Branching fraction and $\boldsymbol{C P}$-violation charge asymmetry measurements for $\boldsymbol{B}$-meson decays to $\boldsymbol{\eta} K^{ \pm}, \boldsymbol{\eta} \boldsymbol{\pi}^{ \pm}, \boldsymbol{\eta}^{\prime} K, \boldsymbol{\eta}^{\prime} \boldsymbol{\pi}^{ \pm}, \omega K$, and $\omega \boldsymbol{\pi}^{ \pm}$
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[^0]We present measurements of the branching fractions for $B^{0}$-meson decays to $\eta^{\prime} K^{0}$ and $\omega K^{0}$, and of the branching fractions and $C P$-violation charge asymmetries for $B^{+}$-meson decays to $\eta \pi^{+}, \eta K^{+}, \eta^{\prime} \pi^{+}$, $\eta^{\prime} K^{+}, \omega \pi^{+}$, and $\omega K^{+}$. The data, collected with the BABAR detector at the Stanford Linear Accelerator Center, represent $383 \times 10^{6} B \bar{B}$ pairs produced in $e^{+} e^{-}$annihilation. The measurements agree with previous results; we find no evidence for direct $C P$ violation.

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Charmless $B$ decays are becoming increasingly useful to test the accuracy of theoretical estimation methods, such as those based on QCD factorization [1-3] or flavor $\operatorname{SU}(3)$ symmetry [4-6]. In this paper we present measurements of branching fractions and, where applicable, charge asymmetries, for eight charmless $B$ decays (and their charge conjugates, implied throughout the paper): $B^{+} \rightarrow \eta \pi^{+}$, $B^{+} \rightarrow \eta K^{+}, \quad B^{+} \rightarrow \eta^{\prime} \pi^{+}, \quad B^{+} \rightarrow \eta^{\prime} K^{+}, \quad B^{0} \rightarrow \eta^{\prime} K^{0}$, $B^{+} \rightarrow \omega \pi^{+}, B^{+} \rightarrow \omega K^{+}$, and $B^{0} \rightarrow \omega K^{0}$. The results presented here represent improvement in precision over previous measurements of these quantities by $B A B A R$ [79], Belle [10-12], and CLEO [13]. We previously reported a branching fraction limit for $B^{0} \rightarrow \eta K^{0}$ [14], and $C P$ asymmetries for $B^{0} \rightarrow \eta^{\prime} K^{0}$ and $B^{0} \rightarrow \omega K^{0}[9,15]$.

Charmless $B$ decays with kaons are usually expected to be dominated by $b \rightarrow s$ loop ("penguin") amplitudes, while $b \rightarrow u$ tree amplitudes typically dominate for the decays with pions. However, the $B \rightarrow \eta K$ decays are especially interesting since they are suppressed relative to the abundant $B \rightarrow \eta^{\prime} K$ decays due to destructive interference between two penguin amplitudes [16]. The Cabibbo-Kobayashi-Maskawa (CKM)-suppressed $b \rightarrow u$ tree amplitudes may interfere significantly with $b \rightarrow s$ penguin amplitudes of similar magnitudes, possibly leading to large direct $C P$ violation in $B^{+} \rightarrow \eta \pi^{+}$and $B^{+} \rightarrow$ $\eta^{\prime} \pi^{+}$[17]; numerical estimates are available in a few cases [2-4,18]. We search for such direct $C P$ violation by measuring the charge asymmetry $\mathcal{A}_{\mathrm{ch}} \equiv\left(\Gamma^{-}-\Gamma^{+}\right) /\left(\Gamma^{-}+\right.$ $\left.\Gamma^{+}\right)$in the rates $\Gamma^{ \pm}=\Gamma\left(B^{ \pm} \rightarrow f^{ \pm}\right)$for each charged final state $f^{ \pm}$.

Finally, phenomenological fits to the branching fractions and charge asymmetries of charmless $B$ decays can be used to understand the relative importance of tree and penguin contributions and may provide sensitivity to the CKM angle $\gamma[4-6,19]$, or to the effect of non-standard-model heavy particles in the loops [20].

