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We present measurements of the branching fractions for the decays $B^\pm \rightarrow a_1^\pm(1260)\pi^0$ and $B^\pm \rightarrow a_1^0(1260)\pi^\pm$ from a data sample of $232 \times 10^6 B\bar{B}$ pairs produced in e^+e^- annihilation through the $\Upsilon(4S)$ resonance. We measure the branching fraction $\mathcal{B}(B^\pm \rightarrow a_1^\pm(1260)\pi^0) \times \mathcal{B}(a_1^\pm(1260) \rightarrow \pi^-\pi^+\pi^\pm) = (13.2 \pm 2.7 \pm 2.1) \times 10^{-6}$ with a significance of 4.2σ , and the branching fraction $\mathcal{B}(B^\pm \rightarrow a_1^0(1260)\pi^\pm) \times \mathcal{B}(a_1^0(1260) \rightarrow \pi^-\pi^+\pi^0) = (20.4 \pm 4.7 \pm 3.4) \times 10^{-6}$ with a significance of 3.8σ , where the first error quoted is statistical and the second is systematic.

the bachelor pion evaluated in the 3π resonance rest frame. Since the a_1 and a_2 have spins of 1 and 2, respectively, the distributions of \mathcal{A} for these two resonances differ. We require $|\mathcal{A}| < 0.6$, which reduces the a_2 background by more than a factor of 2 in both decay channels.

After all the above selections, we have on average 1.20 and 1.56 candidates per event in events where there is at least one candidate, for $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$, respectively, and we select the B candidate with the $(\pi\pi)$ mass nearest to the nominal ρ mass [7]. From the simulation, we find that this algorithm selects the correct-combination candidate in $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$ in 65% and 55% of events containing multiple candidates, respectively.

We use an unbinned maximum-likelihood fit using five variables to extract the background and signal yields of $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$. We describe the B decay kinematics with the two variables ΔE and m_{ES} . We also include the invariant mass of the 3π system (m_{a_1}), the variable \mathcal{A} and a Fisher discriminant \mathcal{F} . This discriminant combines four variables: the angles with respect to the beam axis of the B momentum and B thrust axis in the c.m. frame, and the zeroth and second angular moments of the energy flow around the B thrust axis [2].

The extended likelihood function is

$$\mathcal{L} = \frac{1}{N!} \exp\left(-\sum_j n_j\right) \prod_{i=1}^N \left[\sum_j n_j \mathcal{P}_j(\vec{x}_i; \vec{\alpha}_j) \right], \quad (1)$$

where n_j is the yield of events for hypothesis j (signal, a_2 , $B\bar{B}$ charmless, $B\bar{B}$ charm, or continuum) and N is the number of events in the sample. The probabilities \mathcal{P}_j are products of probability density functions (PDF) for each of the independent variables $\vec{x}_i = \{m_{\text{ES}}, \Delta E, m_{a_1}, \mathcal{F}, \mathcal{A}\}$ evaluated for each event i . The $\vec{\alpha}_j$ are the parameters of the distributions in \vec{x}_i . By minimizing the quantity $-\ln \mathcal{L}$ in two separate fits, we determine the yields for $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$.

To take into account the relatively large number of misreconstructed signal events, the signal is separated into two components, representing the correctly reconstructed (true) and the self-cross-feed (SCF) candidates, with proportions fixed in the fit for each mode. SCF occurs when a track from an $a_1^+ \pi^0$ or $a_1^0 \pi^+$ is exchanged with a track from the rest of the event. The fraction of SCF, determined from MC, is 35% and 44% for $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$, respectively.

