

# OWA operators in the calculation of the average green-house gases emissions

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**Abstract.** This study proposes, through weighted averages and ordered weighted averaging operators, a new aggregation system for the investigation of average gases emissions. We present the ordered weighted averaging operators gases emissions, the induced ordered weighted averaging operators gases emissions, the weighted ordered weighted averaging operators gases emissions and the induced probabilistic weighted ordered weighted averaging operators gases emissions. These operators represent a new way of analyzing the average gases emissions of different variables like countries or regions. The work presents further generalizations by using generalized and quasi-arithmetic means. The article also presents an illustrative example with respect to the calculations of the average gases emissions in the European region.

Keywords: Green-house gases emission, aggregation operators, decision making, ordered weighted average.

## 1. Introduction

Within the exceptionally later decades, since of an gigantic development of the population and the need to supply nourishment for them from one hand and the other hand an immethodical utilization of fossil fuel, our planet is experiencing an unexampled growth in terms of green-house gases (GHG) emission such as CO<sub>2</sub>, CH<sub>4</sub> and N<sub>2</sub>O in its atmosphere that cause an ascending amount of global warming year by year and a drastic climate change [13,15,37].

There are many works that study the ways that can lead the GHG emission toward the minimization. [36], evaluate the potential influence of vehicle electrification on grid infrastructure and road-traffic green-house emission. [12] Study the impact of electrical power generation on GHG emission in Europe, [10] analyze green-house gases emission in concrete manufacture while there are some papers that focus on agriculture and farming [4,17,35].

Besides, although these works exist but it seems vital to present a comprehensive forecast about the future of countries based on the experts' opinions to provide a clear plan and make a suitable decision to decrease this

emission in any of the studied sectors and under various conditions.

Aggregation operators in the related literature with the aim of decision making are diverse and each of them can be used to collect the information [3,26-29]. These techniques give importance to the variables according to certain available subjective or objective findings [34,31,38,40,42].

A very popular aggregation operator is the weighted average. This aggregation operator is flexible to use in a wide range of problems. Another popular aggregation operator is the ordered weighted average (OWA) [41,45]. The OWA operator provides a parametrized family of aggregation operators between the minimum and the maximum, weighting the data according to the attitudinal character of the decision-maker. Based on this operator and with the purpose of expanding it, many authors expand and generalize it [9,16,24,39,46]. There are several types for the concept of expanding and generalizing and the most important item is the form of integrating OWA operator with some key concepts such as, using the induced variables, the probability and the weighted average. [40] propose some new aggregation operators such as the induced ordered weighted geometric averaging (IOWGA) operator, generalized

induced ordered weighted averaging (GIOWA) operator, hybrid weighted averaging (HWA) operator.

The purpose of this work is to concentrate on the analysis of the use of the aggregation operators in the calculation of green-house gases (GHG) emission with the aim of developing better decision-making techniques. To this end, the paper studies several aggregation operators including the WA [3], OWA [23,41], OWAWA and IOWAWA [25], IOWA [44], POWAWA and IPOWAWA operator [29]. With the use of each operator, a new operator for GHG emission is produced including the OWA GHG emission (OWAGE), induced OWA GHG emission (IOWAGE), ordered weighted averaging weighted average GHG emission (OWAWAGE), induced OWAWA GHG emission (IOWAWAGE), probabilistic OWAWA GHG emission (POWAWAGE) and induced probabilistic OWAWA GHG emission (IPOWAWAGE).

The work also presents further generalizations by using generalized and quasi-arithmetic means obtaining the generalized OWAGE (GOWAGE). The aim of this approach is to show a more general framework in the analysis of averages by using complex aggregations including with geometric and quadratic averages. The study presents a wide range of particular types of aggregations under this approach.

During the related literature there are several works dedicated to the application of these aggregation operators such as, demand analysis [32], economic growth analysis [33], portfolio selection [18], support vector machines [22] and the average price [30]. On the other hand, many works are dedicated to making decision in different fields to solve the problem. As an example, [7] with mixing induced OWA operators and Minkowski distances, try to present a method to decide in reinsurance. [8] present a new method for handling multi-criteria fuzzy decision-making problems by using FN-IOWA operators or in the other study, [14] analyse the origin and uses of the ordered weighted geometric operator in multicriteria decision making and [21], proposes a model for the best-suited OWA operators and [6] by using bibliometric method review the contribution in fuzzy decision-making area. This work develops OWA operators in the analysis of the average green-house gases emissions.

The work presents an application regarding the calculation of the average gases emissions in Europe. For doing so, the paper considers a multi-expert aggregation problem where four experts analyze the expected average emissions of each European country for the next period. From, the analysis develops several aggregation methods based on the tools developed in the paper including the OWAGE, IOWG and OWAWAGE operators. The main advantage of

the OWA operator is the possibility of under or overestimate the information according to the attitudinal character of the decision maker. Thus, depending on the degree of optimism or pessimism of the decision maker, the results may lead to different decisions and interpretations of the information.

This paper is organized as follows. Section 2 briefly reviews some basic OWA operators. Section 3 introduces the use of the OWA operator in the calculation of the average green-house gases emissions. Section 4 develops further generalization with generalized and quasi-arithmetic means. Section 5 presents an illustrative example regarding the calculation of average gases emissions with OWA operators. Section 6 ends the paper summarizing the main findings and conclusions of the paper.

## 2. Preliminaries

### 2.1. The induced OWA operator (IOWA)

The IOWA operator [44] is an extension of the OWA operator. The main difference between OWA and IOWA is that the reordering step is not developed with the values of the arguments  $a_i$ . In this case, the reordering step is carried out with order inducing variables. The IOWA operator also includes as particular cases the maximum, the minimum and the average criteria. It can be defined as follows.

**Definition 1.** An IOWA operator of dimension  $n$  is a mapping  $IOWA: R^n \times R^n \rightarrow R$  that has an associated weighting vector  $W$  of dimension  $n$  with  $\sum_{j=1}^n w_j = 1$  and  $w_j \in [0,1]$ , such that:

$$IOWA(\langle u_1, a_1 \rangle, \langle u_2, a_2 \rangle, \dots, \langle u_n, a_n \rangle) = \sum_{j=1}^n w_j b_j, \quad (1)$$

where  $b_j$  is the  $a_i$  value of the IOWA pair  $\langle u_i, a_i \rangle$  having the  $j$ th largest  $u_i$ .  $u_i$  is the order-ranking variable and  $a_i$  is the argument variable.

