathcal{B}(\bar{B}^0 \to \bar{D}^0 X) \frac{\tau_{B^+}}{\tau_{B^0}} - \mathcal{B}(B^- \to D^- X)$$
 (10)

and

$$x + x^* = \frac{1}{2} \left[ \mathcal{B}(B^- \to \bar{D}^0 X) + \mathcal{B}(B^- \to D^- X) + \mathcal{B}(\bar{B}^0 \to \bar{D}^0 X) \frac{\tau_{B^+}}{\tau_{B^0}} + \mathcal{B}(\bar{B}^0 \to D^- X) \frac{\tau_{B^+}}{\tau_{B^0}} \right]$$
(11)

where  $\tau_{B^+}/\tau_{B^0}$  is the ratio of the  $B^+$  to the  $B^0$  lifetime,  $r=\mathcal{B}(D^{*-}\to \bar{D}^0\pi^-), \ x=\mathcal{B}_{\rm dir}(B^-\to \bar{D}^0+D^-X)$  and  $x^*=\mathcal{B}(B^-\to \bar{D}^{*0}+D^{*-}X)$  [31]. That both Eqs. (9) and (10) must be satisfied is a consequence of isospin invariance. From these two equations, we extract  $x^*$  with a chisquared method, and using in addition Eq. (11) we calculate

$$\mathcal{B}(B^{-} \to \bar{D}^{*0} + D^{*-}X) = 9.1 \pm 1.5 \pm 0.6\%$$

$$\mathcal{B}_{dir}(B^{-} \to \bar{D}^{0} + D^{-}X) = 2.1 \pm 1.7 \pm 0.7\%$$

$$< 4.5\% \text{at} \quad 90\% \text{CL}$$

$$\frac{\mathcal{B}_{dir}(\bar{B} \to \bar{D}^{0} + D^{-}X)}{\mathcal{B}(\bar{B} \to \bar{D}^{*0} + D^{*-}X)} = 0.23^{+0.25}_{-0.19} \pm 0.09$$

$$< 0.60 \quad \text{at} \quad 90\% \text{CL}$$

Here the first uncertainty is statistical, the second is systematic and includes charm branching-fraction uncertainties, as well as those affecting the values of  $\tau_B^+/\tau_B^0$  and  $\mathcal{B}(D^{*-}\to \bar{D}^0\pi^-)$  taken from Ref. [24]. The  $\chi^2$  of the fit to Eqs. (9) and (10) is 0.01 for 1 degree of freedom.

# V. CHARM MOMENTUM DISTRIBUTIONS IN THE $\bar{B}$ REST FRAME

As the four-momentum of the recoiling  $\bar{B}$  is fully determined, each reconstructed charm hadron can be boosted into the rest frame of its parent  $\bar{B}$ , yielding the  $p^*$  distribution of the corresponding (anticharm) charm species in

the  $\bar{B}$  frame. The number of  $C(\bar{C})$  candidates, their fractional production rates and the  $\bar{B} \to C(\bar{C})X$  branching fractions are then determined in each  $p^*$  bin by the same

methods as in Sec. IV, separately for  $B^-$  and  $\bar{B}^0$  decays. The systematic uncertainties are assumed to be independent of  $p^*$ , except for the error associated with the  $B^0$  ( $B^+$ )

