## Search for resonances decaying to $\boldsymbol{\eta}_{\boldsymbol{c}} \boldsymbol{\pi}^{+} \boldsymbol{\pi}^{-}$in two-photon interactions

J. P. Lees, ${ }^{1}$ V. Poireau, ${ }^{1}$ V. Tisserand, ${ }^{1}$ J. Garra Tico, ${ }^{2}$ E. Grauges, ${ }^{2}$ A. Palano, ${ }^{3,3 b}$ G. Eigen, ${ }^{4}$ B. Stugu, ${ }^{4}$ D. N. Brown, ${ }^{5}$ L. T. Kerth, ${ }^{5}$ Yu. G. Kolomensky, ${ }^{5}$ G. Lynch, ${ }^{5}$ H. Koch, ${ }^{6}$ T. Schroeder, ${ }^{6}$ D. J. Asgeirsson, ${ }^{7}$ C. Hearty, ${ }^{7}$ T.S. Mattison, ${ }^{7}$ J. A. McKenna, ${ }^{7}$ R. Y. So, ${ }^{7}$ A. Khan, ${ }^{8}$ V.E. Blinov, ${ }^{9}$ A. R. Buzykaev, ${ }^{9}$ V. P. Druzhinin, ${ }^{9}$
V. B. Golubev, ${ }^{9}$ E. A. Kravchenko, ${ }^{9}$ A. P. Onuchin, ${ }^{9}$ S. I. Serednyakov, ${ }^{9}$ Yu. I. Skovpen, ${ }^{9}$ E. P. Solodov, ${ }^{9}$ K. Yu. Todyshev, ${ }^{9}$ A. N. Yushkov, ${ }^{9}$ M. Bondioli, ${ }^{10}$ D. Kirkby, ${ }^{10}$ A. J. Lankford, ${ }^{10}$ M. Mandelkern, ${ }^{10}$ H. Atmacan, ${ }^{11}$ J. W. Gary, ${ }^{11}$ F. Liu, ${ }^{11}$ O. Long, ${ }^{11}$ G. M. Vitug,,${ }^{11}$ C. Campagnari, ${ }^{12}$ T. M. Hong, ${ }^{12}$ D. Kovalskyi, ${ }^{12}$ J. D. Richman, ${ }^{12}$ C. A. West, ${ }^{12}$ A. M. Eisner, ${ }^{13}$ J. Kroseberg, ${ }^{13}$ W. S. Lockman, ${ }^{13}$ A. J. Martinez, ${ }^{13}$ B. A. Schumm, ${ }^{13}$ A. Seiden, ${ }^{13}$ D. S. Chao, ${ }^{14}$ C. H. Cheng, ${ }^{14}$ B. Echenard, ${ }^{14}$ K. T. Flood, ${ }^{14}$ D. G. Hitlin,,${ }^{14}$ P. Ongmongkolkul, ${ }^{14}$ F. C. Porter, ${ }^{14}$ A. Y. Rakitin, ${ }^{14}$ R. Andreassen, ${ }^{15}$ Z. Huard, ${ }^{15}$ B. T. Meadows, ${ }^{15}$ M. D. Sokoloff, ${ }^{15}$ L. Sun, ${ }^{15}$ P. C. Bloom, ${ }^{16}$ W.T. Ford, ${ }^{16}$ A. Gaz, ${ }^{16}$ U. Nauenberg, ${ }^{16}$ J. G. Smith, ${ }^{15}$ S. R. Wagner,,${ }^{16}$ R. Ayad,,${ }^{17, *}$ W. H. Toki, ${ }^{17}$ B. Spaan, ${ }^{18}$ K. R. Schubert, ${ }^{19}$ R. Schwierz, ${ }^{19}$ D. Bernard, ${ }^{20}$ M. Verderi, ${ }^{20}$ P. J. Clark, ${ }^{21}$ S. Playfer, ${ }^{21}$ D. Bettoni, ${ }^{22 a}$ C. Bozzi, ${ }^{22 a}$ R. Calabrese, ${ }^{22 a, 22 b}$ G. Cibinetto, ${ }^{22 a, 22 b}$ E. Fioravanti, ${ }^{22 a, 22 b}$ I. Garzia, ${ }^{22 a, 22 b}$ E. Luppi, ${ }^{22 a, 22 b}$ M. Munerato, ${ }^{22 a, 22 b}$ M. Negrini, ${ }^{22 a, 22 b}$ L. Piemontese, ${ }^{22 a}$ V. Santoro, ${ }^{22 a}$ R. Baldini-Ferroli, ${ }^{23}$ A. Calcaterra, ${ }^{23}$ R. de Sangro, ${ }^{23}$ G. Finocchiaro, ${ }^{23}$ P. Patteri, ${ }^{23}$ I. M. Peruzzi,${ }^{23, \dagger}$ M. Piccolo, ${ }^{23}$ M. Rama, ${ }^{23}$ A. Zallo, ${ }^{23}$ R. Contri, ${ }^{24 a, 24 b}$ E. Guido, ${ }^{24 a, 24 b}$ M. Lo Vetere, ${ }^{24 a, 24 b}$ M. R. Monge, ${ }^{24 a, 24 b}$ S. Passaggio, ${ }^{24 a}$ C. Patrignani, ${ }^{24 a, 24 b}$ E. Robutti, ${ }^{24 a}$ B. Bhuyan, ${ }^{25}$ V. Prasad,,${ }^{25}$ C. L. Lee, ${ }^{26}$ M. Morii, ${ }^{26}$ A. J. Edwards, ${ }^{27}$ A. Adametz,,${ }^{28}$ U. Uwer, ${ }^{28}$ H. M. Lacker, ${ }^{29}$ T. Lueck, ${ }^{29}$ P. D. Dauncey, ${ }^{30}$ P. K. Behera, ${ }^{31}$ U. Mallik, ${ }^{31}$ C. Chen, ${ }^{32}$ J. Cochran, ${ }^{32}$ W. T. Meyer, ${ }^{32}$ S. Prell, ${ }^{32}$ A. E. Rubin, ${ }^{32}$ A. V. Gritsan, ${ }^{33}$ Z. J. Guo, ${ }^{33}$ N. Arnaud, ${ }^{34}$ M. Davier, ${ }^{34}$ D. Derkach,,${ }^{34}$ G. Grosdidier, ${ }^{34}$ F. Le Diberder, ${ }^{34}$ A. M. Lutz, ${ }^{34}$ B. Malaescu, ${ }^{34}$ P. Roudeau, ${ }^{34}$ M. H. Schune, ${ }^{34}$ A. Stocchi, ${ }^{34}$ G. Wormser, ${ }^{34}$ D. J. Lange, ${ }^{35}$ D. M. Wright, ${ }^{35}$ C. A. Chavez, ${ }^{36}$ J. P. Coleman, ${ }^{36}$ J. R. Fry, ${ }^{36}$ E. Gabathuler, ${ }^{36}$ D. E. Hutchcroft, ${ }^{36}$ D. J. Payne, ${ }^{36}$ C. Touramanis, ${ }^{36}$ A. J. Bevan, ${ }^{37}$ F. Di Lodovico, ${ }^{37}$ R. Sacco, ${ }^{37}$ M. Sigamani, ${ }^{37}$ G. Cowan, ${ }^{38}$ D. N. Brown, ${ }^{39}$ C. L. Davis, ${ }^{39}$ A. G. Denig,,$^{40}$ M. Fritsch, ${ }^{40}$ W. Gradl, ${ }^{40}$ K. Griessinger, ${ }^{40}$ A. Hafner, ${ }^{40}$ E. Prencipe, ${ }^{40}$ R. J. Barlow, ${ }^{41, \frac{5}{5}}$ G. Jackson, ${ }^{41}$
G. D. Lafferty, ${ }^{41}$ E. Behn,,${ }^{42}$ R. Cenci, ${ }^{42}$ B. Hamilton, ${ }^{42}$ A. Jawahery, ${ }^{42}$ D. A. Roberts,,${ }^{42}$ C. Dallapiccola, ${ }^{43}$ R. Cowan, ${ }^{44}$ D. Dujmic, ${ }^{44}$ G. Sciolla, ${ }^{44}$ R. Cheaib, ${ }^{45}$ D. Lindemann, ${ }^{45}$ P. M. Patel, ${ }^{45}$ S. H. Robertson, ${ }^{45}$ P. Biassoni, ${ }^{46 a, 46 b}$ N. Neri, ${ }^{46 a}$ F. Palombo, ${ }^{46 a, 46 b}$ S. Stracka, ${ }^{46 a, 46 b}$ L. Cremaldi, ${ }^{47}$ R. Godang, ${ }^{47,8}$ R. Kroeger, ${ }^{47}$ P. Sonnek, ${ }^{47}$ D. J. Summers, ${ }^{47}$ X. Nguyen, ${ }^{48}$ M. Simard, ${ }^{48}$ P. Taras, ${ }^{48}$ G. De Nardo, ${ }^{49 a, 49 b}$ D. Monorchio, ${ }^{49 a, 49 b}$ G. Onorato, ${ }^{49 a, 49 \mathrm{~b}}$ C. Sciacca, ${ }^{49 \mathrm{a}, 49 \mathrm{~b}}$ M. Martinelli ${ }^{50}$ G. Raven, ${ }^{50}$ C.P. Jessop, ${ }^{51}$ J. M. LoSecco, ${ }^{51}$ W. F. Wang, ${ }^{51}$ K. Honscheid, ${ }^{52}$ R. Kass, ${ }^{52}$ J. Brau, ${ }^{53}$ R. Frey,,${ }^{53}$ N. B. Sinev, ${ }^{53}$ D. Strom, ${ }^{53}$ E. Torrence, ${ }^{53}$ E. Feltresi, ${ }^{54 a, 54 b}$ N. Gagliardi, ${ }^{54 a, 54 b}$ M. Margoni, ${ }^{54 a, 54 b}$ M. Morandin, ${ }^{54 a}$ M. Posocco, ${ }^{54 \mathrm{a}}$ M. Rotondo, ${ }^{54 \mathrm{a}}$ G. Simi, ${ }^{54 \mathrm{a}}$ F. Simonetto, ${ }^{54 \mathrm{a}, 54 \mathrm{~b}}$ R. Stroili, ${ }^{54 \mathrm{a}, 54 \mathrm{~b}}$ S. Akar, ${ }^{55}$ E. Ben-Haim, ${ }^{55}$ M. Bomben, ${ }^{55}$ G. R. Bonneaud, ${ }^{55}$ H. Briand, ${ }^{55}$ G. Calderini, ${ }^{55}$ J. Chauveau, ${ }^{55}$ O. Hamon, ${ }^{55}$ Ph. Leruste, ${ }^{55}$ G. Marchiori, ${ }^{55}$ J. Ocariz, ${ }^{55}$ S. Sitt, ${ }^{55}$ M. Biasini, ${ }^{56 a, 56 b}$ E. Manoni, ${ }^{56 a, 56 b}$ S. Pacetti, ${ }^{56 a, 56 b}$ A. Rossi, ${ }^{56 a, 56 b}$ C. Angelini, ${ }^{57 a, 57 b}$ G. Batignani, ${ }^{57 a, 57 b}$ S. Bettarini, ${ }^{57 a, 57 b}$ M. Carpinelli, ${ }^{57 \mathrm{a}, 57 \mathrm{~b}, \|}$ G. Casarosa, ${ }^{57 \mathrm{a}, 57 \mathrm{~b}}$ A. Cervelli, ${ }^{57 \mathrm{a}, 57 \mathrm{~b}}$ F. Forti, ${ }^{57 \mathrm{a}, 57 \mathrm{~b}}$ M. A. Giorgi, ${ }^{57 \mathrm{a}, 57 \mathrm{~b}}$ A. Lusiani, ${ }^{57 \mathrm{a}, 57 \mathrm{c}}$ B. Oberhof, ${ }^{57 \mathrm{a}, 57 \mathrm{~b}}$ E. Paoloni, ${ }^{57 \mathrm{a} a, 57 \mathrm{~b}}$ A. Perez, ${ }^{57 \mathrm{a}}$ G. Rizzo, ${ }^{57 \mathrm{a}, 57 \mathrm{~b}}$ J. J. Walsh, ${ }^{57 \mathrm{a}}$ D. Lopes Pegna, ${ }^{58}$ J. Olsen, ${ }^{58}$ A. J. S. Smith,${ }^{58}$ A. V. Telnov, ${ }^{58}$ F. Anulli, ${ }^{59 a}$ R. Faccini, ${ }^{59 a, 59 b}$ F. Ferrarotto, ${ }^{59 \mathrm{a}}$ F. Ferroni, ${ }^{59 a, 59 \mathrm{~b}}$ M. Gaspero, ${ }^{59 a, 59 b}$ L. Li Gioi, ${ }^{59 \mathrm{a}}$ M. A. Mazzoni, ${ }^{59 \mathrm{a}}$ G. Piredda, ${ }^{59 \mathrm{a}}$ C. Bünger, ${ }^{60}$ O. Grünberg, ${ }^{60}$ T. Hartmann, ${ }^{60}$ T. Leddig, ${ }^{60}$ H. Schröder, ${ }^{60,91}$ C. Voss, ${ }^{60}$ R. Waldi, ${ }^{60}$ T. Adye, ${ }^{61}$ E. O. Olaiya, ${ }^{61}$ F. F. Wilson, ${ }^{61}$ S. Emery, ${ }^{62}$ G. Hamel de Monchenault, ${ }^{62}$ G. Vasseur, ${ }^{62}$ Ch. Yèche, ${ }^{62}$ D. Aston, ${ }^{63}$ D. J. Bard, ${ }^{63}$ R. Bartoldus, ${ }^{63}$ J. F. Benitez, ${ }^{63}$ C. Cartaro, ${ }^{63}$ M. R. Convery, ${ }^{63}$ J. Dorfan, ${ }^{63}$ G. P. Dubois-Felsmann, ${ }^{63}$ W. Dunwoodie, ${ }^{63}$ M. Ebert, ${ }^{63}$ R. C. Field, ${ }^{63}$ M. Franco Sevilla, ${ }^{63}$ B. G. Fulsom, ${ }^{63}$ A. M. Gabareen, ${ }^{63}$ M. T. Graham, ${ }^{63}$ P. Grenier, ${ }^{63}$ C. Hast, ${ }^{63}$ W. R. Innes, ${ }^{63}$ M. H. Kelsey, ${ }^{63}$ P. Kim, ${ }^{63}$ M. L. Kocian, ${ }^{63}$ D. W. G. S. Leith, ${ }^{63}$ P. Lewis, ${ }^{63}$ B. Lindquist, ${ }^{63}$ S. Luitz, ${ }^{63}$ V. Luth,,${ }^{63}$ H. L. Lynch, ${ }^{63}$ D. B. MacFarlane, ${ }^{63}$ D. R. Muller,,${ }^{63}$ H. Neal, ${ }^{63}$ S. Nelson, ${ }^{63}$ M. Perl, ${ }^{63}$ T. Pulliam, ${ }^{63}$ B. N. Ratcliff, ${ }^{63}$ A. Roodman, ${ }^{63}$ A. A. Salnikov, ${ }^{63}$ R. H. Schindler, ${ }^{63}$ A. Snyder, ${ }^{63}$ D. Su, ${ }^{63}$ M. K. Sullivan, ${ }^{63}$ J. Va'vra, ${ }^{63}$ A. P. Wagner, ${ }^{63}$ W. J. Wisniewski, ${ }^{63}$ M. Wittgen, ${ }^{63}$ D. H. Wright, ${ }^{63}$ H. W. Wulsin, ${ }^{63}$ C. C. Young, ${ }^{63}$ V. Ziegler, ${ }^{63}$ W. Park, ${ }^{64}$ M. V. Purohit, ${ }^{64}$ R. M. White, ${ }^{64}$ J.R. Wilson, ${ }^{64}$ A. Randle-Conde, ${ }^{65}$ S. J. Sekula, ${ }^{65}$ M. Bellis, ${ }^{66}$ P. R. Burchat,,${ }^{66}$ T. S. Miyashita, ${ }^{66}$ M.S. Alam,,${ }^{67}$ J. A. Ernst, ${ }^{67}$ R. Gorodeisky, ${ }^{68}$ N. Guttman, ${ }^{68}$ D. R. Peimer, ${ }^{68}$ A. Soffer, ${ }^{68}$ P. Lund, ${ }^{69}$ S. M. Spanier, ${ }^{69}$ J. L. Ritchie, ${ }^{70}$ A. M. Ruland, ${ }^{70}$ R.F. Schwitters, ${ }^{70}$ B. C. Wray, ${ }^{70}$ J. M. Izen, ${ }^{71}$ X.C. Lou, ${ }^{71}$ F. Bianchi, ${ }^{72 a, 72 b}$ D. Gamba, ${ }^{72 a, 72 b}$ L. Lanceri, ${ }^{73 a, 73 b}$ L. Vitale, ${ }^{73 a, 73 b}$ F. Martinez-Vidal, ${ }^{74}$ A. Oyanguren, ${ }^{74}$ H. Ahmed,,${ }^{75}$ J. Albert, ${ }^{75}$ Sw. Banerjee, ${ }^{75}$ F. U. Bernlochner, ${ }^{75}$ H. H. F. Choi, ${ }^{75}$ G. J. King, ${ }^{75}$