### 2.2. The ordered weighted averaging-weighted average (OWAWA)

The OWAWA operator [25] is a new model that unifies the OWA operator and the weighted average in the same formula. Therefore, both concepts can be seen as a particular case of a more general one. It can be defined as follows.

**Definition 2.** An OWAWA operator of dimension  $n$  is a mapping  $OWAWA: R^n \rightarrow R$  that has an associated weighting vector  $W$  of dimension  $n$  such that

$w_j \in [0,1]$  and  $\sum_{j=1}^n w_j = 1$ , according to the following formula:

$$OWAWA(a_1, \dots, a_n) = \sum_{j=1}^n \hat{v}_j b_j \quad (2)$$

where  $b_j$  is the  $j$ th largest of the  $a_i$ , each argument  $a_i$  has an associated weight (WA)  $v_i$  with  $\sum_{i=1}^n v_i = 1$  and  $v_i \in [0,1]$ ,  $\hat{v}_j = \beta w_j + (1-\beta)v_j$  with  $\beta \in [0,1]$  and  $v_j$  is the weight (WA)  $v_i$  ordered according to  $b_j$ , that is, according to the  $j$ th largest of the  $a_i$ .

### 2.3. The probabilistic ordered weighted averaging-weighted average (POWAWA)

The POWAWA [34] operator uses probabilities, weighted average and OWA in the same formulation. It unifies these three concepts by considering the degree of importance that each concept has in the aggregation, depending on the situation considered. The POWAWA operator is defined as follows.

**Definition 3.** A POWAWA operator of dimension  $n$  is a mapping  $POWAWA: R^n \rightarrow R$  that has an associated weighting vector  $W$  of dimension  $n$  with  $w_j \in [0,1]$  and  $\sum_{j=1}^n w_j = 1$  such that:

$$POWAWA(a_1, a_2, \dots, a_n) = \sum_{j=1}^n \hat{v}_j b_j \quad (3)$$

where  $b_j$  is the  $j$ th largest of the  $a_i$ , each argument  $a_i$  has an associated weight  $v_i$  with  $\sum_{i=1}^n v_i = 1$  and  $v_i \in [0,1]$ , a probability  $p_i$  with  $\sum_{i=1}^n p_i = 1$  and  $p_i \in [0,1]$ ,  $\hat{v}_j = C_1 w_j + C_2 v_j + C_3 p_j$ , with  $C_1, C_2$  and  $C_3 \in [0,1]$ ,  $C_1 + C_2 + C_3 = 1$  and  $v_j$   $p_j$  are the weights  $v_i$  and  $p_i$  ordered according to  $b_j$ , that is to say, according to the  $j$ th largest of the  $a_i$ .

### 2.4. The induced probabilistic OWAWA operator

The IPOWAWA [29] is an aggregation operator that extends POWAWA operator that uses order-inducing variables that represent complex reordering processes of an aggregation. Thus, it is an aggregation operator that uses induced variables, the probability, the weighted average and the OWA operator. Moreover, it can assess complex reordering processes by using order-inducing variables. Its main advantage is that it provides a more robust formulation than the

POWAWA operator because it includes a wide range of cases. It can be defined as follows.

**Definition 4.** The IPOWAWA operator of dimension  $n$  is a mapping  $IPOWAWA: R^n \times R^n \rightarrow R$  that has an associated weighting vector  $W$  of dimension  $n$  with  $w_j \in [0,1]$  and  $\sum_{j=1}^n w_j = 1$ , such that:

$$IPOWAWA(\langle u_1, e_1 \rangle, \langle u_2, e_2 \rangle, \dots, \langle u_n, e_n \rangle) = \sum_{j=1}^n \hat{v}_j b_j \quad (4)$$

where  $b_j$  is the  $a_i$  value of the IPOWAWA pair  $\langle u_i, e_i \rangle$  having the  $j$ th largest  $u_i$ ,  $u_i$  is the order-inducing variable, each argument  $a_i$  has an associated weight  $v_i$  with  $\sum_{i=1}^n v_i = 1$  and  $v_i \in [0,1]$ , a probability  $p_i$  with  $\sum_{i=1}^n p_i = 1$  and  $p_i \in [0,1]$ ,  $\hat{v}_j = C_1 w_j + C_2 v_j + C_3 p_j$ , with  $C_1, C_2$  and  $C_3 \in [0,1]$ ,  $C_1 + C_2 + C_3 = 1$ ,  $v_j$  and  $p_j$  are the weights  $v_i$  and  $p_i$  ordered according to  $b_j$ , that is to say according to the  $j$ th largest of the  $e_i$ .

## 3. Calculation of the average green-house gases (GHG) emission with OWA operators

The purpose of this paper is to calculate the average GHG emission. The average GHG emission represents a numerical value that reports the information of the GHG emission. To calculate this item, using many aggregation operators is possible likewise normal arithmetic mean. These possible aggregation operators could be WA, OWA, IOWA or a combination of them such as OWAWA, IOWAWA, etc. Through using them we prepare some possibilities for the future of GHG emission in different scenarios in a spectrum from the worst case to the best case based on experts' opinions.

The basic operator for analyzing a set of GHG emission is OWAGE. The OWAGE operator is an aggregation operator that analyses an average GHG emission under uncertainty situation. It can be defined as follows for the set of GHG emission  $A = \{e_1, e_2, \dots, e_n\}$ :

$$OWAGE(e_1, e_2, \dots, e_n) = \sum_{j=1}^n w_j f_j \quad (5)$$

where  $f_j$  is the  $j$ th largest of the  $e_i$ .