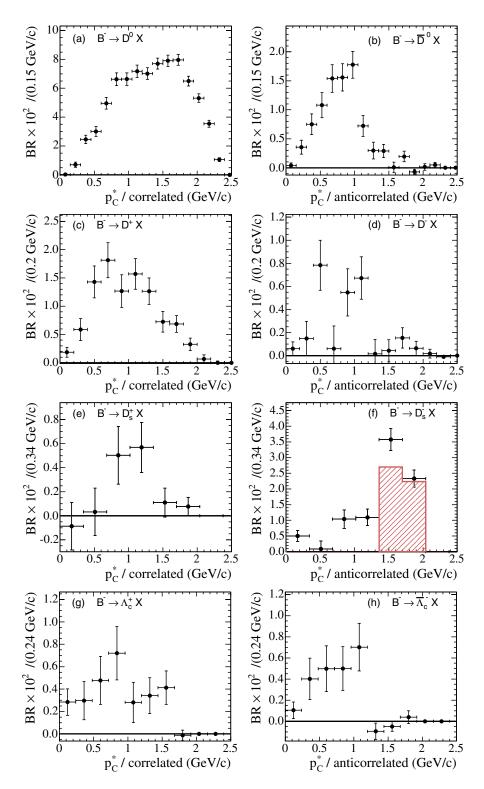


FIG. 6 (color online). Momentum spectra, in the  $B^-$  rest frame, of correlated (left) and anticorrelated (right) charm particles:  $D^0/\bar{D}^0$  (a), (b),  $D^\pm$  (c)(d),  $D_s^\pm$  (e), (f),  $\Lambda_c^\pm$  (g), (h). The error bars are statistical only. The histogram in frame (f) represents the contribution of  $B^- \to D^{(*)0}D_s^{(*)-}$  two-body decays assuming the branching fractions of Ref. [2,24].

contamination in the  $B^+$  ( $B^0$ ) sample : the latter is computed bin-by-bin with a relative uncertainty on  $c_+$  and  $c_0$  increased to 100%.

Figs. 6 and 7 show the result for correlated and anticorrelated  $D^0$ ,  $D^+$ ,  $D_s$  and  $\Lambda_c^+$  production in  $B^-$  and  $\bar{B}^0$ decays, respectively. The numerical values are tabulated in the Appendix. Correlated  $D^0$  and  $D^+$  [Figs. 6(a), 6(c), 7(a), and 7(c)] are produced in several types of transitions :  $b \to c\ell^-\nu$ ,  $b \to c\bar{u}d$  and  $b \to c\bar{c}s$  which explains the fairly large spread of their momentum. High- $p^*$  correlated D's are produced in two-body decays such as  $B^- \to D^0\pi^-$  while low momentum D's might come from higher multiplicity final states such as  $\bar{B} \to D\bar{D}K(X_{\text{light}})$  where  $X_{\text{light}}$  is any

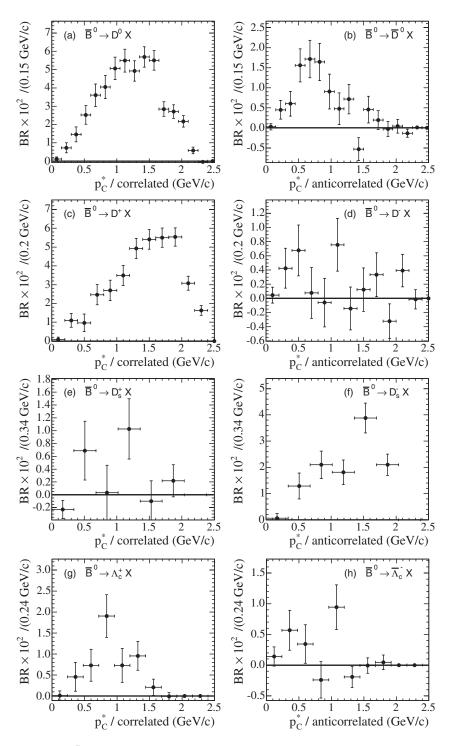


FIG. 7. Momentum spectra, in the  $\bar{B}^0$  rest frame, of correlated (left) and anticorrelated (right) charm particles :  $D^0/\bar{D}^0$  (a), (b),  $D^\pm$  (c)(d),  $D_s^\pm$  (e), (f),  $\Lambda_c^\pm$  (g), (h). The error bars are statistical only.

number of pions and/or photons. The latter processes are also the main source of anticorrelated  $\bar{D}^0$  and  $D^-$  production [Figs. 6(b), 6(d), 7(b), and 7(d)] which explains why anticorrelated  $\bar{D}$  spectra are softer than their correlated counterparts.

Anticorrelated  $D_s^-$  spectra [Figs. 6(f) and 7(f)] have a very different shape compared to anticorrelated  $\bar{D}$  spectra. They are peaked at high  $p^*$  values which is suggestive of the two-body decays  $\bar{B} \to D^{(*)}D_s^-$  and  $\bar{B} \to D^{(*)}D_s^{*-}$ . These decays represent a large fraction of the total anticorrelated  $D_s^-$  production as shown in Fig. 6. In contrast, the corresponding two-body processes  $\bar{B} \to D^{(*)}D^-$  and  $\bar{B} \to D^{(*)}D^{*-}$  are Cabibbo-suppressed.