The results presented here are based on data collected with the BABAR detector [21] at the PEP-II $e^{+} e^{-}$collider [22] located at the Stanford Linear Accelerator Center. An integrated luminosity of $347 \mathrm{fb}^{-1}$, corresponding to $383 \times$ $10^{6} B \bar{B}$ pairs, was recorded at the $Y(4 S)$ resonance (center-of-mass energy $\sqrt{s}=10.58 \mathrm{GeV}$ ).

Charged particles from the $e^{+} e^{-}$interactions are detected, and their momenta measured, by a combination of five layers of double-sided silicon microstrip detectors and a 40-layer drift chamber, both operating in the 1.5 T magnetic field of a superconducting solenoid. Photons and electrons are identified with a $\operatorname{CsI}(\mathrm{Tl})$ electromagnetic
calorimeter (EMC). Further charged particle identification (PID) is provided by the average energy loss $(d E / d x)$ in the tracking devices and by an internally reflecting ring imaging Cherenkov detector (DIRC) covering the central region.

We establish the event selection criteria with the aid of a detailed Monte Carlo (MC) simulation of the $B$ production and decay sequences, and of the detector response [23]. These criteria are designed to retain signal events with high efficiency. When applied to the data, they result in a sample much larger than the expected signal, but with wellcharacterized backgrounds. We extract the signal yields from this sample with a maximum likelihood (ML) fit.

The $B$-daughter candidates are reconstructed through their decays $\quad \pi^{0} \rightarrow \gamma \gamma, \quad K^{0} \rightarrow K_{S}^{0} \rightarrow \pi^{+} \pi^{-}, \quad \omega \rightarrow$ $\pi^{+} \pi^{-} \pi^{0}, \quad \eta \rightarrow \gamma \gamma \quad\left(\eta_{\gamma \gamma}\right), \eta \rightarrow \pi^{+} \pi^{-} \pi^{0}\left(\eta_{3 \pi}\right), \quad \eta^{\prime} \rightarrow$ $\eta_{\gamma \gamma} \pi^{+} \pi^{-}\left(\eta_{\eta \pi \pi}^{\prime}\right)$, and $\eta^{\prime} \rightarrow \rho^{0} \gamma\left(\eta_{\rho \gamma}^{\prime}\right)$, where $\rho^{0} \rightarrow$ $\pi^{+} \pi^{-}$. The invariant mass of these particles' final states are required to lie within about 2 standard deviations of the nominal mass [24] unless the mass is an observable in the ML fit, in which case we accept a wider range. For a $K_{S}^{0}$ candidate we require a successful fit of the decay vertex with the flight direction constrained to the pion pair momentum direction, yielding a flight length greater than 3 times its uncertainty. Secondary charged pions in $\eta^{\prime}, \eta$, and $\omega$ candidates are rejected if classified as protons, kaons, or electrons by their DIRC, $d E / d x$, and EMC PID signatures. For the primary charged track in $B^{+}$decays we define the PID variables $S_{\pi}$ and $S_{K}$ as the number of standard deviations between the measured DIRC Cherenkov angle and that expected for pions and kaons, respectively. We include these observables in the ML fits to distinguish between primary $\pi$ and $K$. For $B^{+} \rightarrow \eta^{\prime} K^{+}$the backgrounds, including cross feed from the pion channel, are small. For this mode we perform a dedicated fit with less restrictive continuum background rejection (see below), and $S_{K}<2$ to exclude pions (and lighter particles).

We reconstruct the $B$-meson candidate by combining the four-momenta of a pair of daughter mesons with a vertex constraint if the ultimate final state includes at least two charged particles. Since the natural widths of the $\eta, \eta^{\prime}$, and $\pi^{0}$ are much smaller than the resolution, we also constrain their masses to nominal values [24] in the fit of the $B$ candidate. From the kinematics of $Y(4 S)$ decay we determine the energy-substituted mass $m_{\mathrm{ES}}=\sqrt{\frac{1}{4} s-\mathbf{p}_{B}^{2}}$ and energy difference $\Delta E=E_{B}-\frac{1}{2} \sqrt{s}$, where $\left(E_{B}, \mathbf{p}_{B}\right)$ is the $B$-meson four-momentum vector, and all values are ex-
pressed in the $Y(4 S)$ frame. The resolution in $m_{\mathrm{ES}}$ is 3.0 MeV and in $\Delta E$ is $24-50 \mathrm{MeV}$, depending on the decay mode. We require $5.25<m_{\mathrm{ES}}<5.29 \mathrm{GeV}$ and $|\Delta E|<$ 0.2 GeV .