In addition to the a_2 , there are three main categories of backgrounds: $B\bar{B}$ charmless, $B\bar{B}$ charm, and continuum. $B\bar{B}$ backgrounds are studied using MC simulations of $B^0\bar{B}^0$ and B^+B^- decays, using a large sample equivalent to $\sim 0.8 \text{ ab}^{-1}$. There are 17 $B\bar{B}$ charmless decays for $B^+ \rightarrow a_1^+ \pi^0$ and 20 for $B^+ \rightarrow a_1^0 \pi^+$ that contribute as background. Those decays with similar distributions are grouped to form 13 and 10 hypotheses, respectively, and

are included in the fit with a fixed yield as determined from MC. The total $B\bar{B}$ charmless yields are 368 ± 92 and 755 ± 164 for $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$, respectively. These are dominated by $B \rightarrow \rho\rho$, $B \rightarrow a_1\rho$, and the other $B \rightarrow a_1\pi$ mode under study. The $B\bar{B}$ charm backgrounds are included as a single hypothesis, with the normalization of the $B\bar{B}$ charm yield as a free parameter. Continuum events come from light quark production. We establish the functional forms and parameter values of the PDFs for $B\bar{B}$ charm and $B\bar{B}$ charmless backgrounds from MC simulations. For continuum, we use off-resonance data for the Fisher, on-resonance data with $|\Delta E| > 0.1 \text{ GeV}$ for m_{ES} , and on-resonance data with $5.25 < m_{\text{ES}} < 5.27 \text{ GeV}/c^2$ for the other variables.

We model the distributions using appropriate functions. The \mathcal{A} distributions are modeled with polynomials. For the true signal component, the remaining distributions are fitted using modified Gaussians [11], and a relativistic Breit-Wigner line shape with a mass-dependent width [12], as necessary. The SCF component and the a_2 have similar shapes to the true signal but have broader or more asymmetric distributions and shifted means. The $B\bar{B}$ backgrounds and continuum distributions are modeled with modified Gaussians, polynomials, nonparametric functions [13], and, for m_{ES} , a phase-space-motivated empirical function [14]. The PDF variables are assumed to be independent except for $B^+ \rightarrow a_1^0 \pi^+$, where a two-dimensional nonparametric PDF [13] in m_{a_1} and ΔE accounts for observed correlations in the MC for both true signal events and SCF.

In the fit there are six free parameters: four yields (signal, continuum, a_2 , and $B\bar{B}$ charm background), and two continuum background parameters (ΔE polynomial coefficient and m_{ES} shape coefficient ξ [14]).

For $B^+ \rightarrow a_1^+ \pi^0$, there are 24 608 events in the data sample. We measure the raw signal yield to be 459 ± 78 events with a reconstruction efficiency of $12.5\% \pm 0.1\%$, corrected for differences in tracking and neutral particle reconstruction between data and MC. The yield of the decay $B^+ \rightarrow a_2^+ \pi^0$ is 28 ± 65 events. For $B^+ \rightarrow a_1^0 \pi^+$, there are 33 375 events in the data sample, and we measure the raw signal yield to be 382 ± 79 events with a corrected reconstruction efficiency of $7.2\% \pm 0.1\%$. The yield of the decay $B^+ \rightarrow a_2^0 \pi^+$ is 107 ± 65 events.

We confirm our fitting procedure by generating and fitting MC samples containing signal and background populations using the yields as found from data. We identify a signal yield bias for $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$ of $16.8\% \pm 0.1\%$ and $10.9\% \pm 0.1\%$, respectively. We fit for the branching fractions taking into account the fitted signal yield, the yield bias, the corrected reconstruction efficiency, daughter branching fractions, and the number of produced B mesons, assuming equal production rates of $B^0\bar{B}^0$ and B^+B^- pairs. The statistical significance is taken as the square root of the difference between the value of