In the case of anticorrelated  $\bar{\Lambda}_c^-$  production associated with  $\Xi_c$  production, for decays such as  $\bar{B} \to \Xi_c \bar{\Lambda}_c^-(X_{\text{light}})$ , the anticorrelated  $\bar{\Lambda}_c^-$  spectra should have a cut-off at  $p^* < 1.15 \text{ GeV}/c$ . This is actually observed in the data, both in  $B^-$  [Fig. 6(h)] and in  $\bar{B}^0$  [Fig. 7(h)] decays.

## VI. CONCLUSIONS

We have measured the branching fractions for inclusive decays of B mesons to flavor-tagged D,  $D_s$  and  $\Lambda_c^+$ , separately for  $B^-$  and  $\bar{B}^0$ . We observe a significant production of anticorrelated  $D^0$  and  $D^+$  mesons in B decays, with the branching fractions reported in Table IV. These results are consistent with and supersede our previous measurement [10]. We find evidence for correlated  $D_s^+$  production in  $B^-$  decays, a process which has not been previously reported.

The sum of all correlated charm branching fractions,  $N_c$ , is compatible with 1, for charged as well as for neutral B mesons. The numbers of charm particles per  $B^-$  decay  $(n_c^- = 1.208 \pm 0.023 \pm 0.040^{+0.035}_{-0.029})$  and per  $\bar{B}^0$  decay  $(n_c^0 = 1.203 \pm 0.030 \pm 0.034^{+0.044}_{-0.035})$  are consistent with previous measurements [7,9,10] and with theoretical expectations [3-6].

Assuming isospin conservation in the  $b \to c\bar{c}s$  transition, we show that anticorrelated  $\bar{D}$  mesons are mainly produced by cascade decays  $\bar{B} \to \bar{D}^* X \to \bar{D} X$ .

Finally, the technique developed for this analysis allows us to measure the inclusive momentum spectra of flavor-tagged D,  $D_s$  and  $\Lambda_c^+$  in the rest frame of the  $\bar{B}$  parent, separately in  $B^-$  and  $\bar{B}^0$  decays, eventually providing insight into B-decay mechanisms.

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BMBF and DFG (Germany), INFN (Italy), FOM (The Netherlands), NFR (Norway), MIST (Russia), and PPARC (United Kingdom). Individuals have received support from CONACyT (Mexico), Marie Curie EIF (European Union), the A.P. Sloan Foundation, the Research Corporation, and the Alexander von Humboldt Foundation.

### APPENDIX : CHARM p\* SPECTRA

This appendix tabulates the measured  $p^*$  dependence of the branching fractions displayed in Figs. 6 and 7. In Tables VI, VIII, VIII, IX, X, XI, XII, and XIII, the first uncertainty is statistical, the second is systematic and includes charm branching-fraction uncertainties. Within each table, the statistical uncertainties are uncorrelated whereas the systematic errors are fully correlated.

TABLE VI. Correlated and anticorrelated  $D^0$  roduction in  $B^-$  decays.