[^0]${ }^{49 \mathrm{~b}}$ Dipartimento di Scienze Fisiche, Università di Napoli Federico II, I-80126 Napoli, Italy<br>${ }^{50}$ NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, Netherlands<br>${ }^{51}$ University of Notre Dame, Notre Dame, Indiana 46556, USA<br>${ }^{52}$ Ohio State University, Columbus, Ohio 43210, USA<br>${ }^{53}$ University of Oregon, Eugene, Oregon 97403, USA<br>${ }^{54 \mathrm{a}}$ INFN Sezione di Padova, I-35131 Padova, Italy<br>${ }^{54 \mathrm{~b}}$ Dipartimento di Fisica, Università di Padova, I-35131 Padova, Italy<br>${ }^{55}$ Laboratoire de Physique Nucléaire et de Hautes Energies, IN2P3/CNRS, Université Pierre et Marie Curie-Paris6,<br>Université Denis Diderot-Paris7, F-75252 Paris, France<br>${ }^{56 \mathrm{a}}$ INFN Sezione di Perugia, I-06100 Perugia, Italy<br>${ }^{56 \mathrm{~b}}$ Dipartimento di Fisica, Università di Perugia, I-06100 Perugia, Italy<br>${ }^{57 a}$ INFN Sezione di Pisa, I-56127 Pisa, Italy<br>${ }^{57 \mathrm{~b}}$ Dipartimento di Fisica, Università di Pisa, I-56127 Pisa, Italy<br>${ }^{57 \mathrm{c}}$ Scuola Normale Superiore di Pisa, I-56127 Pisa, Italy<br>${ }^{58}$ Princeton University, Princeton, New Jersey 08544, USA<br>${ }^{59 \mathrm{a}}$ INFN Sezione di Roma, I-00185 Roma, Italy<br>${ }^{59 b}$ Dipartimento di Fisica, Università di Roma La Sapienza, I-00185 Roma, Italy<br>${ }^{60}$ Universität Rostock, D-18051 Rostock, Germany<br>${ }^{61}$ Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, United Kingdom<br>${ }^{62}$ CEA, Irfu, SPP, Centre de Saclay, F-91191 Gif-sur-Yvette, France<br>${ }^{63}$ SLAC National Accelerator Laboratory, Stanford, California 94309, USA<br>${ }^{64}$ University of South Carolina, Columbia, South Carolina 29208, USA<br>${ }^{65}$ Southern Methodist University, Dallas, Texas 75275, USA<br>${ }^{66}$ Stanford University, Stanford, California 94305-4060, USA<br>${ }^{67}$ State University of New York, Albany, New York 12222, USA<br>${ }^{68}$ Tel Aviv University, School of Physics and Astronomy, Tel Aviv, 69978, Israel<br>${ }^{69}$ University of Tennessee, Knoxville, Tennessee 37996, USA<br>${ }^{70}$ University of Texas at Austin, Austin, Texas 78712, USA<br>${ }^{71}$ University of Texas at Dallas, Richardson, Texas 75083, USA<br>${ }^{72 \mathrm{a}}$ INFN Sezione di Torino, I-10125 Torino, Italy<br>${ }^{72 \mathrm{~b}}$ Dipartimento di Fisica Sperimentale, Università di Torino, I-10125 Torino, Italy<br>${ }^{73 \mathrm{a}}$ INFN Sezione di Trieste, I-34127 Trieste, Italy<br>${ }^{73 \mathrm{~b}}$ Dipartimento di Fisica, Università di Trieste, I-34127 Trieste, Italy<br>${ }^{74}$ IFIC, Universitat de Valencia-CSIC, E-46071 Valencia, Spain<br>${ }^{75}$ University of Victoria, Victoria, British Columbia, Canada V8W $3 P 6$<br>${ }^{76}$ Department of Physics, University of Warwick, Coventry CV4 7AL, United Kingdom<br>${ }^{77}$ University of Wisconsin, Madison, Wisconsin 53706, USA<br>(Received 12 June 2012; published 6 November 2012)