The other significant aggregation operator is the induced OWA (IOWA) that its reordering step is developed with order including variables. So, by using the IOWA operator we obtain IOWA GHG emission (IOWAGE) that can be defined as follows:

$$IOWAGE(\langle u_1, e_1 \rangle, \langle u_2, e_2 \rangle, \dots, \langle u_n, e_n \rangle) = \sum_{j=1}^n w_j f_j \quad (6)$$

where  $f_j$  is the  $e_i$  value of the IOWA pair  $\langle u_i, e_i \rangle$  having the  $j$ th largest  $u_i$ .  $u_i$  is the order-ranking variable and  $e_i$  is the argument variable.

It is important to mention that this operator is based on considering no extra information. One of the very important aspects of the average GHG emission is the importance of each of them and in other words, their weights in comparison with each other. To this end it is better to use some approaches of information aggregation that combine OWA operators and WA. In the literature there are some aggregation operators with this structure like, the WOWA operator [38], the hybrid average [26] and the OWAWA operators [25]. In this work we apply OWAWA to obtain the OWAWA GHG emission (OWAWAGE) and it is defined as follows for a set of GHG emission  $A = \{e_1, e_2, \dots, e_n\}$ :

$$OWAWAGE(e_1, e_2, \dots, e_n) = \sum_{j=1}^n \hat{v}_j f_j \quad (7)$$

where  $f_j$  is the  $j$ th largest of the  $e_i$ , each argument  $e_i$  has an associated weight (WA)  $v_i$  with  $\sum_{i=1}^n v_i = 1$  and  $v_i \in [0, 1]$ ,  $\hat{v}_j = \beta w_j + (1 - \beta)v_j$  with  $\beta \in [0, 1]$  and  $v_j$  is the weight (WA)  $v_i$  ordered according to  $b_j$ , that is, according to the  $j$ th largest of the  $e_i$ .

To focus more deeply on our contributions, we implement IOWAWA which is a combination of IOWA operators and WA in the same formulation. By using the IOWAWA operator we obtain IOWAWA GHG emission (IOWAWAGE) that can be defined as follows:

$$IOWAWAGE(\langle u_1, e_1 \rangle, \langle u_2, e_2 \rangle, \dots, \langle u_n, e_n \rangle) = \sum_{j=1}^n \hat{v}_j f_j \quad (8)$$

where  $f_j$  is the  $e_i$  value of the IOWAWA pair  $\langle u_i, e_i \rangle$  having the  $j$ th largest  $u_i$ ,  $u_i$  is the order including variable and  $e_i$  is the argument variable, each argument  $e_i$  has an associated weight (WA)  $v_i$  with  $\sum_{i=1}^n v_i = 1$  and  $v_i \in [0, 1]$ ,  $\hat{v}_j = \beta w_j + (1 - \beta)v_j$  with  $\beta \in [0, 1]$  and  $v_j$  is the weight (WA)  $v_i$  ordered according to  $f_j$ , that is, according to the  $j$ th largest  $u_i$ .

Besides, the other aspect that can be considered and leads results to a better form is probabilities in the attitudinal character of the decision-maker. For this

reason, we apply POWAWA operator. By applying the Eq. (3) we could obtain the probabilistic OWAWA GHG emission (POWAWAGE). It can be defined as follows:

$$POWAWAGE(e_1, e_2, \dots, e_n) = \sum_{j=1}^n \hat{v}_j f_j \quad (9)$$

where  $f_j$  is the  $j$ th largest of the  $e_i$ , each argument  $e_i$  has an associated weight  $v_i$  with  $\sum_{i=1}^n v_i = 1$  and  $v_i \in [0, 1]$ , a probability  $p_i$  with  $\sum_{i=1}^n p_i = 1$  and  $p_i \in [0, 1]$ ,  $\hat{v}_j = C_1 w_j + C_2 v_j + C_3 p_j$ , with  $C_1, C_2$  and  $C_3 \in [0, 1]$ ,  $C_1 + C_2 + C_3 = 1$  and  $v_j, p_j$  are the weights  $v_i$  and  $p_i$  ordered according to  $f_j$ , that is to say, according to the  $j$ th largest of the  $e_i$ .

Let us analyze the different families of IOWAWAGE and POWAWAGE in the following paragraphs

First, we are considering the two main cases of the IOWAWAGE operator that are found by analyzing the coefficient  $\beta$ . Basically:

- If  $\beta = 0$ , we get the WA.
- If  $\beta = 1$ , the IOWA operator.
- If  $\beta = 1$  and the ordered position of  $u_i$  is the same than the ordered position of  $f_i$  such that  $f_j$  is the  $j$ th largest of  $e_i$ , the OWA operator.
- Note that when  $\beta$  increases, we are giving more importance to the IOWAGE operator and when  $\beta$  decreases, we give more importance to the WA.

Another group of interesting families are the maximum-WAGE, the minimum-WAGE, the step-IOWAWAGE operator and the usual average.

- The maximum-WAGE is found when  $w_p = 1$  and  $w_j = 0$ , for all  $j \neq p$ , and  $u_p = \text{Max}\{e_i\}$ .
- The minimum-WAGE is formed when  $w_p = 1$  and  $w_j = 0$ , for all  $j \neq p$ , and  $u_p = \text{Min}\{e_i\}$ .

The arithmetic-WAGE is obtained when  $w_j = 1/n$  for all  $j$ , and the weighted average is equal to the OWA when the ordered position of  $i$  is the same as the ordered position of  $j$ . The arithmetic-WAGE (A-WAGE) can be formulated as follows:

$$A\text{-WAGE}(\langle u_1, e_1 \rangle, \langle u_2, e_2 \rangle, \dots, \langle u_n, e_n \rangle) = \frac{1}{n} \beta a_i + (1 - \beta) \sum_{i=1}^n v_i e_i, \quad (10)$$

Note that if  $v_i = 1/n$ , for all  $i$ , then, we get the unification between the arithmetic mean (and simple average) and the IOWAGE operator, that is, the

arithmetic-IOWAGE (A-IOWAGE). The A-IOWAGE operator can be formulated as follows:

$$A-IOWAGE(\langle u, e_1 \rangle, \langle u, e_2 \rangle, \dots, \langle u, e_n \rangle) = \beta \sum_{j=1}^n w_j b_j + (1-\beta) \frac{1}{n} e. \quad (11)$$

Following the OWA literature [29,41,43], we can develop many other families of IOWAWA operators such as:

- The olympic-IOWAWAGE operator ( $w_1 = w_n = 0$ , and  $w_j = 1/(n-2)$  for all others).
- The general olympic-IOWAWAGE operator ( $w_j = 0$  for  $j = 1, 2, \dots, k, n, n-1, \dots, n-k+1$ ; and for all others  $w_{j^*} = 1/(n-2k)$ , where  $k < n/2$ ).
- The S-IOWAWAGE (green-house gases emission) ( $w_1 = (1/n)(1 - (\alpha + \beta) + \alpha$ ,  
 $w_n = (1/n)(1 - (\alpha + \beta) + \beta$ , and  $w_j = (1/n)(1 - (\alpha + \beta)$  for  $j = 2$  to  $n-1$  where  $\alpha, \beta \in [0, 1]$  and  $\alpha + \beta \leq 1$ ).
- The centered-IOWAWAGE (if it is symmetric, strongly decaying from the center to the maximum and the minimum, and inclusive).

Now we consider the different families of POWAWAGE operators that are found in the weighting vector  $\hat{V}$  and the coefficients  $C_1, C_2$  and  $C_3$ .

If  $w_1 = 1$  and  $w_j = 0$ , for all  $j \neq 1$ , the POWAWAGE operator becomes the maximum probabilistic weighted average GHG emission (Max-PWAGE) which is formulated as follows:

$$Max-PWAGE = C_1 Max\{b_j\} + C_2 \sum_{i=1}^n v_i |x_i - y_i| + C_3 \sum_{i=1}^n p_i |x_i - y_i| \quad (12)$$

If  $w_n = 1$  and  $w_j = 0$ , for all  $j \neq n$ , the POWAWAGE becomes the minimum probabilistic weighted average GHG emission (Min-PWAGE), which is formulated in the following way:

$$Min-PWAGE = C_1 Min\{b_j\} + C_2 \sum_{i=1}^n v_i |x_i - y_i| + C_3 \sum_{i=1}^n p_i |x_i - y_i| \quad (13)$$

The arithmetic PWAGE (if  $w_j = 1/n$ , for all  $j$ ):

$$ArithmeticPWAGE = C_1 \left( \frac{1}{n} \sum_{j=1}^n b_j \right) + C_2 \sum_{i=1}^n v_i |x_i - y_i| + C_3 \sum_{i=1}^n p_i |x_i - y_i| \quad (14)$$

- The arithmetic POWAGE operator (if  $v_i = 1/n$ , for all  $i$ ):

$$ArithmeticPOWAGE = C_1 \sum_{j=1}^n w_j b_j + C_2 \left( \frac{1}{n} \sum_{i=1}^n |x_i - y_i| \right) + C_3 \sum_{i=1}^n p_i |x_i - y_i| \quad (15)$$

Many other particular cases can be studied by looking at different expressions of the weighting vectors and the coefficients  $C_1, C_2$  and  $C_3$ , for example:

- If  $C_1 = 1$ , we obtain the OWAGE operator.
- If  $C_2 = 1$ , the weighted GHG emission (WGE).
- If  $C_3 = 1$ , the probabilistic GHG emission (PGE).
- If  $C_1 = 0$ , the probabilistic weighted averaging GHG emission (PWAGE).
- If  $C_2 = 0$ , the probabilistic OWA GHG emission (POWAGE).
- If  $C_3 = 0$ , the OWAWA GHG emission (OWAWAGE) [31].

**Example 1.** Assume we have the following arguments  $A = (60, 40, 70, 20)$  that represent a set of four different gases emissions and the following weighting vector  $W = (0.50, 0.25, 0.15, 0.10)$ . If we aggregate the WA aggregation, we get the following result:

$$WAGE = 0.50 \times 60 + 0.25 \times 40 + 0.15 \times 70 + 0.10 \times 20 = 52.50,$$

Now we assume the same arguments and the same weighting vector. If we aggregate OWA aggregation, we get the following result:

$$OWAGE = 0.50 \times 70 + 0.25 \times 60 + 0.15 \times 40 + 0.10 \times 20 = 58.$$

### Generalizations with generalized and quasi-arithmetic means

Generalization of the OWA operators is possible to do by generalized and quasi-arithmetic averaging aggregation operators that as the most common one generalized OWA (GOWA) [43] and then quasi-arithmetic OWA (Quasi-OWA) [11] are formed. These functions apply a general framework including particular cases. The GOWA operator applied to the analysis of gases emissions is called GOWA gases emissions (GOWAGE) and is defined as follows.

**Definition 8.** A GOWAGE operator of dimension  $n$  is a mapping  $GOWA : R^n \rightarrow R$  that has an associated weighting vector  $W$  of dimension  $n$  with  $\sum_{j=1}^n w_j = 1$  and  $w_j \in [0, 1]$ , such that:

$$GOWAGE(e_1, e_2, \dots, e_n) = \left( \sum_{j=1}^n w_j b_j^\lambda \right)^{1/\lambda} \quad (16)$$

where  $b_j$  is the  $j$ th largest of the  $e_j$ , and  $\lambda$  is a parameter such that  $\lambda \in (-\infty, \infty) - \{0\}$ .

Like the section 3, this operator also has the particular cases of the maximum, the minimum and the generalized mean (GM). Besides, there are some special cases that can be obtained by maneuvering on the values of  $\lambda$ , such as:

Table 1 European average GHG emission according to different scenario-expert 1

Country	Abbreviation	Population	Weight	Scenario 1	Scenario 2	Scenario 3	Scenario 4	Scenario 5	Scenario 6	Scenario 7
Albania	ALB	2,934,363	0.003959	0.21	0.18	0.26	0.25	0.31	0.19	0.24
Andorra	AND	76,953	0.000104	0.39	0.46	0.13	0.40	0.43	0.39	0.15
Austria	AUT	8,751,820	0.011808	0.13	0.25	0.15	0.31	0.26	0.22	0.22
Belarus	BLR	9,452,113	0.012753	0.36	0.27	0.30	0.45	0.32	0.42	0.13
Belgium	BEL	11,498,519	0.015515	0.47	0.44	0.32	0.39	0.21	0.27	0.46
Bosnia and Herzegovina	BIH	3,503,554	0.004727	0.23	0.34	0.38	0.14	0.44	0.28	0.24
Bulgaria	BGR	7,036,848	0.009495	0.15	0.22	0.37	0.35	0.44	0.15	0.25
Cyprus	CYP	1,189,085	0.001604	0.47	0.48	0.47	0.15	0.14	0.37	0.13
Czech R	CZE	10,625,250	0.014336	0.15	0.42	0.39	0.37	0.14	0.50	0.47
Denmark	DNK	5,754,356	0.007764	0.24	0.35	0.13	0.17	0.49	0.25	0.18
Estonia	EST	1,306,788	0.001763	0.49	0.31	0.27	0.27	0.15	0.36	0.46
Finland	FIN	5,542,517	0.007478	0.14	0.22	0.28	0.20	0.50	0.19	0.34
France	FRA	65,233,271	0.088017	0.19	0.23	0.23	0.43	0.20	0.18	0.46
Germany	DEU	82,293,457	0.111035	0.16	0.49	0.47	0.29	0.26	0.17	0.22
Greece	GRC	11,142,161	0.015034	0.32	0.46	0.45	0.42	0.29	0.29	0.22
Hungary	HUN	9,688,847	0.013073	0.18	0.34	0.26	0.47	0.37	0.37	0.16
Iceland	ISL	337,780	0.000456	0.34	0.41	0.22	0.39	0.22	0.24	0.19
R Ireland	IRL	4,803,748	0.006482	0.47	0.13	0.39	0.27	0.35	0.36	0.46
Italy	ITA	59,290,969	0.079999	0.44	0.14	0.50	0.20	0.49	0.19	0.23
Kosovo	RKS	1,808,698	0.002440	0.21	0.28	0.39	0.13	0.40	0.39	0.41
Latvia	LVA	1,929,938	0.002604	0.31	0.14	0.27	0.38	0.23	0.13	0.26
Liechtenstein	LIE	38,155	0.000051	0.46	0.27	0.33	0.43	0.16	0.27	0.35
Lithuania	LTU	2,876,475	0.003881	0.28	0.31	0.36	0.28	0.29	0.20	0.46
Luxembourg	LUX	590,321	0.000796	0.23	0.34	0.26	0.33	0.18	0.48	0.13
Macedonia	MKD	2,085,051	0.002813	0.18	0.33	0.37	0.14	0.41	0.25	0.43
Malta	MLT	432,089	0.000583	0.26	0.41	0.48	0.43	0.41	0.32	0.39
Moldova	MDA	4,041,065	0.005452	0.46	0.38	0.48	0.14	0.31	0.47	0.18
Monaco	MCO	38,897	0.000052	0.20	0.16	0.13	0.45	0.37	0.22	0.48
Montenegro	MNE	629,219	0.000849	0.28	0.47	0.19	0.13	0.20	0.18	0.44
Netherlands	NLD	17,084,459	0.023051	0.34	0.27	0.16	0.31	0.46	0.31	0.48
Norway	NOR	5,353,363	0.007223	0.23	0.27	0.36	0.18	0.32	0.28	0.35
Poland	POL	38,104,832	0.051413	0.50	0.27	0.19	0.44	0.20	0.13	0.26
Portugal	PRT	10,291,196	0.013886	0.38	0.33	0.30	0.30	0.32	0.35	0.50
Romania	ROU	19,580,634	0.026419	0.20	0.33	0.29	0.14	0.16	0.46	0.20
Russia	RUS	143,964,709	0.194246	0.17	0.30	0.18	0.26	0.18	0.45	0.36
San Marino	SMR	33,557	0.000045	0.50	0.36	0.17	0.43	0.30	0.49	0.37
Serbia	SRB	8,762,027	0.011822	0.23	0.30	0.16	0.45	0.19	0.23	0.32
Slovakia	SVK	5,449,816	0.007353	0.48	0.49	0.30	0.30	0.43	0.26	0.39
Slovenia	SVN	2,081,260	0.002808	0.25	0.25	0.50	0.18	0.15	0.49	0.45
Spain	ESP	46,397,452	0.062602	0.17	0.13	0.26	0.18	0.20	0.44	0.43
Sweden	SWE	9,982,709	0.013469	0.44	0.29	0.30	0.37	0.45	0.32	0.48
Switzerland	CHE	8,544,034	0.011528	0.21	0.42	0.27	0.50	0.41	0.41	0.25
Ukraine	UKR	44,009,214	0.059380	0.45	0.47	0.45	0.22	0.17	0.47	0.21
United Kingdom	GBR	66,573,504	0.089825	0.40	0.49	0.17	0.42	0.35	0.29	0.27
Vatican city	VAT	801	0.000001	0.23	0.28	0.16	0.27	0.37	0.23	0.18
European average		741,145,874	1	0.310	0.323	0.304	0.299	0.307	0.314	0.323