$p^*$ range (GeV/ $c$ )	correlated prod. $\mathcal{B}(B^- \to X_c X)$ (%)	anticorrelated prod. $\mathcal{B}(B^- \to X_{\bar{c}}X)$ (%)
0.00-0.15	$0.03 \pm 0.06 \pm 0.01$	$0.04 \pm 0.04 \pm 0.01$
0.15 - 0.30	$0.70 \pm 0.18 \pm 0.03$	$0.36 \pm 0.12 \pm 0.02$
0.30 - 0.45	$2.45 \pm 0.29 \pm 0.11$	$0.75 \pm 0.18 \pm 0.03$
0.45 - 0.60	$3.01 \pm 0.34 \pm 0.13$	$1.08 \pm 0.22 \pm 0.05$
0.60 - 0.75	$4.96 \pm 0.40 \pm 0.22$	$1.54 \pm 0.24 \pm 0.07$
0.75 - 0.90	$6.62 \pm 0.44 \pm 0.30$	$1.56 \pm 0.23 \pm 0.07$
0.90-1.05	$6.63 \pm 0.43 \pm 0.30$	$1.78 \pm 0.23 \pm 0.07$
1.05-1.20	$7.18 \pm 0.43 \pm 0.32$	$0.72 \pm 0.18 \pm 0.04$
1.20-1.35	$7.01 \pm 0.41 \pm 0.32$	$0.30 \pm 0.14 \pm 0.05$
1.35-1.50	$7.70 \pm 0.38 \pm 0.35$	$0.29 \pm 0.11 \pm 0.02$
1.50-1.65	$7.90 \pm 0.39 \pm 0.36$	$0.01 \pm 0.09 \pm 0.05$
1.65-1.80	$7.96 \pm 0.38 \pm 0.40$	$0.20 \pm 0.09 \pm 0.02$
1.80-1.95	$6.49 \pm 0.33 \pm 0.32$	$-0.07 \pm 0.04 \pm 0.02$
1.95-2.10	$5.32 \pm 0.29 \pm 0.26$	$0.02 \pm 0.06 \pm 0.02$
2.10-2.25	$3.54 \pm 0.24 \pm 0.19$	$0.05 \pm 0.04 \pm 0.01$
2.25-2.40	$1.06 \pm 0.13 \pm 0.06$	-

TABLE VII. Correlated and anticorrelated  $D^+$  production in  $B^-$  decays.

$p^*$ range (GeV/c)	correlated prod. $\mathcal{B}(B^- \to X_c X)$ (%)	anticorrelated prod. $\mathcal{B}(B^- \to X_{\bar{c}}X)$ (%)
0.00-0.20	$0.19 \pm 0.09 \pm 0.02$	$0.06 \pm 0.06 \pm 0.01$
0.20 - 0.40	$0.59 \pm 0.19 \pm 0.06$	$0.15 \pm 0.15 \pm 0.02$
0.40 - 0.60	$1.43 \pm 0.28 \pm 0.14$	$0.78 \pm 0.22 \pm 0.07$
0.60 - 0.80	$1.81 \pm 0.31 \pm 0.17$	$0.06 \pm 0.20 \pm 0.02$
0.80 - 1.00	$1.27 \pm 0.29 \pm 0.13$	$0.55 \pm 0.21 \pm 0.05$
1.00-1.20	$1.57 \pm 0.27 \pm 0.16$	$0.67 \pm 0.18 \pm 0.06$
1.20 - 1.40	$1.27 \pm 0.23 \pm 0.16$	$0.02 \pm 0.12 \pm 0.03$
1.40-1.60	$0.72 \pm 0.18 \pm 0.15$	$0.04 \pm 0.10 \pm 0.04$
1.60-1.80	$0.69 \pm 0.15 \pm 0.16$	$0.15 \pm 0.09 \pm 0.04$
1.80 - 2.00	$0.33 \pm 0.11 \pm 0.16$	$0.06 \pm 0.06 \pm 0.03$
2.00-2.20	$0.07 \pm 0.07 \pm 0.09$	$0.02 \pm 0.04 \pm 0.03$

TABLE VIII. Correlated and anticorrelated  $D_s$  production in  $B^-$  decays.

$p^*$ range (GeV/c)	correlated prod. $\mathcal{B}(B^- \to X_c X)$ (%)	anticorrelated prod. $\mathcal{B}(B^- \to X_{\bar{c}}X)$ (%)
0.00-0.34 0.34-0.68 0.68-1.02	$-0.09 \pm 0.20 \pm 0.02$ $0.03 \pm 0.20 \pm 0.03$ $0.50 \pm 0.24 \pm 0.10$	$0.50 \pm 0.17 \pm 0.08$ $0.09 \pm 0.25 \pm 0.04$ $1.04 \pm 0.30 \pm 0.16$
1.02–1.36 1.36–1.70 1.70–2.04	$0.57 \pm 0.21 \pm 0.12$ $0.11 \pm 0.12 \pm 0.03$ $0.08 \pm 0.08 \pm 0.02$	$1.09 \pm 0.26 \pm 0.17$ $3.57 \pm 0.35 \pm 0.55$ $2.33 \pm 0.27 \pm 0.36$