We report a study of the process $\gamma \gamma \rightarrow X \rightarrow \eta_{c} \pi^{+} \pi^{-}$, where $X$ stands for one of the resonances $\chi_{c 2}(1 P)$, $\eta_{c}(2 S), X(3872), X(3915)$, or $\chi_{c 2}(2 P)$. The analysis is performed with a data sample of $473.9 \mathrm{fb}^{-1}$ collected with the $B A B A R$ detector at the PEP-II asymmetric-energy electron-positron collider. We do not observe a significant signal for any channel, and calculate $90 \%$ confidence-level upper limits on the products of branching fractions and two-photon widths $\Gamma_{X \rightarrow \gamma \gamma} \mathcal{B}\left(X \rightarrow \eta_{c} \pi^{+} \pi^{-}\right): 15.7 \mathrm{eV}$ for $\chi_{c 2}(1 P), 133 \mathrm{eV}$ for $\eta_{c}(2 S), 11.1 \mathrm{eV}$ for $X(3872)$ (assuming it to be a spin-2 state), 16 eV for $X(3915)$ (assuming it to be a spin-2 state), and 18 eV for $\chi_{c 2}(2 P)$. We also report upper limits on the ratios of branching fractions $\mathcal{B}\left(\eta_{c}(2 S) \rightarrow \eta_{c} \pi^{+} \pi^{-}\right) / \mathcal{B}\left(\eta_{c}(2 S) \rightarrow K_{S}^{0} K^{+} \pi^{-}\right)<10.0 \quad$ and $\quad \mathcal{B}\left(\chi_{c 2}(1 P) \rightarrow \eta_{c} \pi^{+} \pi^{-}\right) / \mathcal{B}\left(\chi_{c 2}(1 P) \rightarrow\right.$ $\left.K_{S}^{0} K^{+} \pi^{-}\right)<32.9$ at the $90 \%$ confidence level.

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[^1]Two-photon fusion events provide a useful production mode to study charmonium states with quantum numbers $J^{P C}=0^{ \pm+}, 2^{ \pm+}, 4^{ \pm+}, \ldots, 3^{++}, 5^{++}, \ldots$ [1,2]. Di-pion transitions among these states have been searched for only in the case of $\eta_{c}(2 S) \rightarrow \eta_{c} \pi^{+} \pi^{-}$[3], in contrast to the narrower vector states, where di-pion transitions have been studied extensively. In particular, the transition amplitude for $\eta_{c}(2 S) \rightarrow \eta_{c} \pi^{+} \pi^{-}$[4] is expected [5] to have
the same approximately linear dependence on the squared invariant mass of the di-pion system as the $\psi(2 S) \rightarrow$ $J / \psi \pi^{+} \pi^{-}$decay [6]. Phase-space integration of the squared amplitude, evaluated for the peak masses $M_{\eta_{c}}$ and $M_{\eta_{c}(2 S)}$ [1] of the $\eta_{c}$ and $\eta_{c}(2 S)$, respectively, yields $\Gamma\left(\eta_{c}(2 S) \rightarrow \eta_{c} \pi^{+} \pi^{-}\right) / \Gamma\left(\psi(2 S) \rightarrow J / \psi \pi^{+} \pi^{-}\right) \approx 2.9$. This leads to the branching fraction prediction $\mathcal{B}\left(\eta_{c}(2 S) \rightarrow\right.$ $\left.\eta_{c} \pi^{+} \pi^{-}\right)=\left(2.2_{-0.6}^{+1.6}\right) \%$, where the uncertainty is due to the uncertainty on the width of the $\eta_{c}(2 S)$ [1]. This decay may be further suppressed due to the contribution of the chromomagnetic interaction to the decay amplitude [7].

In recent years, experiments have reported evidence for charmoniumlike states, such as the $X(3872)$ [8] and $Y(4260)[9,10]$, which do not fit well into the conventional $c \bar{c}$ picture. This has prompted much theoretical activity and proposals for new models [11]. Several studies of these states have been performed with the $J / \psi \pi^{+} \pi^{-}$final state [9,12], but no search using the $\eta_{c} \pi^{+} \pi^{-}$final state has been conducted. Such a search may shed light on the quantum numbers or the internal dynamics of these states. In particular, it has been suggested [13] that if the $X(3872)$ is the $1^{1} D_{2}$ state $\eta_{c 2}$, then the branching fraction $\mathcal{B}(X(3872) \rightarrow$ $\left.\eta_{c} \pi^{+} \pi^{-}\right)$could be significantly larger than $\mathcal{B}(X(3872) \rightarrow$ $J / \psi \pi^{+} \pi^{-}$). The quantum numbers $J^{P C}=2^{-+}$of the $\eta_{c 2}$ are consistent with the results of an angular analysis of $X(3872) \rightarrow J / \psi \pi^{+} \pi^{-}$[14] and would allow production of $X(3872)$ in two-photon fusion.

We present herein a study of the process $\gamma \gamma \rightarrow X \rightarrow$ $\eta_{c} \pi^{+} \pi^{-}$, where $X$ is one of the resonances $\chi_{c 2}(1 P)$, $\eta_{c}(2 S), X(3872), X(3915)$, or $\chi_{c 2}(2 P)$, and the $\eta_{c}$ is reconstructed in the final state $K_{S}^{0} K^{+} \pi^{-}$[15].