Table 2 European average GHG emission according to different scenarios-expert 2

Abbr.	1	2	3	4	5	6	7
ALB	0.22	0.48	0.39	0.27	0.17	0.35	0.26
AND	0.26	0.38	0.49	0.29	0.18	0.22	0.14
AUT	0.45	0.20	0.39	0.21	0.13	0.47	0.35
BLR	0.20	0.46	0.24	0.25	0.45	0.16	0.24
BEL	0.49	0.43	0.14	0.21	0.20	0.42	0.40
BIH	0.48	0.48	0.15	0.43	0.39	0.33	0.26
BGR	0.37	0.23	0.42	0.16	0.38	0.39	0.29
CYP	0.28	0.34	0.26	0.23	0.25	0.22	0.36
CZE	0.16	0.27	0.32	0.15	0.36	0.44	0.20
DNK	0.25	0.18	0.32	0.16	0.39	0.29	0.45
EST	0.18	0.50	0.22	0.28	0.14	0.40	0.18
FIN	0.30	0.49	0.29	0.41	0.38	0.50	0.35
FRA	0.34	0.25	0.19	0.34	0.50	0.20	0.26
DEU	0.13	0.44	0.24	0.31	0.32	0.44	0.13
GRC	0.17	0.26	0.16	0.43	0.17	0.43	0.31
HUN	0.48	0.21	0.20	0.50	0.44	0.41	0.38
ISL	0.21	0.33	0.24	0.42	0.34	0.44	0.13
IRL	0.13	0.38	0.13	0.23	0.25	0.50	0.25
ITA	0.47	0.35	0.34	0.30	0.26	0.33	0.34
RKS	0.45	0.46	0.18	0.35	0.34	0.25	0.45
LVA	0.25	0.15	0.33	0.50	0.42	0.34	0.27
LIE	0.35	0.37	0.15	0.16	0.26	0.27	0.29
LTU	0.20	0.42	0.17	0.17	0.29	0.48	0.50
LUX	0.32	0.33	0.13	0.24	0.27	0.34	0.49
MKD	0.40	0.16	0.41	0.46	0.45	0.38	0.45
MLT	0.46	0.22	0.20	0.23	0.35	0.19	0.32
MDA	0.45	0.22	0.24	0.39	0.39	0.44	0.25
MCO	0.45	0.32	0.24	0.50	0.26	0.42	0.28
MNE	0.24	0.23	0.39	0.40	0.20	0.27	0.32
NLD	0.39	0.13	0.19	0.27	0.44	0.13	0.27
NOR	0.23	0.20	0.28	0.32	0.44	0.28	0.26
POL	0.24	0.13	0.27	0.22	0.50	0.38	0.18
PRT	0.42	0.33	0.43	0.24	0.35	0.30	0.37
ROU	0.49	0.34	0.31	0.37	0.15	0.34	0.13
RUS	0.15	0.40	0.37	0.38	0.23	0.34	0.47
SMR	0.22	0.33	0.28	0.28	0.36	0.49	0.21
SRB	0.44	0.30	0.21	0.16	0.28	0.45	0.49
SVK	0.13	0.40	0.46	0.22	0.26	0.27	0.36
SVN	0.44	0.37	0.16	0.25	0.45	0.49	0.41
ESP	0.19	0.39	0.25	0.16	0.42	0.31	0.50
SWE	0.26	0.38	0.47	0.38	0.27	0.37	0.46
CHE	0.47	0.33	0.28	0.34	0.31	0.43	0.43
UKR	0.48	0.37	0.13	0.36	0.20	0.36	0.15
GBR	0.46	0.32	0.21	0.41	0.42	0.31	0.44
VAT	0.22	0.18	0.15	0.22	0.40	0.50	0.19
EA.	<b>0.319</b>	<b>0.321</b>	<b>0.267</b>	<b>0.301</b>	<b>0.320</b>	<b>0.357</b>	<b>0.316</b>

Abbr.: Abbreviation, EA.: European average

- If  $\lambda = 1$ , the usual OWAGE operator.
- If  $\lambda \rightarrow 0$ , the ordered weighted geometric average gases emissions (OWGAGE).
- If  $\lambda = 2$ , the ordered weighted quadratic average gases emissions (OWQAGE).
- If  $\lambda = -1$ , the ordered weighted harmonic average gases emissions (OWHAGE).

Table 3 European average GHG emission according to different scenarios-expert 3

Abbr.	1	2	3	4	5	6	7
ALB	0.29	0.31	0.37	0.21	0.17	0.35	0.26
AND	0.36	0.36	0.24	0.29	0.22	0.28	0.27
AUT	0.22	0.29	0.35	0.35	0.37	0.29	0.38
BLR	0.32	0.24	0.18	0.23	0.22	0.37	0.32
BEL	0.22	0.19	0.37	0.18	0.19	0.25	0.34
BIH	0.38	0.19	0.38	0.32	0.32	0.26	0.30
BGR	0.28	0.25	0.15	0.37	0.28	0.21	0.38
CYP	0.36	0.19	0.26	0.26	0.17	0.33	0.29
CZE	0.19	0.32	0.23	0.16	0.23	0.27	0.30
DNK	0.29	0.29	0.15	0.38	0.36	0.15	0.27
EST	0.22	0.20	0.36	0.23	0.33	0.26	0.35
FIN	0.24	0.36	0.32	0.16	0.33	0.34	0.33
FRA	0.35	0.34	0.24	0.36	0.28	0.17	0.26
DEU	0.38	0.34	0.38	0.37	0.15	0.28	0.34
GRC	0.21	0.20	0.28	0.18	0.31	0.17	0.25
HUN	0.25	0.26	0.38	0.22	0.38	0.17	0.37
ISL	0.23	0.18	0.16	0.22	0.37	0.18	0.24
IRL	0.28	0.21	0.38	0.33	0.28	0.30	0.36
ITA	0.18	0.34	0.23	0.16	0.38	0.16	0.28
RKS	0.36	0.16	0.34	0.17	0.17	0.21	0.20
LVA	0.31	0.19	0.20	0.24	0.15	0.26	0.30
LIE	0.26	0.32	0.31	0.22	0.36	0.27	0.26
LTU	0.22	0.24	0.32	0.15	0.28	0.36	0.33
LUX	0.17	0.21	0.19	0.21	0.23	0.29	0.21
MKD	0.29	0.35	0.35	0.25	0.16	0.35	0.27
MLT	0.22	0.34	0.23	0.25	0.18	0.29	0.16
MDA	0.32	0.20	0.26	0.16	0.23	0.23	0.34
MCO	0.32	0.17	0.32	0.36	0.27	0.38	0.20
MNE	0.15	0.26	0.18	0.24	0.24	0.31	0.28
NLD	0.18	0.18	0.22	0.30	0.32	0.20	0.34
NOR	0.19	0.17	0.29	0.18	0.26	0.28	0.22
POL	0.34	0.22	0.34	0.23	0.29	0.23	0.29
PRT	0.33	0.22	0.25	0.21	0.19	0.27	0.20
ROU	0.18	0.21	0.24	0.29	0.24	0.18	0.34
RUS	0.30	0.28	0.34	0.33	0.35	0.18	0.17
SMR	0.16	0.38	0.30	0.20	0.37	0.16	0.16
SRB	0.15	0.27	0.22	0.21	0.27	0.16	0.34
SVK	0.23	0.33	0.15	0.33	0.30	0.21	0.19
SVN	0.20	0.35	0.24	0.22	0.36	0.26	0.32
ESP	0.37	0.37	0.21	0.21	0.22	0.27	0.20
SWE	0.27	0.38	0.33	0.33	0.25	0.26	0.20
CHE	0.28	0.27	0.30	0.35	0.24	0.30	0.34
UKR	0.32	0.33	0.33	0.15	0.32	0.30	0.36
GBR	0.37	0.37	0.38	0.15	0.23	0.23	0.29
VAT	0.15	0.38	0.15	0.26	0.31	0.20	0.26
EA.	<b>0.264</b>	<b>0.271</b>	<b>0.276</b>	<b>0.248</b>	<b>0.270</b>	<b>0.254</b>	<b>0.281</b>