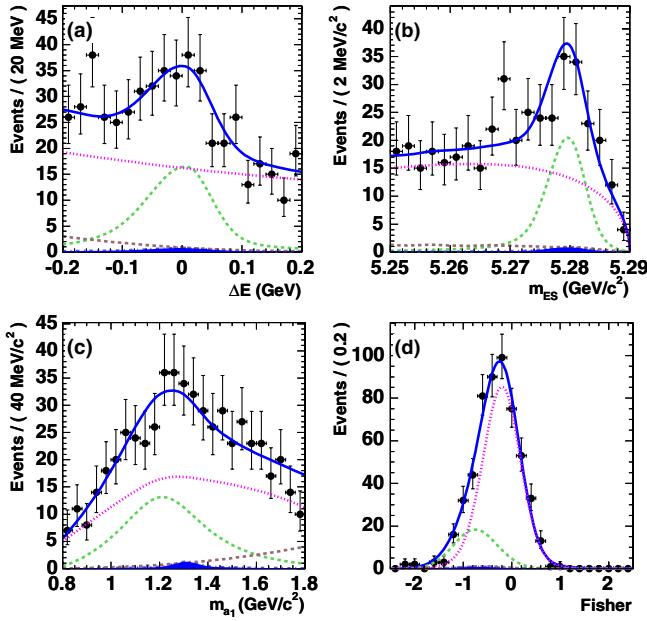


FIG. 1 (color online). Projections of (a) ΔE , (b) m_{ES} , (c) m_{a_1} , and (d) \mathcal{F} for $B^+ \rightarrow a_1^+ \pi^0$. Points represent on-resonance data, dashed lines the signal, dotted lines the continuum, dash-dotted lines the $B\bar{B}$ charm background, the filled region the a_2 background, and solid lines the full fit function. These plots are made with a requirement on the signal likelihood to enhance the signal, and thus do not show all events in the data sample.

$-2 \ln \mathcal{L}$ for zero signal and the value at its minimum. We measure the branching fraction $\mathcal{B}(B^+ \rightarrow a_1^+ \pi^0) \times \mathcal{B}(a_1^+ \rightarrow \pi^- \pi^+ \pi^+) = (13.2 \pm 2.7) \times 10^{-6}$ with a statistical significance of 5.3σ and the branching fraction $\mathcal{B}(B^+ \rightarrow a_1^0 \pi^+) \times \mathcal{B}(a_1^0 \rightarrow \pi^- \pi^+ \pi^0) = (20.4 \pm 4.7) \times 10^{-6}$ with a statistical significance of 4.7σ , where the errors are statistical.

Figures 1 and 2 show the ΔE , m_{ES} , m_{a_1} , and \mathcal{F} projections for $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$ made by selecting events with a signal likelihood (computed without the variable shown in the figure) exceeding a threshold that optimizes the expected sensitivity.

The systematic errors are summarized in Table I. We determine the sensitivity to the parameters of the signal and background PDF components by varying these within their uncertainties. The effect of varying the mass and width of the a_1 by the errors as reported in Ref. [2] is included in the PDF parameters' variation systematic. The uncertainty in the fit bias correction is taken as half of the fit bias correction. The effect of possible interference between a_2 and a_1 is estimated by adding the a_2 and a_1 amplitudes together with a varying phase difference and using half the maximum change in yield as an uncertainty. The uncertainty in SCF is investigated by varying the SCF fraction. We also perform a separate fit treating the SCF as an independent background component. The fitted branching fraction is compatible with the nominal fit within the

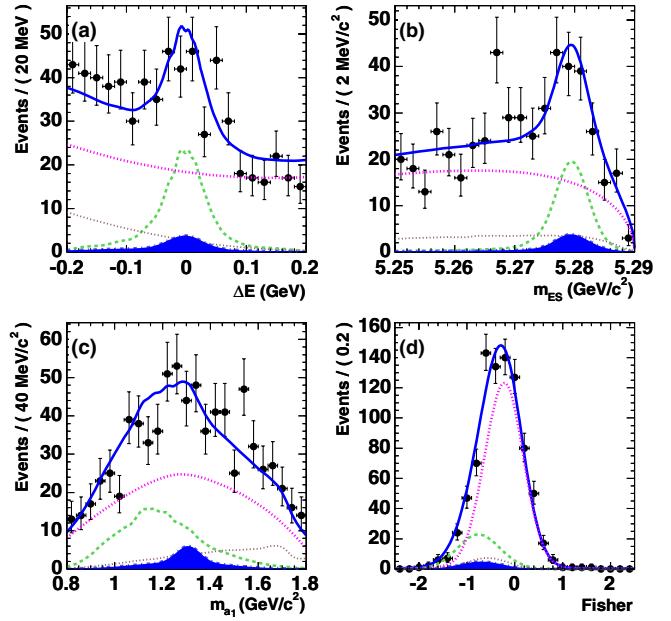


FIG. 2 (color online). Projections of (a) ΔE , (b) m_{ES} , (c) m_{a_1} , and (d) \mathcal{F} for $B^+ \rightarrow a_1^0 \pi^+$, using the same criteria and line styles as Fig. 1.