The data sample was collected with the BABAR detector at the PEP-II asymmetric-energy $e^{+} e^{-}$collider located at the SLAC National Accelerator Laboratory. It consists of $429.1 \pm 1.9 \mathrm{fb}^{-1}$ collected at the energy of the $\mathrm{Y}(4 S)$ resonance, constituting the entire $B A B A R \Upsilon(4 S)$ data set, and $44.8 \pm 0.2 \mathrm{fb}^{-1}$ collected about 40 MeV below the $Y(4 S)$ resonance. The $B A B A R$ detector is described in detail in Ref. [16].

Samples of Monte Carlo (MC) simulated events are analyzed with the same reconstruction and analysis procedures as the data sample, following a GEANT4-based [17] detector simulation [16]. Simulated background samples include $e^{+} e^{-} \rightarrow q \bar{q}$ continuum events $(q=u, d, s, c)$ generated with JETSET [18], $\mathrm{Y}(4 S) \rightarrow B \bar{B}$ decays generated with EVTGEN [19] and JETSET, and $e^{+} e^{-} \rightarrow \tau^{+} \tau^{-}$events generated with KK [20]. In order to study initial-stateradiation (ISR) background and the invariant-mass resolution, a sample of $e^{+} e^{-} \rightarrow \gamma \psi(2 S)$ events with $\psi(2 S) \rightarrow$ $J / \psi \pi^{+} \pi^{-}$and $J / \psi \rightarrow K_{S}^{0} K^{+} \pi^{-}$is generated with EVTGEN. The GAMGAM [21] generator is used to generate signal event samples for each of the $X$ states studied, with the decay $X \rightarrow \eta_{c} \pi^{+} \pi^{-}$simulated with an amplitude that is uniform throughout the decay phase space, independent
of the final-state kinematic variables. The decay $\eta_{c} \rightarrow$ $K_{S}^{0} K^{+} \pi^{-}$is generated with a uniform amplitude or with equal and incoherent $K_{0}^{*}(1430)^{-} K^{+}$and $\bar{K}_{0}^{*}(1430)^{0} K^{0}$ contributions. The GAMGAM generator is also used to generate $\gamma \gamma \rightarrow \eta_{c} \rightarrow K_{S}^{0} K^{+} \boldsymbol{\pi}^{-}$events.

The analysis is performed with two data samples. The sample used to search for the process $\gamma \gamma \rightarrow X \rightarrow$ $\eta_{c} \pi^{+} \pi^{-}$is referred to as the "main sample." Properties of the $\eta_{c}$ and its decay into $K_{S}^{0} K^{+} \pi^{-}$are studied with a separate "control sample" of $\gamma \gamma \rightarrow \eta_{c} \rightarrow K_{S}^{0} K^{+} \pi^{-}$ events. For the main (control) sample, we select events that contain six (four) charged-particle tracks.

For both samples, charged kaon candidates are identified using likelihood values calculated from measurements of specific energy loss and information from a detector of internally reflected Cherenkov radiation. All other tracks are assumed to be pions. A $K_{S}^{0}$ candidate is reconstructed by fitting a $\pi^{+} \pi^{-}$pair to a common vertex, with invariant mass in the range $0.491<m\left(\pi^{+} \pi^{-}\right)<0.503 \mathrm{GeV} / c^{2}$. A kinematic fit is performed, constraining $m\left(\pi^{+} \pi^{-}\right)$to the nominal $K_{S}^{0}$ mass [22]. An $\eta_{c} \rightarrow K_{S}^{0} K^{+} \pi^{-}$decay candidate is reconstructed by combining a $K_{S}^{0}$ candidate with a $K^{+}$and a $\pi^{-}$and requiring the resulting invariant mass to lie in the range $2.77<m\left(K_{S}^{0} K^{+} \pi^{-}\right)<3.22 \mathrm{GeV} / c^{2}$. In the main sample, the decay $X \rightarrow \eta_{c} \pi^{+} \pi^{-}$is reconstructed by combining an $\eta_{c}$ candidate with the remaining two tracks in the event. A kinematic fit is applied, requiring the $X$-candidate decay vertex to be consistent with the $e^{+} e^{-}$interaction region. The angle $\alpha_{K_{S}^{0}}$ between the $K_{S}^{0}$ momentum vector and the line connecting the $\eta_{c}$ and the $K_{S}^{0}$ decay vertices is required to satisfy $\cos \alpha_{K_{S}^{0}}>0.99$.

In the control sample, we require the polar angle (the angle with respect to the beam axis) $\theta_{\eta_{c}}$ of the $\eta_{c}$ candidate to satisfy $\left|\cos \theta_{\eta_{c}}\right|>0.99$ and the transverse momentum of the $\eta_{c}$ candidate to satisfy $p_{\eta_{c}}^{T}<0.5 \mathrm{GeV} / c$, both in the center-of-mass (c.m.) frame of the $e^{+} e^{-}$system. The extra energy in the event, defined as the total energy in calorimeter clusters not associated with the identified tracks, is required to satisfy $E_{\mathrm{ex}}<0.5 \mathrm{GeV}$ in the c.m. frame. The $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$distribution of the selected control-sample events, shown in Fig. 1(a), exhibits clear $\eta_{c}$ and $J / \psi$ peaks, with the $J / \psi$ produced in ISR events. In the main sample, continuum background is strongly suppressed with the requirements $\left|\cos \theta_{X}\right|>0.85, p_{X}^{T}<1.5 \mathrm{GeV} / c$, and $E_{\text {ex }}<0.8 \mathrm{GeV}$, where $\cos \theta_{X}$ and $p_{X}^{T}$ are the polar angle and transverse momentum of the $X$ candidate. In addition, the total visible energy in the event, obtained from all charged tracks and calorimeter clusters, is required to satisfy $E_{v i s}<10 \mathrm{GeV}$ in the laboratory frame.

In the main sample, we suppress QED background by requiring $R 2<0.7$, where $R 2$ is the ratio of the second and zeroth Fox-Wolfram moments [23]. We suppress background due to ISR events with a requirement on the missing mass squared $m_{\text {miss }}^{2} \equiv\left(p_{e^{+} e^{-}}-p_{X}\right)^{2}>10 \mathrm{GeV}^{2} / c^{4}$,
where $p_{e^{+} e^{-}}\left(p_{X}\right)$ is the total 4-momentum of the beam particles ( $X$ candidate).

Additional background suppression in the main sample is obtained by using the Dalitz plot for the $\eta_{c}$ candidates. The Dalitz plot is shown in Fig. 1(b) for control-sample events in the $\eta_{c}$ peak region $2.94<m\left(K_{S}^{0} K^{+} \pi^{-}\right)<$ $3.02 \mathrm{GeV} / c^{2}$, and in Figs. 1(c) and 1(d) for main-sample events in the lower and upper $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$sidebands $2.8<m\left(K_{S}^{0} K^{+} \pi^{-}\right)<2.9 \mathrm{GeV} / c^{2} \quad$ and $\quad 3.05<$ $m\left(K_{S}^{0} K^{+} \pi^{-}\right)<3.2 \mathrm{GeV} / c^{2}$, respectively. These distributions indicate that true $\eta_{c} \rightarrow K_{S}^{0} K^{+} \pi^{-}$decays often proceed via intermediate $K_{0}^{*}(1430)$ states, while background events contain $K^{*}$ (892) decays and random combinations. Taking advantage of this difference to suppress non- $\eta_{c}$ background in the main sample, we require $\mid m^{2}\left(K_{S}^{0} \pi^{-}\right)-$ $M_{K_{0}^{*}(1430)^{-}}^{2} \mid<0.5 \mathrm{GeV}^{2} / c^{4}$ or $\left|m^{2}\left(K^{+} \pi^{-}\right)-M_{K_{0}^{*}(1430)^{0}}^{2}\right|<$ $0.5 \mathrm{GeV}^{2} / c^{4}$, and exclude events that satisfy $\mid m^{2}\left(K_{S}^{0} \pi^{-}\right)-$ $M_{K^{*}(892)^{-}}^{2} \mid<0.35 \mathrm{GeV}^{2} / c^{4}$ or $\left|m^{2}\left(K^{+} \pi^{-}\right)-M_{K^{*}(892)^{0}}^{2}\right|<$ $0.2 \mathrm{GeV}^{2} / c^{4}$, where $M_{R}$ is the peak mass of resonance $R$ [22]. The Dalitz-plot region selected by these criteria is enclosed within the solid lines in Figs. 1(b)-1(d). The criteria are the result of maximizing $\varepsilon_{\eta_{c}}^{D P} / \sqrt{\varepsilon_{S B}^{D P}}$, where $\varepsilon_{\eta_{c}}^{D P}=(63.5 \pm 3.2) \%$ is the efficiency of the Dalitz-plot


FIG. 1 (color online). (a) The $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$distribution for the control sample. The vertical lines indicate the $\eta_{c}$ peak mass region. Also shown are the $K_{S}^{0} K^{+} \pi^{-}$Dalitz plots for (b) controlsample events in the $\eta_{c}$ peak mass region and for main-sample events in the (c) lower and (d) upper $\eta_{c}$ mass sidebands. Solid black lines indicate the regions defined by the Dalitz-plot selection criteria. The dotted blue box in the upper left corner of (c) and (d) indicates the Dalitz-plot-sideband background region used for the neural-network training.
requirements for $\eta_{c}$ decays, determined by fitting the $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$distribution of the control sample, and $\varepsilon_{S B}^{D P}=(30.74 \pm 0.21) \%$ is the corresponding efficiency for main-sample events in the $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$sidebands. The $\bar{D}^{0} \rightarrow K^{+} \pi^{-}$band, evident in Fig. 1(c), becomes insignificant following a neural-network requirement, described below. Therefore, no explicit effort is made to remove this source of background.