Quasi-arithmetic OWA gases emissions (Quasi-OWAGE) operator is the other generalization that uses the quasi-arithmetic means instead of the generalized means. So, it replaces the parameter  $\lambda$  by a strictly continuous monotonic function  $g$ .

**Definition 9.** A Quasi-OWAGE operator of dimension  $n$  is a mapping Quasi-OWAGE:  $R^n \rightarrow R$  that has an associated weighting vector  $W$  of dimension  $n$  with

$$\sum_{j=1}^n w_j = 1 \text{ and } w_j \in [0, 1], \text{ then:}$$

Table 4 European average GHG emission according to different scenarios-expert 4

Abbr.	1	2	3	4	5	6	7
ALB	0.33	0.36	0.28	0.25	0.29	0.34	0.19
AND	0.21	0.28	0.25	0.35	0.24	0.39	0.34
AUT	0.38	0.38	0.22	0.35	0.39	0.28	0.28
BLR	0.39	0.48	0.34	0.23	0.26	0.41	0.26
BEL	0.42	0.25	0.47	0.33	0.44	0.22	0.29
BIH	0.37	0.44	0.44	0.32	0.32	0.48	0.23
BGR	0.31	0.38	0.45	0.38	0.32	0.49	0.24
CYP	0.28	0.28	0.27	0.34	0.32	0.31	0.34
CZE	0.26	0.48	0.23	0.32	0.45	0.49	0.38
DNK	0.29	0.49	0.47	0.26	0.26	0.40	0.32
EST	0.32	0.36	0.42	0.27	0.34	0.26	0.33
FIN	0.48	0.38	0.26	0.45	0.47	0.39	0.34
FRA	0.38	0.28	0.29	0.39	0.37	0.40	0.46
DEU	0.24	0.26	0.22	0.26	0.27	0.27	0.45
GRC	0.48	0.32	0.37	0.27	0.28	0.41	0.45
HUN	0.44	0.36	0.23	0.26	0.34	0.25	0.27
ISL	0.31	0.29	0.32	0.39	0.19	0.27	0.28
IRL	0.46	0.22	0.30	0.29	0.30	0.43	0.48
ITA	0.31	0.38	0.40	0.41	0.42	0.28	0.41
RKS	0.22	0.34	0.31	0.25	0.32	0.37	0.39
LVA	0.31	0.49	0.35	0.30	0.42	0.31	0.38
LIE	0.43	0.22	0.31	0.29	0.45	0.22	0.22
LTU	0.49	0.35	0.42	0.29	0.32	0.40	0.34
LUX	0.36	0.25	0.30	0.29	0.36	0.41	0.28
MKD	0.44	0.31	0.40	0.37	0.46	0.39	0.42
MLT	0.41	0.34	0.32	0.35	0.36	0.44	0.43
MDA	0.43	0.35	0.43	0.49	0.37	0.44	0.39
MCO	0.44	0.19	0.37	0.36	0.26	0.29	0.18
MNE	0.34	0.32	0.27	0.14	0.28	0.32	0.41
NLD	0.30	0.37	0.35	0.38	0.49	0.35	0.22
NOR	0.49	0.25	0.39	0.40	0.41	0.32	0.38
POL	0.44	0.36	0.32	0.28	0.48	0.36	0.42
PRT	0.38	0.45	0.49	0.33	0.27	0.41	0.23
ROU	0.40	0.38	0.35	0.32	0.29	0.27	0.32
RUS	0.35	0.27	0.32	0.33	0.31	0.27	0.40
SMR	0.27	0.40	0.36	0.27	0.44	0.30	0.39
SRB	0.49	0.28	0.27	0.38	0.45	0.38	0.44
SVK	0.37	0.31	0.42	0.30	0.41	0.42	0.42
SVN	0.31	0.35	0.36	0.43	0.43	0.30	0.25
ESP	0.44	0.41	0.24	0.25	0.34	0.46	0.27
SWE	0.28	0.45	0.49	0.39	0.24	0.49	0.42
CHE	0.24	0.39	0.30	0.41	0.30	0.27	0.46
UKR	0.34	0.40	0.42	0.25	0.29	0.34	0.42
GBR	0.26	0.39	0.37	0.43	0.38	0.30	0.27
VAT	0.18	0.12	0.21	0.19	0.23	0.15	0.20
EA.	0.366	0.348	0.342	0.330	0.359	0.353	0.351

$$Quasi-OWAGE(e_1, e_2, \dots, e_n) = g^{-1} \left( \sum_{j=1}^n w_j g(b_{(j)}) \right) \quad (17)$$

where  $b_j$  is the  $j$ th largest of the  $e_i$  and  $g$  is strictly continuous monotonic function.

### 5. Illustrative example

In this section through a numerical example we try to show the applicability of OWA operators. This work concentrates on the calculation of different OWA operators' aggregation on green-house gases emission

of European countries and makes a comparison on them to gain a clear decision about their possible future scenarios. To this end and with the purpose of giving a correct overview to solve the problem, a group of four experts analyses the information in seven scenarios. This step by step process can be explained as follows.

**Step 1:** Four experts analyze the green-house gases emission of European countries in seven possible scenarios in future based on the environmental and economic situation of the mentioned country. Table 1, 2, 3 and 4 represent the opinions of the experts. Table 2,3 and 4 are the same as 1 but to avoid repeating, we summarized them to a short form.

**Step 2:** The next step belongs to unify the experts' opinions to achieve to a collective result that cover all the information. To this end, it is necessary to assign the degree of importance to each of the experts:  $Z = (0.4, 0.35, 0.15, 0.1)$ . Table 5 reports the collective results of each country.