TABLE IX. Correlated and anticorrelated  $\Lambda_c^+$  production in  $B^-$  decays.

correlated prod. $\mathcal{B}(B^- \to X_c X)$ (%)	anticorrelated prod. $\mathcal{B}(B^- \to X_{\bar{c}}X)$ (%)
$0.28 \pm 0.12 \pm 0.09$	$0.10 \pm 0.08 \pm 0.03$
	$0.40 \pm 0.20 \pm 0.12$ $0.50 \pm 0.22 \pm 0.15$
$0.72 \pm 0.24 \pm 0.22$	$0.50 \pm 0.22 \pm 0.13$ $0.50 \pm 0.21 \pm 0.15$
$0.28 \pm 0.18 \pm 0.09$	$0.70 \pm 0.23 \pm 0.21$
	$\mathcal{B}(B^- \to X_c X) \ (\%)$ $0.28 \pm 0.12 \pm 0.09$ $0.30 \pm 0.17 \pm 0.09$ $0.48 \pm 0.21 \pm 0.15$ $0.72 \pm 0.24 \pm 0.22$

TABLE X. Correlated and anticorrelated  $D^0$  production in  $\bar{B}^0$  decays.

$p^*$ range (GeV/ $c$ )	correlated prod. $\mathcal{B}(B^- \to X_c X)$ (%)	anticorrelated prod. $\mathcal{B}(B^- \to X_{\bar{c}}X)$ (%)
0.00-0.15	$0.11 \pm 0.12 \pm 0.01$	$0.03 \pm 0.08 \pm 0.01$
0.15-0.30	$0.73 \pm 0.28 \pm 0.03$	$0.45 \pm 0.23 \pm 0.03$
0.30 - 0.45	$1.46 \pm 0.41 \pm 0.07$	$0.60 \pm 0.31 \pm 0.04$
0.45 - 0.60	$2.53 \pm 0.51 \pm 0.11$	$1.56 \pm 0.41 \pm 0.11$
0.60 - 0.75	$3.60 \pm 0.62 \pm 0.16$	$1.71 \pm 0.47 \pm 0.12$
0.75 - 0.90	$4.05 \pm 0.63 \pm 0.20$	$1.64 \pm 0.46 \pm 0.12$
0.90 - 1.05	$5.07 \pm 0.61 \pm 0.23$	$0.90 \pm 0.43 \pm 0.07$
1.05-1.20	$5.50 \pm 0.62 \pm 0.25$	$0.48 \pm 0.40 \pm 0.06$
1.20-1.35	$4.93 \pm 0.56 \pm 0.24$	$0.72 \pm 0.37 \pm 0.08$
1.35-1.50	$5.70 \pm 0.56 \pm 0.27$	$-0.53 \pm 0.29 \pm 0.07$
1.50-1.65	$5.51 \pm 0.53 \pm 0.27$	$0.45 \pm 0.33 \pm 0.09$
1.65-1.80	$2.85 \pm 0.40 \pm 0.23$	$0.19 \pm 0.24 \pm 0.07$
1.80-1.95	$2.71 \pm 0.37 \pm 0.19$	$-0.03 \pm 0.19 \pm 0.06$
1.95-2.10	$2.17 \pm 0.32 \pm 0.16$	$0.04 \pm 0.17 \pm 0.05$
2.10-2.25	$0.58 \pm 0.18 \pm 0.11$	$-0.14 \pm 0.10 \pm 0.02$

[1] Charge conjugation is implied for all decay processes mentioned in this paper.

TABLE XI. Correlated and anticorrelated  $D^+$  production in  $\bar{B}^0$  decays.