Further background suppression is achieved by combining six variables into a neural-network discriminator. Two of the variables are $E_{\mathrm{ex}}$ and $p_{X}^{T}$. Each of the remaining four variables is a discrete output value of a kaon- or pionidentification algorithm applied to one of the chargedparticle tracks that is not a daughter of the $K_{S}^{0}$ candidate. The distributions of the neural-network input variables are shown in Figs. 2(c) and 2(d). The neural network is trained with signal MC and main-sample background events in the Dalitz-plot sideband region $m^{2}\left(K^{+} \pi^{-}\right)>2.5 \mathrm{GeV}^{2} / c^{4}$,


FIG. 2 (color online). Signal (unhatched) and background (hatched) distributions of the neural-network input variables (a) $E_{\text {ex }}$, (b) $p_{X}^{T}$, and the (c) kaon and (d) pion identification variables. (e) The distributions of the neural-network output variable $V_{\mathrm{NN}}$. (f) The $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$distribution of the data with the step-1 fit function overlaid.
$m^{2}\left(K_{S}^{0} \pi^{-}\right)<1.5 \mathrm{GeV}^{2} / c^{4}$, indicated by the dashed boxes in Figs. 1(c) and 1(d). This region is chosen since it contains only $(3.40 \pm 0.66) \%$ of $\eta_{c}$ decays in the control sample. We find only insignificant differences in the neuralnetwork signal-to-background separation when using different signal samples or the mirror Dalitz-plot region $m^{2}\left(K^{+} \pi^{-}\right)<1.5 \mathrm{GeV}^{2} / c^{4}, \quad m^{2}\left(K_{S}^{0} \pi^{-}\right)>2.5 \mathrm{GeV}^{2} / c^{4}$ for the background. The distributions of the output variable $V_{\mathrm{NN}}$ are shown in Fig. 2(e) for signal and background events. We find the optimal selection on this variable to be $V_{\mathrm{NN}}>0.84$. The signal efficiency of this selection is $72 \%$ for the $\eta_{c}(2 S)$, and varies by up to $4 \%$, depending on the $X$ mass. The background efficiency is $(10.4 \pm 0.2) \%$ for the neural-network training region and $(7.4 \pm 0.2) \%$ for the mirror region.

We find 2863 main-sample events that satisfy all the selection criteria, with only about 700 events expected from non- $\gamma \gamma$ background MC. We conclude that the majority of the background is due to $\gamma \gamma$ events, for which we have no generic generator. More than one $X$ candidate is reconstructed in $3.8 \%$ of the events. In these cases, we select the candidate for which $m^{2}\left(K_{S}^{0} \pi^{-}\right)$or $m^{2}\left(K^{+} \pi^{-}\right)$is closest to the $K_{0}^{*}(1430)$ peak.

In addition to these samples, an ISR-produced sample of $\psi(2 S) \rightarrow J / \psi \pi^{+} \pi^{-}$events is used to evaluate a systematic uncertainty associated with the detector resolution. This sample is selected in the same way as the main sample, except that the neural-network and Dalitz-plot selections are not applied, the $K_{S}^{0} K^{+} \pi^{-}$invariant mass is required to be between 3.0 and $3.2 \mathrm{GeV} / c^{2}$, and $m_{\text {miss }}^{2}$ must be less than $1 \mathrm{GeV}^{2} / c^{4}$.

We define four categories of events in the main sample: signal corresponds to $\gamma \gamma \rightarrow X \rightarrow \eta_{c} \pi^{+} \pi^{-}$events; combinatorial background (CB), which is by far the most copious background, arises from random combinations of final-state particles; events with a true $\eta_{c} \rightarrow K_{S}^{0} K^{+} \pi^{-}$ decay and two pions not originating from an $X$ resonance decay are categorized as $\eta_{c}$-peaking background ( $\eta_{c} \mathrm{~B}$ ); $X$-peaking background ( $X \mathrm{~B}$ ) corresponds to decays $X \rightarrow$ $K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}$that do not proceed through an intermediate $\eta_{c}$.

The extraction of the signal yield proceeds in two steps. In step 1, we determine the values of the $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$-distribution parameters of the combinatorial background from a one-dimensional fit to $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$, without any restrictions on $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$.

In step 2, we extract the signal yield for each $X$ resonance hypothesis from a two-dimensional fit to the $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$versus $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$distribution for events in an $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$window around the resonance peak. The fits use the unbinned, extended-maximum-likelihood method and are performed with the ROOFIT package [24].

From events in the $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$sidebands, we observe that all correlation between the $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$and
$m\left(K_{S}^{0} K^{+} \pi^{-}\right)$distributions for the combinatorial background is accounted for by the phase space $\Phi\left(m\left(K_{S}^{0} K^{+} \pi^{-}\right), m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)\right)$of the three-body final state consisting of the $\pi^{+}, \pi^{-}$, and the ( $K_{S}^{0} K^{+} \pi^{-}$) system. This is used to construct the probability-density function (PDF) [25] of the step-1 fit. This PDF is a function of $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$with $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$as a conditional variable, and is given by

$$
\begin{equation*}
\mathcal{H}\left(m_{3} \mid m_{5}\right)=N_{\eta_{c}} \mathcal{H}_{\eta_{c}}\left(m_{3}\right)+N_{\dot{\eta}_{c}} \mathcal{H}_{\dot{\eta}_{c}}\left(m_{3} \mid m_{5}\right), \tag{1}
\end{equation*}
$$

where $N_{\eta_{c}}\left(N_{h_{c}}\right)$ is the number of events with (without) a true $\eta_{c} \rightarrow K_{S}^{0} K^{+} \pi^{-}$decay. We have used the notation $m_{3} \equiv m\left(K_{S}^{0} K^{+} \pi^{-}\right)$and $m_{5} \equiv m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$for brevity.

The PDF for non $\eta_{c}$ events in Eq. (1) is

$$
\begin{equation*}
\mathcal{H}_{\dot{\eta}_{c}}\left(m_{3} \mid m_{5}\right)=\mathcal{P}_{2}\left(m_{3} ; a_{1}, a_{2}, m_{3}^{0}\right) \Phi\left(m_{3}, m_{5}\right) \tag{2}
\end{equation*}
$$

where $\mathcal{P}_{2}\left(m_{3} ; a_{1}, a_{2}, m_{3}^{0}\right)=1+a_{1}\left(m_{3}-m_{3}^{0}\right)+a_{2}\left(m_{3}-\right.$ $\left.m_{3}^{0}\right)^{2}$ is a second-order polynomial and $m_{3}^{0}$ is a constant offset set to $3.0 \mathrm{GeV} / c^{2}$ in order to reduce correlations between $a_{1}$ and $a_{2}$. Determination of the coefficients $a_{1}, a_{2}$ is the main purpose of the step- 1 fit. The PDF for $\eta_{c}$ events in Eq. (1) is

$$
\begin{equation*}
\mathcal{H}_{\eta_{c}}\left(m_{3}\right)=\mathcal{W}\left(m_{3} ; M_{\eta_{c}}, \Gamma_{\eta_{c}}, \vec{r}_{m_{3}}\right) \tag{3}
\end{equation*}
$$

where $\mathcal{W}$ is a relativistic Breit-Wigner function $\left[\left(\tilde{m}_{3}^{2}-M_{\eta_{c}}^{2}\right)^{2}+M_{\eta_{c}}^{2} \Gamma_{\eta_{c}}^{2}\right]^{-1}$ convolved with a detectorresolution function $\mathcal{R}\left(m_{3}-\tilde{m}_{3} ; \vec{r}_{m_{3}}\right)$ that depends on a set of parameters $\vec{r}_{m_{3}}$ and the difference between the measured $m_{3}$ and the true invariant mass $\tilde{m}_{3}$ of the $K_{S}^{0} K^{+} \pi^{-}$ system. The resolution function is the sum of two Crystal Ball functions [26] with oppositely directed tails and common Gaussian-parameter values,

$$
\begin{align*}
\mathcal{R}\left(x ; \vec{r}_{x}\right)= & \left(a_{l}+a_{r}\right) \exp \left[-(x-\bar{x})^{2} /\left(2 \sigma^{2}\right)\right] \\
& +a_{r} T_{r}(x)+a_{l} T_{l}(x) \tag{4}
\end{align*}
$$

where

$$
T_{i}(x)= \begin{cases}A_{i}\left[\sigma /\left(x_{i}^{\prime}-\bar{x}\right)\right]^{n_{i}} ; & x>\bar{x}+\alpha_{i} \sigma  \tag{5}\\ 0 ; & x \leq \bar{x}+\alpha_{i} \sigma\end{cases}
$$

and we have defined $x_{i}^{\prime}=x+\sigma\left(n_{i} / \alpha_{i}-\alpha_{i}\right)$, and $A_{i}=$ $\left(n_{i} / \alpha_{i}\right)^{n_{i}} \times \exp \left(-\alpha_{i}^{2} / 2\right)$. In Eq. (4), the subscripts $r$ and $l$ label the parameters of the right and left tails, respectively. The values of the resolution-function parameters $\vec{r}_{m_{3}}=$ $\left(\bar{x}, \sigma, n_{i}, \alpha_{i}, a_{i}\right)$ are determined from fits to the signal MC samples.