Backgrounds arise primarily from random combinations of particles in continuum $e^{+} e^{-} \rightarrow q \bar{q}$ events $(q=u, d, s$, $c)$. We reduce these with requirements on the angle $\theta_{\mathrm{T}}$ between the thrust axis of the $B$ candidate in the $Y(4 S)$ frame and that of the rest of the charged tracks and neutral calorimeter clusters in the event. The distribution is sharply peaked near $\left|\cos \theta_{\mathrm{T}}\right|=1$ for $q \bar{q}$ jet pairs, and nearly uniform for $B$-meson decays. We require $\left|\cos \theta_{\mathrm{T}}\right|<0.90$ ( $<0.65$ for $\eta_{\rho \gamma}^{\prime} \pi^{+},<0.80$ for $\omega \pi^{+}$and $\omega K^{+}$), which optimizes the expected signal yield relative to its background-dominated statistical error. In the ML fit we discriminate further against $q \bar{q}$ background with a Fisher discriminant $\mathcal{F}$ that combines several variables which


FIG. 1 (color online). Plots of signal-enhanced subsets of the data distribution for $B^{+} \rightarrow \omega K^{+}$projected on each of the fit variables: (a) $m_{E S}$, (b) $\Delta E$, (c) $\mathcal{F}$, (d) $\mathcal{H}^{\omega}$, (e) $\omega$ mass, and (f) $S_{\pi}$. Points with errors represent the data, solid curves the full fit functions, dashed curves the sum of the background functions, and dot-dashed curves the signal from $B^{+} \rightarrow \omega \pi^{+}$. The variable $\Delta E$ is computed with the pion mass.
characterize the energy flow in the event [25]. It provides about 1 standard deviation of separation between $B$ decay events and $q \bar{q}$ background [see Fig. 1(c)].

We also impose restrictions on resonance decay angles to exclude the most asymmetric decays where soft-particle backgrounds accumulate and the acceptance changes rapidly. We define the decay angle $\theta_{\text {dec }}^{r}$ for a meson $r$ that decays to two particles as the angle between the momenta of a daughter particle and the meson's parent, measured in the meson's rest frame. We define $\mathcal{H}^{r} \equiv \cos \theta_{\text {dec }}^{r}$ and require $\left|\mathcal{H}^{\rho^{0}}\right|<0.9$ for $B \rightarrow \eta_{\rho \gamma}^{\prime} K$ and $\left|\mathcal{H}^{\rho^{0}}\right|<0.7$ for $B^{+} \rightarrow \eta_{\rho \gamma}^{\prime} \pi^{+}$. For the three-body $\omega \rightarrow 3 \pi$ mode the direction for the decay is the normal to the decay plane, and we include $\mathcal{H}^{\omega}$ as an observable in the ML fit.

The average number of candidates found per selected event is in the range 1.05 to 1.13 , depending on the final state. We choose the candidate with the daughter resonance mass closest to the nominal value. From the simulation we find that this algorithm selects the correct-combination candidate in about two-thirds of the events containing multiple candidates, and that it induces negligible bias in the ML fits.