$p^*$ range (GeV/c)	correlated prod. $\mathcal{B}(B^- \to X_c X)$ (%)	anticorrelated prod. $\mathcal{B}(B^- \to X_{\bar{c}}X)$ (%)
0.00-0.20	$0.08 \pm 0.12 \pm 0.01$	$0.05 \pm 0.11 \pm 0.01$
0.20-0.40	$1.10 \pm 0.37 \pm 0.09$	$0.42 \pm 0.28 \pm 0.07$
0.40 - 0.60	$0.97 \pm 0.47 \pm 0.08$	$0.68 \pm 0.36 \pm 0.11$
0.60 - 0.80	$2.47 \pm 0.54 \pm 0.19$	$0.08 \pm 0.36 \pm 0.02$
0.80 - 1.00	$2.70 \pm 0.54 \pm 0.21$	$-0.06 \pm 0.34 \pm 0.02$
1.00-1.20	$3.49 \pm 0.53 \pm 0.28$	$0.76 \pm 0.37 \pm 0.12$
1.20-1.40	$4.92 \pm 0.54 \pm 0.39$	$-0.14 \pm 0.30 \pm 0.04$
1.40-1.60	$5.41 \pm 0.52 \pm 0.44$	$0.12 \pm 0.31 \pm 0.04$
1.60-1.80	$5.50 \pm 0.51 \pm 0.45$	$0.33 \pm 0.31 \pm 0.06$
1.80 - 2.00	$5.54 \pm 0.49 \pm 0.45$	$-0.32 \pm 0.25 \pm 0.06$
2.00-2.20	$3.08 \pm 0.37 \pm 0.25$	$0.39 \pm 0.23 \pm 0.06$
2.20-2.40	$1.63 \pm 0.26 \pm 0.13$	$-0.01 \pm 0.14 \pm 0.01$

TABLE XII. Correlated and anticorrelated  $D_s$  production in  $\bar{B}^0$  decays.

$p^*$ range (GeV/c)	correlated prod. $\mathcal{B}(B^- \to X_c X)$ (%)	anticorrelated prod. $\mathcal{B}(B^- \to X_{\bar{c}}X)$ (%)
0.00-0.34 0.34-0.68 0.68-1.02 1.02-1.36 1.36-1.70 1.70-2.04	$-0.23 \pm 0.14 \pm 0.03$ $0.69 \pm 0.46 \pm 0.10$ $0.03 \pm 0.43 \pm 0.01$ $1.03 \pm 0.47 \pm 0.16$ $-0.10 \pm 0.32 \pm 0.03$ $0.22 \pm 0.25 \pm 0.04$	$0.07 \pm 0.17 \pm 0.02$ $1.29 \pm 0.49 \pm 0.20$ $2.10 \pm 0.52 \pm 0.32$ $1.81 \pm 0.47 \pm 0.28$ $3.88 \pm 0.57 \pm 0.60$ $2.10 \pm 0.40 \pm 0.32$

TABLE XIII. Correlated and anticorrelated  $\Lambda_c^+$  production in  $\bar{B}^0$  decays.

$p^*$ range (GeV/ $c$ )	correlated prod. $\mathcal{B}(B^- \to X_c X)$ (%)	anticorrelated prod. $\mathcal{B}(B^- \to X_{\bar{c}}X)$ (%)
0.00-0.24	$0.01 \pm 0.11 \pm 0.01$	$0.14 \pm 0.16 \pm 0.05$
0.24 - 0.48	$0.46 \pm 0.34 \pm 0.15$	$0.57 \pm 0.33 \pm 0.19$
0.48 - 0.72	$0.73 \pm 0.38 \pm 0.23$	$0.34 \pm 0.31 \pm 0.12$
0.72 - 0.96	$1.90 \pm 0.51 \pm 0.60$	$-0.24 \pm 0.30 \pm 0.08$
0.96 - 1.20	$0.73 \pm 0.40 \pm 0.23$	$0.94 \pm 0.36 \pm 0.32$
1.20-1.44	$0.96 \pm 0.35 \pm 0.30$	$-0.19 \pm 0.17 \pm 0.07$
1.44-1.68	$0.21 \pm 0.19 \pm 0.07$	$-0.01 \pm 0.13 \pm 0.01$

<sup>[2]</sup> W.-M. Yao et al. (Particle Data Group), J. Phys. G 33, 1 (2006).

<sup>[3]</sup> E. Bagan et al., Phys. Lett. B 351, 546 (1995).

<sup>[4]</sup> G. Buchalla et al., Phys. Lett. B 364, 188 (1995).