In addition to $a_{1}$ and $a_{2}$, the parameter determined in the step-1 fit are the yields $N_{\eta_{c}}$ and $N_{\eta_{c}}$, and the mass $M_{\eta_{c}}$ and width $\Gamma_{\eta_{c}}$ of the $\eta_{c}$ peak. In order to obtain $M_{\eta_{c}}$ and $\Gamma_{\eta_{c}}$ from the data, the step- 1 fit is performed simultaneously on the main sample and the control sample. The PDF for the control sample is

$$
\begin{align*}
\mathcal{H}^{\prime}\left(m_{3}\right)= & N_{J / \psi}^{\prime} \mathcal{W}\left(m_{3} ; M_{J / \psi}, \Gamma_{J \psi}, \vec{r}_{m_{3}}\right) \\
& +N_{\eta_{c}}^{\prime} \mathcal{H}_{\eta_{c}}\left(m_{3}\right)+N_{\mathrm{bgd}}^{\prime} \mathcal{P}_{2}\left(m_{3} ; a_{1}^{\prime}, a_{2}^{\prime}, m_{3}^{0}\right) . \tag{6}
\end{align*}
$$

Additional control-sample parameter values determined in the fit are the peak $J / \psi$ mass $M_{J / \psi}$, the background parameters $a_{1}^{\prime}, a_{2}^{\prime}$, and the $\eta_{c}, J / \psi$, and background event yields $N_{\eta_{c}}^{\prime}, N_{J \psi}^{\prime}$, and $N_{\text {bgd }}^{\prime}$.

The $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$distribution of the data and the step-1 PDF are shown in Fig. 2(f). The fitted parameter values are $a_{1}=1.24 \pm 0.19\left(\mathrm{GeV} / c^{2}\right)^{-1}, \quad a_{2}=0.2 \pm 1.4\left(\mathrm{GeV} / c^{2}\right)^{-2}$, $N_{\eta_{c}}=50 \pm 37, \quad N_{\eta_{c}}^{\prime}=10350 \pm 300, \quad$ and $\quad N_{J / \psi}^{\prime}=$ $1877 \pm 90$. The large relative uncertainties for $a_{1}$ and $a_{2}$ are the result of the near linearity of the $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$ distribution and the correlation between the two parameters, which is taken into account in the evaluation of systematic uncertainties. The $\eta_{c}$ parameter values determined in the step-1 fit are $\Gamma_{\eta_{c}}=31.7 \pm 1.5 \mathrm{MeV} / c^{2}$ and $M_{\eta_{c}}=2.98285 \pm 0.00038 \mathrm{GeV} / c^{2}$, where the uncertainties are statistical only. These results are consistent with previous measurements [22].

The PDF for the step-2 fit is a linear combination of the PDFs of the four event types,

$$
\begin{equation*}
\mathcal{P}=N_{\text {sig }} \mathcal{P}_{\text {sig }}+N_{\mathrm{CB}} \mathcal{P}_{\mathrm{CB}}+N_{\eta_{c} \mathrm{~B}} \mathcal{P}_{\eta_{c} \mathrm{~B}}+N_{X B} \mathcal{P}_{X B} . \tag{7}
\end{equation*}
$$

The signal PDF is a relativistic Breit-Wigner function convolved with the resolution function, for both $m_{3}$ and $m_{5}$ :

$$
\begin{equation*}
\mathcal{P}_{\text {sig }}\left(m_{3}, m_{5}\right)=\mathcal{H}_{\eta_{c}}\left(m_{3}\right) \mathcal{W}\left(m_{5} ; M_{X}, \Gamma_{X}, \vec{r}_{m_{5}}\right), \tag{8}
\end{equation*}
$$

where $M_{X}$ and $\Gamma_{X}$ are the known mass and width of the resonance of interest [1,22,27], and $\vec{r}_{m_{5}}$ are the parameters of the $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$resolution function $\mathcal{R}\left(m_{5}-\tilde{m}_{5} ; \vec{r}_{m_{5}}\right)$, obtained from a fit to signal MC. The combinatorial-background PDF is

$$
\begin{equation*}
\mathcal{P}_{\mathrm{CB}}\left(m_{3}, m_{5}\right)=\mathcal{H}_{\phi_{c}}\left(m_{3} \mid m_{5}\right) \mathcal{C}_{2}\left(m_{5} ; b_{1}^{\mathrm{CB}}, b_{2}^{\mathrm{CB}}\right), \tag{9}
\end{equation*}
$$

where $\mathcal{C}_{2}\left(m_{5} ; b_{1}^{\mathrm{CB}}, b_{2}^{\mathrm{CB}}\right)$ is a second-order Chebychev polynomial with first- (second-)order coefficients $b_{1}^{\mathrm{CB}}\left(b_{2}^{\mathrm{CB}}\right)$. The $\eta_{c}$-peaking background PDF is

$$
\begin{equation*}
\mathcal{P}_{\eta_{c} \mathrm{~B}}\left(m_{3}, m_{5}\right)=\mathcal{H}_{\eta_{c}}\left(m_{3}\right) \mathcal{C}_{1}\left(m_{5} ; b_{1}^{\eta_{c} \mathrm{~B}}\right), \tag{10}
\end{equation*}
$$

where $\mathcal{C}_{1}\left(m_{5} ; b_{1}^{\eta_{c} \mathrm{~B}}\right)$ is a first-order Chebychev polynomial. The $X$-peaking background PDF is

$$
\begin{equation*}
\mathcal{P}_{X \mathrm{~B}}\left(m_{3}, m_{5}\right)=\mathcal{P}_{1}\left(m_{3} ; c_{1}^{X \mathrm{~B}}, m_{3}^{0}\right) \mathcal{W}\left(m_{5} ; M_{X}, \Gamma_{X}, \vec{r}_{m_{5}}\right), \tag{11}
\end{equation*}
$$

where $\mathcal{P}_{1}\left(m_{3} ; c_{1}^{X \mathrm{~B}}, m_{3}^{0}\right)$ is a first-order polynomial. The parameter values determined with the step-2 fit are the four yields of Eq. (7) and the background shape parameters $b_{1}^{\mathrm{CB}}, b_{2}^{\mathrm{CB}}, b_{1}^{\eta_{c} \mathrm{~B}}$, and $c_{1}^{X \mathrm{~B}}$.

The step-2 fit is performed four times in different $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$windows, fitting for the (1) $\chi_{c 2}(1 P)$, (2) $\eta_{c}(2 S)$, (3) $X(3872)$ and $X(3915)$, or (4) $X(3872)$ and $\chi_{c 2}(2 P)$ resonances. A simultaneous fit to the three resonances $X(3872), X(3915)$, and $\chi_{c 2}(2 P)$ is observed to be unstable when tested with parametrized MC experiments, due to the large number of fit parameters, small signal, and large overlap of the $X(3915)$ and $\chi_{c 2}(2 P)$ line shapes. Therefore, we conduct fits (3) and (4) separately to test for the existence of a signal for either set of line shape parameters. The $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$and $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$ distributions and fit functions are shown in Fig. 3. The difference between the fit function of fit (3) and that of fit (4) is almost indistinguishable within the thickness of the curve in Fig. 3(f). The fitted signal yields are summarized in Table I.

No significant signal or peaking background is observed in any of the fits. However, a hint of $X$-peaking background


FIG. 3 (color online). Distributions of (a),(c),(e) $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$ and (b),(d),(f) $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$with the step-2 fit PDF overlaid for the fit regions of the (a),(b) $\chi_{c 2}(1 P)$, (c),(d) $\eta_{c}(2 S)$, and (e),(f) $X(3872), X(3915)$ and $\chi_{c 2}(2 P)$. The vertical dashed lines in (f) indicate the peak mass positions of the $X(3872), X(3915)$, and $\chi_{c 2}(2 P)$ [22].
is visible in the $\chi_{c 2}(1 P)$ and $\eta_{c}(2 S)$ fits of Figs. 3(b) and 3 (d), with event yields of $33 \pm 14$ and $47 \pm 24$, respectively, where the uncertainties are statistical only. This may be due to decays of $\chi_{c 2}(1 P)$ and $\eta_{c}(2 S)$ into $K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}$[28], which are suppressed in this analysis by the $2.77<m\left(K_{S}^{0} K^{+} \pi^{-}\right)<3.22 \mathrm{GeV} / c^{2}$ requirement. Fits (3) and (4) yield insignificant $X$-peaking background, roughly canceling the negative signal yields. The results shown in Table I for the $X(3872)$ are obtained from fit (4). The $X(3872)$ yield from fit (3) is 1.6 events lower than in fit (4). Since no signal is observed for the $X(3915)$ or the $\chi_{c 2}(2 P)$, we obtain a conservative upper limit on the yield of the $X(3915)\left(\chi_{c 2}(2 P)\right)$ by fixing the $\chi_{c 2}(2 P)(X(3915))$ yield to zero.