We obtain yields for each channel from an extended maximum likelihood fit with the input observables $\Delta E$, $m_{\mathrm{ES}}, \mathcal{F}, m_{r}$ (the invariant mass of the $\eta, \eta^{\prime}$, or $\omega$ candidate), and, for charged decays other than $B^{+} \rightarrow \eta^{\prime} K^{+}$, the PID variables $S_{\pi}$ and $S_{K}$. The selected data sample sizes are given in the second column of Table I. Besides the signal events they contain $q \bar{q}$ (dominant) and $B \bar{B}$ with $b \rightarrow$ $c$ combinatorial background, and a fraction of background from other charmless $B \bar{B}$ modes, which we estimate from the simulation to be less than $2 \%$ of the total fit sample. The latter events have ultimate final states different from the signal, but with similar kinematics so that broad peaks near those of the signal appear in some observables, requiring a separate component in the probability density function (PDF). The yield of this component is free in the fit for all cases except $B^{0} \rightarrow \omega K_{S}^{0}$, where the fit stability requires fixing the yield to the expectation from MC. The likelihood function is

$$
\begin{align*}
\mathcal{L}= & \exp \left(-\sum_{j, k} Y_{j k}\right) \prod_{i}^{N} \sum_{j, k} Y_{j k} \mathcal{P}_{j}\left(m_{\mathrm{ES}}{ }^{i}\right) \mathcal{P}_{j}\left(\mathcal{F}^{i}\right) \mathcal{P}_{j}\left(\Delta E_{k}^{i}\right) \\
& \times\left[\mathcal{P}_{j}\left(S_{k}^{i}\right) \mathcal{P}_{j}\left(m_{r}^{i}\right) \mathcal{P}_{j}\left(\mathcal{H}_{r}^{i}\right)\right], \tag{1}
\end{align*}
$$

where $N$ is the number of events in the sample, and for each component $j$ (signal, combinatorial background, or charmless $B \bar{B}$ background) and flavor $k$ (primary $K^{+}$or $\pi^{+}$), $Y_{j k}$ is the yield of events and $\mathcal{P}_{j}\left(x_{k}^{i}\right)$ the PDF for observable $x_{k}$ in event $i$. Some factors in [] are omitted for some modes. The flavor-dependent factors $\mathcal{P}_{j}\left(\Delta E_{k}^{i}\right)$ and $\mathcal{P}_{j}\left(S_{k}^{i}\right)$ take common functional forms for the pion or kaon, e.g., $F_{j}\left(\Delta E_{\pi}^{i}\right)$ or $F_{j}\left(\Delta E_{K}^{i}=\Delta E_{\pi}^{i}+\delta \Delta E\left(\mathbf{p}^{i}\right)\right)$, where $\mathbf{p}$ is the primary-track momentum; $S_{k}^{i}$ is treated similarly. For the modes $B \rightarrow \eta_{\eta \pi \pi}^{\prime} K$ we found no need for the $B \bar{B}$ back-

TABLE I. Number of events $N$ in the sample, fitted signal yield $Y_{S}$, and measured bias (to be subtracted from $Y_{S}$ ) in events (ev.), detection efficiency $\epsilon$, daughter branching fraction product ( $\Pi \mathcal{B}_{i}$ ), and measured branching fraction $\mathcal{B}$ and charge asymmetry $\mathcal{A}_{\text {ch }}$ with statistical errors for each decay chain, and for the combined measurements the branching fraction and charge asymmetry with statistical and systematic error. The number of produced $B \bar{B}$ pairs is given in the text.