increased statistical uncertainty, but the statistical significance is reduced to 3.5σ and 3.0σ for $B^+ \rightarrow a_1^+ \pi^0$ and $B^+ \rightarrow a_1^0 \pi^+$, respectively. A systematic uncertainty of 1.6% is estimated for the difference in reconstruction efficiency in the decay modes through the dominant P -wave $(\pi\pi)_\rho$ and the S -wave $(\pi\pi)_\sigma$. An error is assigned for the uncertainty in the fixed charmless $B\bar{B}$ background yields and possible interference effects by varying the individual components by the reported error on the branching fractions [7]. The systematic errors for the flight direc-

TABLE I. Summary of systematic errors for the $a_1^+ \pi^0$ and $a_1^0 \pi^+$ branching fraction measurements.

Systematic	$a_1^+ \pi^0$	$a_1^0 \pi^+$
PDF Parameter Variation	8.6%	8.8%
Fit Bias	8.4%	5.5%
$a_1 - a_2$ Interference	6.6%	7.4%
SCF Variation	4.4%	8.2%
Tracking Efficiency	3.9%	3.9%
π^0 Efficiency	3.0%	3.0%
Flight Direction Criteria	2.0%	2.0%
P -wave and S -wave Reconstruction	1.6%	...
Charmless $B\bar{B}$ Background	1.4%	3.1%
Number of $B\bar{B}$ Pairs	1.1%	1.1%
$\cos\theta_T$ Selection Criteria	1.1%	1.8%
Track Multiplicity	1.0%	1.0%
$\rho\pi\pi$, 4π Cross Feed	0.9%	0.5%
$a_1 K$ Cross Feed	...	0.4%
Total	16%	16%

tion criteria, number of $B\bar{B}$ pairs, $\cos\theta_T$ selection criteria, track multiplicity, potential backgrounds from $\rho\pi\pi$ and 4π , and a_1K cross feed are small. The total systematic error for both modes is 16%. The significance of the branching fractions, combining both statistical and systematic errors, is 4.2σ for $B^+ \rightarrow a_1^+ \pi^0$ and 3.8σ for $B^+ \rightarrow a_1^0 \pi^+$.

In conclusion, we have measured the branching fractions $\mathcal{B}(B^\pm \rightarrow a_1^\pm(1260)\pi^0) \times \mathcal{B}(a_1^\pm(1260) \rightarrow \pi^-\pi^+\pi^\pm) = (13.2 \pm 2.7 \pm 2.1) \times 10^{-6}$ and $\mathcal{B}(B^\pm \rightarrow a_1^0(1260)\pi^\pm) \times \mathcal{B}(a_1^0(1260) \rightarrow \pi^-\pi^+\pi^0) = (20.4 \pm 4.7 \pm 3.4) \times 10^{-6}$. Neglecting isoscalar contributions to the two-pion state, we assume $\mathcal{B}(a_1^\pm(1260) \rightarrow \pi^-\pi^+\pi^\pm)$ is equal to $\mathcal{B}(a_1^\pm(1260) \rightarrow \pi^+\pi^0\pi^0)$ and $\mathcal{B}(a_1^\pm(1260) \rightarrow (3\pi)^\pm)$ is equal to 100% [7], resulting in $\mathcal{B}(B^\pm \rightarrow a_1^\pm(1260)\pi^0) = (26.4 \pm 5.4 \pm 4.1) \times 10^{-6}$. We measure $\mathcal{B}(B^\pm \rightarrow a_1^0(1260)\pi^\pm) = (20.4 \pm 4.7 \pm 3.4) \times 10^{-6}$, assuming $\mathcal{B}(a_1^0(1260) \rightarrow \pi^-\pi^+\pi^0)$ is equal to 100%. The first errors quoted are statistical and the second are systematic. The signals are seen with significances of 4.2σ and 3.8σ , respectively, and are in agreement with factorization model predictions [3].

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