We estimate systematic uncertainties on the signal yields associated with the fit procedure by repeating the fits with the variations described below and adding the different uncertainties in quadrature. We account for uncertainties in the $X$ mass and width values by varying them within their uncertainties [22]. This is the source of the largest signal-yield systematic uncertainty, except for the $\chi_{c 2}(1 P)$. The order of the polynomial in each PDF is varied to account for uncertainties due to background modeling. We vary the resolution-function Gaussian width [ $\sigma$ in Eq. (4)] by $2 \mathrm{MeV} / c^{2}$ for the $m\left(K_{S}^{0} K^{+} \pi^{-}\right)$PDF to account for a difference between the $J / \psi$ mass resolution in MC and in the control sample, and by $0.9 \mathrm{MeV} / c^{2}$ for the $m\left(K_{S}^{0} K^{+} \pi^{-} \pi^{+} \pi^{-}\right)$PDF due to a difference in the $\psi(2 S)$ mass resolution between MC and data. An additional uncertainty is evaluated by using the sum of three Gaussians to define the resolution function. To address the possibility that correlations between the $m_{5}$ and $m_{3}$ distributions are not taken fully into account by the phase-space factor $\Phi\left(m_{3}, m_{5}\right)$ in Eq. (2), we replace the parameters $a_{i}$ of Eq. (2) by $a_{i}\left(1+a_{i}^{\prime \prime} m_{5}\right)$. The values of the parameters $a_{i}^{\prime \prime}$ are found to be consistent with zero, and we conservatively use their uncertainties to evaluate the systematic uncertainty on the signal yield. The effect of not
accounting for phase-space correlations between $m_{3}$ and $m_{5}$ in the signal and $\eta_{c}$-peaking background PDFs is determined to be small compared to other systematic uncertainties, except for the $\chi_{c 2}(1 P)$, for which this uncertainty is dominant and equals 2.4 events. Statistical uncertainties from the step-1 fit are propagated to the step-2 fit, accounting for correlations among the parameters.

We test the entire fit procedure using parametrized MC experiments generated with the PDFs of Eqs. (1) and (7). A bias of up to two events on the signal yield is found and used as a correction that is accounted for in the values shown in Table I. A systematic uncertainty on this correction is evaluated by repeating this study after varying the generated signal yield by its statistical uncertainty in the data fit.

Since the dominant combinatorial background is distributed in phase space differently from signal and often contains additional final-state particles, interference between signal and background is expected to be relatively small. In addition, the small signal yields make the evaluation of such interference effects unreliable. Therefore, we do not attempt to account for possible interference.

We evaluate systematic uncertainties on track and $K_{S}^{0}$ reconstruction efficiencies, accounting for the momentum and angular distribution of signal tracks, as well as on the uncertainty of the Dalitz-plot requirement efficiency. A $2 \%$ systematic uncertainty is assigned due to differences between the distributions of the selection variables in the control sample and in $\gamma \gamma \rightarrow \eta_{c} \rightarrow K_{S}^{0} K^{+} \pi^{-}$MC. Differences between the data and MC distributions of the particle-identification variables are studied using a highpurity sample of $D^{*+} \rightarrow \pi^{+} D^{0}, D^{0} \rightarrow K^{-} \pi^{+}$events, and found to have negligible impact on the efficiency.

The expected Dalitz-plot dependence of the $X \rightarrow$ $\eta_{c} \pi^{+} \pi^{-}$decay is unknown. However, we account for uncertainties in this amplitude, which is uniform in our simulated signal samples, by weighting events according to $\left(m^{2}(\pi \pi)-4 M_{\pi}^{2}\right)^{2}$ [5], where $m^{2}(\pi \pi)$ is the squared dipion mass and $M_{\pi}$ is the $\pi^{-}$mass. From the weighted sample, we extract an efficiency correction of up to $4.6 \%$

TABLE I. Results of the step-2 fits. For each resonance $X$, we show the peak mass and width used in the PDF (from Refs. [1,22,27]); the mass range of the fit; the efficiency; the bias-corrected signal yield with statistical and systematic uncertainties; the product of the $\gamma \gamma \rightarrow X$ production cross section and $X \rightarrow \eta_{c} \pi^{+} \pi^{-}$branching fraction, and the $90 \%$ C.L. upper limit (UL) on this product; the product of the two-photon partial width $\Gamma_{\gamma \gamma}$ and the $X \rightarrow \eta_{c} \pi^{+} \pi^{-}$branching fraction, and the $90 \%$ C.L. upper limit on this product. For the $X(3872)$ and the $X(3915)$ we assume $J=2$.

| Resonance | $M_{X}\left(\mathrm{MeV} / c^{2}\right)$ | $\Gamma_{X}(\mathrm{MeV})$ | $m_{5}$ range ( $\mathrm{GeV} / c^{2}$ ) | $\varepsilon(\%)$ | $N_{\text {sig }}$ | $\sigma \mathcal{B}(\mathrm{fb})$ |  | $\Gamma_{\gamma \gamma} \mathcal{B}(\mathrm{eV})$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Central value | UL | Central value | UL |
| $\chi_{\text {c2 }}(1 P)$ | $3556.20 \pm 0.09$ | $1.97 \pm 0.11$ | 3.500-3.612 | $3.60 \pm 0.39$ | $10.22_{-6.3}^{+7.7} \pm 3.5$ | $37_{-23}^{+28} \pm 15$ | 80 | $7.2+5.4 \pm 2.9$ | 15.7 |
| $\eta_{c}(2 S)$ | $3638.5 \pm 1.7$ | $13.4 \pm 5.6$ | 3.565-3.728 | $3.53 \pm 0.35$ | $17_{-11}^{+12} \pm 3$ | $61_{-41}^{+44} \pm 16$ | 123 | $65_{-44}^{+47} \pm 18$ | 133 |
| $X(3872)$ | $3871.57 \pm 0.25$ | $3.0 \pm 2.1$ | 3.807-4.047 | $3.92 \pm 0.38$ | $-4.7_{-6.9}^{+7.9} \pm 2.8$ | $-16_{-23}^{+26} \pm 10$ | 38 | $-4.5{ }_{-6.7}^{+7.7} \pm 2.9$ | 11.1 |
| $X(3915)$ | $3915.0 \pm 3.6$ | $17.0 \pm 10.4$ | 3.807-4.047 | $3.79 \pm 0.37$ | $-13_{-11}^{+11} \pm 7$ | $-44_{-38}^{+38} \pm 25$ | 53 | $-13_{-12}^{+12} \pm 8$ | 16 |
| $\chi_{c 2}(2 P)$ | $3927.2 \pm 2.6$ | $24 \pm 6$ | 3.807-4.047 | $3.75 \pm 0.36$ | $-15_{-13}^{+14} \pm 4$ | $-53_{-46}^{+49} \pm 18$ | 60 | $-16_{-14}^{+15} \pm 6$ | 18 |

(incorporated into the values in Table I) and a systematic uncertainty of the same magnitude.

Finally, we account for a $0.45 \%$ uncertainty on the integrated luminosity, for the uncertainties on the $K_{S}^{0}, \eta_{c}$, and $\eta_{c}(2 S)$ branching fractions [22], and for MC-statistical uncertainties.

The results are summarized in Table I. From the signal yield $N_{\text {sig }}$ of each resonance, the integrated luminosity $L$, and the signal efficiency $\varepsilon$, we compute the product $\sigma \mathcal{B}=$ $N_{\text {sig }} /(L \varepsilon)$ of the $e^{+} e^{-} \rightarrow X e^{+} e^{-}$production cross section and the $X \rightarrow \eta_{c} \pi^{+} \pi^{-}$branching fraction. We also evaluate the results in terms of the product $\Gamma_{\gamma \gamma} \mathcal{B}$, where $\Gamma_{\gamma \gamma}$ is the two-photon width of the resonance, by utilizing the GAMGAM generator to determine the cross section as a function of $\Gamma_{\gamma \gamma}$. A $4 \%$ uncertainty is assigned to the GAMGAM calculation [2]. Since we find no significant signal for the $X$ resonances, we calculate $90 \%$ confidence-level (C.L.) Bayesian upper limits on these quantities, assuming a Gaussian likelihood incorporating statistical and systematic uncertainties.