| Mode | $N$ (ev.) | $Y_{S}(\mathrm{ev}$. | Bias (ev.) | $\epsilon(\%)$ | $\Pi \mathcal{B}_{i}(\%)$ | $\mathcal{B}\left(10^{-6}\right)$ | $\mathcal{A}_{\text {ch }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{\eta} \boldsymbol{\pi}^{+}$ |  |  |  |  |  | $\mathbf{5 . 0} \pm 0.5 \pm 0.3$ | $\mathbf{- 0 . 0 8} \pm \mathbf{0 . 1 0} \pm \mathbf{0 . 0 1}$ |
| $\eta_{\gamma \gamma} \pi^{+}$ | 44883 | $258{ }_{-29}^{+30}$ | $6 \pm 3$ | 34.1 | 39.4 | $4.9 \pm 0.6$ | $-0.05 \pm 0.12$ |
| $\eta_{3 \pi} \pi^{+}$ | 22333 | $115_{-19}^{+20}$ | $6 \pm 3$ | 23.8 | 22.6 | $5.5 \pm 1.0$ | $-0.13 \pm 0.18$ |
| $\boldsymbol{\eta} \boldsymbol{K}^{+}$ |  |  |  |  |  | $\mathbf{3 . 7} \pm \mathbf{0 . 4} \pm 0.1$ | $\mathbf{- 0 . 2 2} \pm \mathbf{0 . 1 1} \pm 0.01$ |
| $\eta_{\gamma \gamma} K^{+}$ | 44883 | $197{ }_{-24}^{+25}$ | $6 \pm 3$ | 32.7 | 39.4 | $3.9 \pm 0.5$ | $-0.25 \pm 0.13$ |
| $\eta_{3 \pi} K^{+}$ | 22333 | $71_{-15}^{+16}$ | $4 \pm 2$ | 23.2 | 22.6 | $3.3 \pm 0.8$ | $-0.15 \pm 0.23$ |
| $\boldsymbol{\eta}^{\prime} \boldsymbol{\pi}^{+}$ |  |  |  |  |  | $3.9 \pm 0.7 \pm 0.3$ | $\mathbf{0 . 2 1} \pm 0.17 \pm 0.01$ |
| $\eta_{\eta \pi \pi}^{\prime} \pi^{+}$ | 16879 | $88_{-15}^{+16}$ | $14 \pm 3$ | 27.2 | 17.5 | $4.0 \pm 0.9$ | $0.14 \pm 0.20$ |
| $\eta_{\rho \gamma}^{\prime} \pi^{+}$ | 35523 | $97_{-22}^{+23}$ | $23 \pm 7$ | 18.4 | 29.4 | $3.6 \pm 1.1$ | $0.35 \pm 0.30$ |
| $\boldsymbol{\eta}^{\prime} \boldsymbol{K}^{+}$ |  |  |  |  |  | $\mathbf{7 0 . 0} \pm \mathbf{1 . 5} \pm \mathbf{2 . 8}$ | $\mathbf{0 . 0 1 0} \pm \mathbf{0 . 0 2 2} \pm \mathbf{0 . 0 0 6}$ |
| $\eta_{\eta \pi \pi}^{\prime} K^{+}$ | 3170 | $1060 \pm 35$ | $0 \pm 1$ | 23.2 | 17.5 | $68.2 \pm 2.3$ | $-0.005 \pm 0.033$ |
| $\eta_{\rho \gamma}^{\prime} K^{+}$ | 79501 | $2405 \pm 69$ | $31 \pm 16$ | 29.2 | 29.4 | $72.2 \pm 2.1$ | $0.022 \pm 0.028$ |
| $\boldsymbol{\eta}^{\prime} \boldsymbol{K}^{\mathbf{0}}$ |  |  |  |  |  | $\mathbf{6 6 . 6} \pm \mathbf{2 . 6} \pm \mathbf{2 . 8}$ | (see [15]) |
| $\eta_{\eta \pi \pi}^{\prime} K^{0}$ | 1100 | $329 \pm 20$ | $3 \pm 1$ | 23.2 | 6.1 | $60.7 \pm 3.7$ | . . . |
| $\eta_{\rho \gamma}^{\prime} K^{0}$ | 19927 | $831 \pm 38$ | $35 \pm 17$ | 28.0 | 10.2 | $72.8 \pm 3.5$ | $\cdots$ |
| $\boldsymbol{\omega} \boldsymbol{\pi}^{+}$ | 76735 | $516 \pm 38$ | $44 \pm 22$ | 20.5 | 89.1 | $6.7 \pm 0.5 \pm 0.4$ | $-\mathbf{0 . 0 2} \pm 0.08 \pm 0.01$ |
| $\omega K^{+}$ | 76735 | $457 \pm 32$ | $29 \pm 15$ | 20.0 | 89.1 | $6.3 \pm 0.5 \pm 0.3$ | $-\mathbf{0 . 0 1} \pm 0.07 \pm 0.01$ |
| $\omega K^{0}$ | 15914 | $146 \pm 18$ | $10 \pm 5$ | 21.2 | 30.8 | $5.4 \pm 0.8 \pm 0.3$ | (see [9]) |

ground component. The factored form of the PDF indicated in Eq. (1) is a good approximation, particularly for the $q \bar{q}$ component, since correlations among observables