<sup>[5]</sup> M. Neubert, 17th Int. Symposium on Lepton-Photon Interactions, 1995, Beijing, China (World Scientific, Singapore, 1995), p. 298.

<sup>[6]</sup> A. Lenz, hep-ph/0011258 and references therein.

- [7] ALEPH, CDF, DELPHI, L3, OPAL, SLD combined results, hep-ex/0112028.
- [8] L. Gibbons *et al.* (CLEO collaboration), Phys. Rev. D 56, 3783 (1997).
- [9] T.E. Coan *et al.* (CLEO collaboration), Phys. Rev. Lett. 80, 1150 (1998).
- [10] B. Aubert *et al.* (BABAR collaboration), Phys. Rev. D 70, 091106(R) (2004).
- [11] B. Aubert *et al.* (BABAR collaboration), Phys. Rev. D 74, 091105(R) (2006).
- [12] J. Abdallah *et al.* (DELPHI collaboration), Phys. Lett. B **561**, 26 (2003).
- [13] R. Ammar *et al.* (CLEO collaboration), Phys. Rev. D 55, 13 (1997).
- [14] R. Seuster *et al.* (BELLE collaboration), Phys. Rev. D 73, 032002 (2006).
- [15] R. Barate *et al.* (ALEPH collaboration), Eur. Phys. J. C 4, 387 (1998).
- [16] B. Aubert *et al.* (BABAR collaboration), Phys. Rev. D 68, 092001 (2003).
- [17] R. Chistov *et al.* (BELLE collaboration), Phys. Rev. D 74, 111105 (2006).
- [18] C. W. Bauer, B. Grinstein, D. Pirjol, and I. W. Stewart, Phys. Rev. D **67**, 014010 (2003).
- [19] I. Bigi, L. Maiani, F. Piccinini, A.D. Polosa, and V. Riquer, Phys. Rev. D 72, 114016 (2005).
- [20] B. Aubert et al. (BABAR collaboration), Nucl. Instr. Methods Phys. Res., Sect. A 479, 1 (2002).

- [21] S. Agostinelli et al. (GEANT4 Collaboration), Nucl. Instr. Methods Phys. Res., Sect. A 506, 250 (2003).
- [22] T. Skwarnicki et al. (CRYSTAL BALL collaboration), DESY Report No. F31-86-02 (unpublished).
- [23] H. Albrecht *et al.* (ARGUS collaboration), Z. Phys. C 48, 543 (1990).
- [24] S. Eidelman *et al.* (Particle Data Group), Phys. Lett. B 592, 1 (2004).
- [25] We consider any  $K^+K^-$  combination with an invariant mass in the range  $1010.6 < m_{K^+K^-} < 1028.6 \text{ MeV}/c^2$  to be a  $\phi$  meson when reconstructing the  $D_s^+ \to \phi (\to K^+K^-)\pi^+$  decay.
- [26] In some cases, a satellite contribution needs to be added. It includes a reflection from  $D^0 \to K^-K^+$  in the  $D^0 \to K^-\pi^+$  mass spectra and a signal at the  $D^+$  mass (from  $D^+ \to \phi \pi^+$ ,  $\bar{K}^{*0}K^+$ ,  $K_S^0K^+$  Cabibbo-suppressed decays) in the  $D_S$  mass spectra.
- [27] B. Barish *et al.* (CLEO collaboration), Phys. Rev. Lett. **79**, 3599 (1997).
- [28] We also neglect the contribution of the  $\bar{B} \to D\Lambda^0 \bar{\Lambda}_c^-$  decays because of the very small phase space available.
- [29] N. Gabyshev *et al.* (BELLE collaboration), Phys. Rev. Lett. **97**, 202003 (2006).
- [30] M. Beneke et al., Phys. Rev. D 59, 054003 (1999).
- [31] Assuming isospin conservation, we have also:  $x = \mathcal{B}_{\text{dir}}(\bar{B}^0 \to \bar{D}^0 + D^- X) \times \frac{\tau_{B^+}}{\tau_{B^0}}$  and  $x^* = \mathcal{B}(\bar{B}^0 \to \bar{D}^{*0} + D^{*-} X) \times \frac{\tau_{B^+}}{\tau_{B^0}}$ .