Using the efficiency-corrected yields for the $\chi_{c 2}$ and $\eta_{c}(2 S)$ from [1], we find the relative branching fractions

$$
\begin{gather*}
\frac{\mathcal{B}\left(\eta_{c}(2 S) \rightarrow \eta_{c} \pi^{+} \pi^{-}\right)}{\mathcal{B}\left(\eta_{c}(2 S) \rightarrow K_{S}^{0} K^{+} \pi^{-}\right)}=4.9_{-3.3}^{+3.5} \pm 1.3 \pm 0.8  \tag{12}\\
\frac{\mathcal{B}\left(\chi_{c 2}(1 P) \rightarrow \eta_{c} \pi^{+} \pi^{-}\right)}{\mathcal{B}\left(\chi_{c 2}(1 P) \rightarrow K_{S}^{0} K^{+} \pi^{-}\right)}=14.5_{-8.9}^{+10.9} \pm 7.3 \pm 2.5
\end{gather*}
$$

where the first uncertainty is statistical, the second is systematic, and the third is due to the uncertainty on $\mathcal{B}\left(\eta_{c} \rightarrow\right.$ $K_{S}^{0} K^{+} \pi^{-}$) [22]. The $90 \%$ C.L. upper limits on the two ratios in Eq. (12) are 10.0 and 32.9, respectively. Using $\mathcal{B}\left(\eta_{c}(2 S) \rightarrow K_{S}^{0} K^{+} \pi^{-}\right)$and $\mathcal{B}\left(\chi_{c 2}(1 P) \rightarrow K_{S}^{0} K^{+} \pi^{-}\right)$from

Ref. [22], we obtain the $90 \%$ C.L. upper limits $\mathcal{B}\left(\eta_{c}(2 S) \rightarrow\right.$ $\left.\eta_{c} \pi^{+} \pi^{-}\right)<7.4 \%$ and $\mathcal{B}\left(\chi_{c 2}(1 P) \rightarrow \eta_{c} \pi^{+} \pi^{-}\right)<2.2 \%$.

In summary, we report a study of the process $\gamma \gamma \rightarrow$ $\eta_{c} \pi^{+} \pi^{-}$and provide, for the first time, upper limits on the branching fractions of $\chi_{c 2}(1 P)$ and $\eta_{c}(2 S)$ decays to $\eta_{c} \pi^{+} \pi^{-}$relative to the branching fractions of the decays into $K_{S}^{0} K^{+} \pi^{-}$. We also report upper limits on the products $\sigma \mathcal{B}$ and $\Gamma_{\gamma \gamma} \mathcal{B}$ for the $\chi_{c 2}(1 P), \eta_{c}(2 S), X(3872), X(3915)$, and $\chi_{c 2}(2 P)$ resonances.

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[^0]:    ${ }^{1}$ Laboratoire d'Annecy-le-Vieux de Physique des Particules (LAPP), Université de Savoie, CNRS/IN2P3, F-74941 Annecy-Le-Vieux, France
    ${ }^{2}$ Universitat de Barcelona, Facultat de Fisica, Departament ECM, E-08028 Barcelona, Spain
    ${ }^{3 a}$ INFN Sezione di Bari, I-70126 Bari, Italy
    ${ }^{3 \mathrm{~b}}$ Dipartimento di Fisica, Università di Bari, I-70126 Bari, Italy
    ${ }^{4}$ University of Bergen, Institute of Physics, N-5007 Bergen, Norway
    ${ }^{5}$ Lawrence Berkeley National Laboratory and University of California, Berkeley, California 94720, USA
    ${ }^{6}$ Ruhr Universität Bochum, Institut für Experimentalphysik 1, D-44780 Bochum, Germany
    ${ }^{7}$ University of British Columbia, Vancouver, British Columbia, Canada V6T 1Z1
    ${ }^{8}$ Brunel University, Uxbridge, Middlesex UB8 3PH, United Kingdom
    ${ }^{9}$ Budker Institute of Nuclear Physics, Novosibirsk 630090, Russia
    ${ }^{10}$ University of California at Irvine, Irvine, California 92697, USA
    ${ }^{11}$ University of California at Riverside, Riverside, California 92521, USA
    ${ }^{12}$ University of California at Santa Barbara, Santa Barbara, California 93106, USA
    ${ }^{13}$ University of California at Santa Cruz, Institute for Particle Physics, Santa Cruz, California 95064, USA
    ${ }^{14}$ California Institute of Technology, Pasadena, California 91125, USA
    ${ }^{15}$ University of Cincinnati, Cincinnati, Ohio 45221, USA
    ${ }^{16}$ University of Colorado, Boulder, Colorado 80309, USA
    ${ }^{17}$ Colorado State University, Fort Collins, Colorado 80523, USA
    ${ }^{18}$ Technische Universität Dortmund, Fakultät Physik, D-44221 Dortmund, Germany
    ${ }^{19}$ Technische Universität Dresden, Institut für Kern- und Teilchenphysik, D-01062 Dresden, Germany
    ${ }^{20}$ Laboratoire Leprince-Ringuet, Ecole Polytechnique, CNRS/IN2P3, F-91128 Palaiseau, France
    ${ }^{21}$ University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom
    ${ }^{22 a}$ INFN Sezione di Ferrara, I-44100 Ferrara, Italy
    ${ }^{22 \mathrm{~b}}$ Dipartimento di Fisica, Università di Ferrara, I-44100 Ferrara, Italy
    ${ }^{23}$ INFN Laboratori Nazionali di Frascati, I-00044 Frascati, Italy
    ${ }^{24 a}$ INFN Sezione di Genova, I-16146 Genova, Italy
    ${ }^{24 \mathrm{~b}}$ Dipartimento di Fisica, Università di Genova, I-16146 Genova, Italy
    ${ }^{25}$ Indian Institute of Technology Guwahati, Guwahati, Assam, 781 039, India
    ${ }^{26}$ Harvard University, Cambridge, Massachusetts 02138, USA
    ${ }^{27}$ Harvey Mudd College, Claremont, California 91711, USA
    ${ }^{28}$ Universität Heidelberg, Physikalisches Institut, Philosophenweg 12, D-69120 Heidelberg, Germany
    ${ }^{29}$ Humboldt-Universität zu Berlin, Institut für Physik, Newtonstrasse 15, D-12489 Berlin, Germany
    ${ }^{30}$ Imperial College London, London, SW7 2AZ, United Kingdom
    ${ }^{31}$ University of Iowa, Iowa City, Iowa 52242, USA
    ${ }^{32}$ Iowa State University, Ames, Iowa 50011-3160, USA
    ${ }^{33}$ Johns Hopkins University, Baltimore, Maryland 21218, USA
    ${ }^{34}$ Laboratoire de l'Accélérateur Linéaire, IN2P3/CNRS et Université Paris-Sud 11, Centre Scientifique d'Orsay, B.P. 34, F-91898 Orsay Cedex, France
    ${ }^{35}$ Lawrence Livermore National Laboratory, Livermore, California 94550, USA
    ${ }^{36}$ University of Liverpool, Liverpool L69 7ZE, United Kingdom
    ${ }^{37}$ Queen Mary, University of London, London, E1 4NS, United Kingdom
    ${ }^{38}$ University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom
    ${ }^{39}$ University of Louisville, Louisville, Kentucky 40292, USA
    ${ }^{40}$ Johannes Gutenberg-Universität Mainz, Institut für Kernphysik, D-55099 Mainz, Germany
    ${ }^{41}$ University of Manchester, Manchester M13 9PL, United Kingdom
    ${ }^{42}$ University of Maryland, College Park, Maryland 20742, USA
    ${ }^{43}$ University of Massachusetts, Amherst, Massachusetts 01003, USA
    ${ }^{44}$ Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, Massachusetts 02139, USA
    ${ }^{45}$ McGill University, Montréal, Québec, Canada H3A $2 T 8$
    ${ }^{46 \mathrm{a}}$ INFN Sezione di Milano, I-20133 Milano, Italy
    ${ }^{46 \mathrm{~b}}$ Dipartimento di Fisica, Università di Milano, I-20133 Milano, Italy
    ${ }^{47}$ University of Mississippi, University, Mississippi 38677, USA
    ${ }^{48}$ Université de Montréal, Physique des Particules, Montréal, Québec, Canada H3C 3J7
    ${ }^{49 \mathrm{a}}$ INFN Sezione di Napoli, I-80126 Napoli, Italy

[^1]:    *Now at: University of Tabuk, Tabuk 71491, Saudi Arabia.
    ${ }^{\dagger}$ Also at: Università di Perugia, Dipartimento di Fisica, Perugia, Italy.
    ${ }^{\ddagger}$ Now at: University of Huddersfield, Huddersfield HD1 3DH, United Kingdom.
    ${ }^{\S}$ Now at: University of South Alabama, Mobile, Alabama 36688, USA.
    "Also at: Università di Sassari, Sassari, Italy.
    ${ }^{4}$ Deceased.