FIG. 2 (color online). Plots of signal-enhanced subsets of the data distributions projected onto $m_{\mathrm{ES}}$ for the decays:
(a) $B^{+} \rightarrow \eta \pi^{+}$,
(b) $B^{+} \rightarrow \eta K^{+}$,
(c) $B^{+} \rightarrow \eta^{\prime} \pi^{+}$,
(d) $B^{+} \rightarrow \eta^{\prime} K^{+}$,
(e) $\quad B^{0} \rightarrow \eta^{\prime} K^{0}$,
(f) $B^{+} \rightarrow \omega \pi^{+}$,
(g) $B^{+} \rightarrow \omega K^{+}$, and (h) $B^{0} \rightarrow \omega K^{0}$. The solid line represents the result of the fit, and the dot-dashed line the background contribution. The dashed line gives the sum of background and the $\eta_{3 \pi}[(\mathrm{a}),(\mathrm{b})]$ or $\eta_{\eta \pi \pi}^{\prime}$ [(c)-(e)] component of the signal. The dotted line shows the $K$ or $\pi$ cross-feed component, where applicable.
measured in the data are typically a few percent or less. Distortions of the fit results caused by our approximations are measured in simulation and included in the bias corrections and systematic errors discussed below.

We determine the PDFs for the signal and $B \bar{B}$ background components from fits to MC samples. We calibrate the resolutions in $\Delta E$ and $m_{\mathrm{ES}}$ with large data control samples of $B$ decays to charmed final states of similar topology [e.g. $B \rightarrow D(K \pi \pi) \pi$ ]. We develop PDFs for the combinatorial background with fits to the data from which the signal region $\left(5.27 \mathrm{GeV}<m_{\mathrm{ES}}<5.29 \mathrm{GeV}\right.$ and $|\Delta E|<0.1 \mathrm{GeV}$ ) has been excluded.

We use the following functional forms for the PDFs: the sum of two Gaussians for $\mathcal{P}_{\text {sig }}\left(m_{\mathrm{ES}}\right), \mathcal{P}_{\text {sig, } B \bar{B}}(\Delta E)$, and the sharper structures in $\mathcal{P}_{B \bar{B}}\left(m_{\mathrm{ES}}\right)$ and $\mathcal{P}_{j}\left(m_{r}\right)$; linear or quadratic dependences for combinatorial components of $\mathcal{P}_{B \bar{B}, q \bar{q}}\left(m_{r}\right)$ and for $\mathcal{P}_{q \bar{q}}(\Delta E)$; and a Gaussian function with separate low- and high-side width parameters for $\mathcal{P}_{j}(\mathcal{F})$. The $q \bar{q}$ background in $m_{\mathrm{ES}}$ is described by the threshold function $x \sqrt{1-x^{2}} \exp \left[-\xi\left(1-x^{2}\right)\right]$, with $x \equiv 2 m_{\mathrm{ES}} / \sqrt{s}$ and parameter $\xi$. These functions are discussed in more detail in [25], and some of them are illustrated in Fig. 1.

We allow the parameters most important for the determination of the background PDFs to vary in the fit, along with the yields for all components, and for charged modes the signal and $q \bar{q}$ background charge asymmetries. Specifically, the free background parameters are most or all of the following, depending on the decay mode: $\xi$ for $m_{\mathrm{ES}}$, linear and quadratic coefficients for $\Delta E$, area and slope of the combinatorial component for $m_{r}$, and the
mean, width, and width difference parameters for $\mathcal{F}$. Results for the signal yields are presented in the third column of Table I for each sample.

We validate the fitting procedure by applying it to ensembles of simulated $q \bar{q}$ experiments drawn from the PDF into which we have embedded the expected number of signal and $B \bar{B}$ background events randomly extracted from the fully simulated MC samples. Biases obtained by this procedure with inputs that reproduce the yields found in the data are reported in the fourth column of Table I.

In Fig. 1 we show, as a representative of the fits, the projections of the PDF and data for the $B^{+} \rightarrow \omega K^{+}$fit, and in Fig. 2 projections onto $m_{\mathrm{ES}}$ for each of the eight decays, with submodes combined. The data plotted are subsamples enriched in signal with a threshold requirement on the ratio of signal to total likelihood (computed without the plotted variable) that retains $35 \%-80 \%$ of the signal, depending on the mode.

We determine the reconstruction efficiencies as the ratio of reconstructed and accepted events in simulation to the number generated. We compute the branching fraction for each channel by subtracting the fit bias from the measured yield, and dividing the result by the efficiency (including secondary branching fractions) and the number of produced $B \bar{B}$ pairs [25]. We assume equal decay rates of the $Y(4 S)$ to $B^{+} B^{-}$and $B^{0} \bar{B}^{0}$. Table I gives the numbers pertinent to these computations. The statistical error on the signal yield or branching fraction is taken as the change in the central value when the quantity $-2 \ln \mathcal{L}$ increases by one unit from its minimum value.

We combine results where we have multiple decay channels by adding the functions $-2 \ln \left\{\left[\mathcal{L}(\mathcal{B}) / \mathcal{L}\left(\mathcal{B}_{0}\right)\right] \otimes\right.$ $\left.G\left(\sigma^{\prime}\right)\right\}$, where $\mathcal{B}_{0}$ is the central value from the fit for each decay channel, and $\otimes G$ denotes convolution with a Gaussian function to include the systematic error $\sigma^{\prime}$ discussed below. We give the resulting final branching fractions for each mode in Table I.

Systematic uncertainties on the branching fractions arise from the PDFs, $B \bar{B}$ backgrounds, fit bias, and efficiency. PDF uncertainties not already accounted for by free parameters in the fit are estimated from the consistency of fits to MC and data in control modes. Varying the signal-PDF parameters within these errors, we estimate yield uncertainties of $0.4 \%-2.2 \%$, depending on the mode. For the $B \bar{B}$ backgrounds we vary the input branching fractions within their uncertainties for the modes that contribute most to the selected sample. The resulting changes in the signal yield are taken in quadrature and scaled to the total of all modes to determine the systematic uncertainty. For the $\eta_{\eta \pi \pi}^{\prime} K$ modes, where no $B \bar{B}$ component is used, we use $10 \%$ of the expected $B \bar{B}$ background in the sample, as this is the typical correlation with the signal yield. For $\omega K_{S}^{0}$ where the $B \bar{B}$ yield is fixed, we take as a systematic uncertainty the average change in the signal yield when the $B \bar{B}$ yield is varied between zero and twice the nominal value. The
uncertainty of the bias (Table I) is a quadrature sum of its components: the statistical uncertainty from the simulated experiments, and half of the corrections attributable to correlations omitted from the signal and $B \bar{B}$ background models, and to PID of the primary charged track. The primary-track PID correction is significant only for misidentified kaons from $B^{+} \rightarrow \eta^{\prime} K^{+}$in the $B^{+} \rightarrow \eta^{\prime} \pi^{+}$ channels.

Uncertainties in our knowledge of the efficiency, found from auxiliary studies, include $0.5 \% \times N_{t}$ and $1.5 \% \times N_{\gamma}$, where $N_{t}$ and $N_{\gamma}$ are the number of tracks and photons, respectively, in the $B$ candidate. The uncertainty in the total number of $B \bar{B}$ pairs in the data sample is $1.1 \%$. Published data [24] provide the uncertainties in the $B$-daughter product branching fractions $(0.7 \%-3.2 \%)$. The uncertainties in the efficiency from the event selection are below $0.5 \%$.

For the measurements of $\mathcal{A}_{\mathrm{ch}}$, biases arise, in principle, from charge-dependent effects in the track reconstruction or particle identification, or from imperfect modeling of the interactions with material in the detector. We study these by comparing this effect in MC for the signal, $q \bar{q}$ background in the data, and control samples mentioned previously. We apply corrections, and assign systematic errors, to $\mathcal{A}_{\text {ch }}$ equal to $-0.010 \pm 0.005$ for modes with a primary kaon and $0.000 \pm 0.005$ for those with a primary pion. We apply an additional correction with uncertainty for dilution of the $\mathcal{A}_{\text {ch }}$ measurement associated with the yield bias, which is significant only for $B^{+} \rightarrow \eta_{\eta \pi \pi}^{\prime} \pi^{+}$. This is obtained from the same MC studies that are used to estimate the yield bias.

After combining the measurements, we obtain for the branching fractions

$$
\begin{aligned}
\mathcal{B}\left(B^{+} \rightarrow \eta \pi^{+}\right) & =(5.0 \pm 0.5 \pm 0.3) \times 10^{-6} \\
\mathcal{B}\left(B^{+} \rightarrow \eta K^{+}\right) & =(3.7 \pm 0.4 \pm 0.1) \times 10^{-6} \\
\mathcal{B}\left(B^{+} \rightarrow \eta^{\prime} \pi^{+}\right) & =(3.9 \pm 0.7 \pm 0.3) \times 10^{-6} \\
\mathcal{B}\left(B^{+} \rightarrow \eta^{\prime} K^{+}\right) & =(70.0 \pm 1.5 \pm 2.8) \times 10^{-6} \\
\mathcal{B}\left(B^{0} \rightarrow \eta^{\prime} K^{0}\right) & =(66.6 \pm 2.6 \pm 2.8) \times 10^{-6} \\
\mathcal{B}\left(B^{+} \rightarrow \omega \pi^{+}\right) & =(6.7 \pm 0.5 \pm 0.4) \times 10^{-6} \\
\mathcal{B}\left(B^{+} \rightarrow \omega K^{+}\right) & =(6.3 \pm 0.5 \pm 0.3) \times 10^{-6} \\
\mathcal{B}\left(B^{0} \rightarrow \omega K^{0}\right) & =(5.4 \pm 0.8 \pm 0.3) \times 10^{-6}
\end{aligned}
$$

For the charge asymmetries we find

$$
\begin{aligned}
& \mathcal{A}_{\mathrm{ch}}\left(B^{+} \rightarrow \eta \pi^{+}\right)=-0.08 \pm 0.10 \pm 0.01 \\
& \mathcal{A}_{\mathrm{ch}}\left(B^{+} \rightarrow \eta K^{+}\right)=-0.22 \pm 0.11 \pm 0.01 \\
& \mathcal{A}_{\mathrm{ch}}\left(B^{+} \rightarrow \eta^{\prime} \pi^{+}\right)=0.21 \pm 0.17 \pm 0.01 \\
& \mathcal{A}_{\mathrm{ch}}\left(B^{+} \rightarrow \eta^{\prime} K^{+}\right)=0.010 \pm 0.022 \pm 0.006 \\
& \mathcal{A}_{\mathrm{ch}}\left(B^{+} \rightarrow \omega \pi^{+}\right)=-0.02 \pm 0.08 \pm 0.01 \\
& \mathcal{A}_{\mathrm{ch}}\left(B^{+} \rightarrow \omega K^{+}\right)=-0.01 \pm 0.07 \pm 0.01
\end{aligned}
$$

The first error quoted is statistical and the second system-
atic. These results are generally consistent with published measurements [7-13] and supersede our previous ones [79]; for $\mathcal{B}\left(B^{+} \rightarrow \eta K^{+}\right)$we find a value about twice that of [10]. The theoretical estimates are in agreement with the data (though the data have been used in some predictions), but with greater uncertainty [1-3]. Approaches that fit all available data with a moderate number of model parameters have proved fruitful [4-6]. We find no clear evidence for direct $C P$-violation charge asymmetries in these decays. The world averages of the measurements of $\mathcal{A}_{\text {ch }}$ for $B^{+} \rightarrow \eta \pi^{+}\left(B^{+} \rightarrow \eta K^{+}\right)$are both negative and 2.3 (3.0) standard deviations from zero, while the predictions of [3] are positive, though with large errors.

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