**Step 3:** Based on the objective of this work it is necessary to assign weighting vectors to consider subjective and objective information and an attitudinal character that underestimates the results.

- OWA:  
 $W = (0.1; 0.15; 0.1; 0.2; 0.15; 0.25; 0.05)$
- Weighted average:  
 $V = (0.2; 0.15; 0.1; 0.15; 0.1; 0.1; 0.2)$
- Probability:  
 $P = (0.1; 0.2; 0.1; 0.1; 0.2; 0.1; 0.2)$
- OWAWA:  $\beta = 0.3$
- POWAWA:  $C_1 = 0.2; C_2 = 0.4; C_3 = 0.4$
- $U = (0.6; 0.2; 0.4; 0.7; 0.3; 0.4; 0.8)$

**Step 4:** Present the obtained results of the average green-house gases for each country for the OWAGE, WAGE, OWAWAGE, IOWAGE, IOWAWAGE, POWAWAGE and IPOWAWAGE. Table 6 dedicates to the aggregated results.

**Step 5:** Rank the countries from the lowest to the highest in each of the operators to draw some conclusions. Table 7 presents the results of this ranking based on the abbreviation of the name of each country.

### 6. Conclusions

The purpose of this study is to concentrate on the analysis of the use of the aggregation operators in the calculation of GHG emission with the aim of developing better decision-making techniques. In this study we reviewed some of the important operators of the family of OWA. This review started with simple WA and continued with OWA operator.



Table 5 European average GHG emission according to different scenario-collective results

Country	Scenario 1	Scenario 2	Scenario 3	Scenario 4	Scenario 5	Scenario 6	Scenario 7
Albania	0.24	0.32	0.32	0.25	0.24	0.29	0.25
Andorra	0.32	0.40	0.28	0.34	0.29	0.31	0.18
Austria	0.28	0.25	0.27	0.29	0.24	0.32	0.30
Belarus	0.30	0.35	0.27	0.33	0.34	0.32	0.21
Belgium	0.43	0.38	0.28	0.29	0.23	0.31	0.40
Bosnia and Herzegovina	0.35	0.38	0.31	0.29	0.39	0.31	0.26
Bulgaria	0.26	0.24	0.36	0.29	0.38	0.28	0.28
Cyprus	0.37	0.37	0.35	0.21	0.20	0.31	0.26
Czech R	0.17	0.36	0.33	0.26	0.26	0.44	0.34
Denmark	0.26	0.30	0.23	0.21	0.41	0.26	0.30
Estonia	0.32	0.37	0.28	0.27	0.19	0.35	0.33
Finland	0.25	0.35	0.29	0.29	0.43	0.34	0.34
France	0.29	0.26	0.22	0.38	0.33	0.21	0.36
Germany	0.19	0.43	0.35	0.31	0.27	0.29	0.23
Greece	0.27	0.34	0.32	0.37	0.25	0.33	0.28
Hungary	0.32	0.28	0.25	0.42	0.39	0.34	0.28
Iceland	0.28	0.34	0.23	0.38	0.28	0.30	0.19
R Ireland	0.32	0.24	0.29	0.27	0.30	0.41	0.37
Italy	0.40	0.27	0.39	0.25	0.39	0.24	0.29
Kosovo	0.32	0.33	0.30	0.23	0.34	0.31	0.39
Latvia	0.29	0.19	0.29	0.39	0.30	0.24	0.28
Liechtenstein	0.39	0.31	0.26	0.29	0.25	0.27	0.30
Lithuania	0.26	0.34	0.29	0.22	0.29	0.34	0.44
Luxembourg	0.27	0.31	0.21	0.28	0.24	0.40	0.28
Macedonia	0.30	0.27	0.38	0.29	0.39	0.32	0.41
Malta	0.34	0.33	0.33	0.33	0.35	0.28	0.34
Moldova	0.43	0.29	0.36	0.27	0.33	0.42	0.25
Monaco	0.33	0.22	0.22	0.45	0.31	0.32	0.34
Montenegro	0.25	0.34	0.27	0.24	0.21	0.25	0.37
Netherlands	0.33	0.22	0.20	0.30	0.44	0.23	0.36
Norway	0.25	0.23	0.32	0.25	0.36	0.28	0.30
Poland	0.38	0.22	0.25	0.32	0.35	0.26	0.25
Portugal	0.39	0.33	0.36	0.27	0.31	0.33	0.38
Romania	0.32	0.32	0.30	0.26	0.18	0.36	0.21
Russia	0.20	0.33	0.28	0.32	0.24	0.35	0.37
San Marino	0.33	0.36	0.25	0.33	0.35	0.42	0.28
Serbia	0.32	0.29	0.20	0.31	0.26	0.31	0.39
Slovakia	0.31	0.42	0.35	0.28	0.35	0.27	0.35
Slovenia	0.32	0.32	0.33	0.24	0.31	0.44	0.40
Spain	0.23	0.29	0.25	0.18	0.29	0.37	0.40
Sweden	0.34	0.35	0.38	0.37	0.34	0.35	0.43
Switzerland	0.31	0.36	0.28	0.41	0.34	0.39	0.35
Ukraine	0.43	0.41	0.32	0.26	0.22	0.39	0.23
United Kingdom	0.40	0.40	0.24	0.38	0.36	0.29	0.33
Vatican city	0.21	0.24	0.16	0.24	0.36	0.31	0.20
European average	0.31	0.32	0.29	0.30	0.31	0.32	0.32

Moreover, we also analyzed some operators that form by combination of two or more aggregation operators. So, these operators are, IOWAGE, OWAAGE, IOWAAGE, POWAAGE and IPOWAAGE.

In addition, through these formulations, we found some particular cases in either IOWAAGE or POWAAGE operators such as, olympic-IOWAAGE, S-IOWAAGE, centered-IOWAAGE, maximum, minimum and arithmetic probabilistic weighted average, and arithmetic probabilistic ordered weighted average.

Furthermore, some other generalizations are developed by using generalized and quasi-arithmetic means obtaining the GOWAGE and the Quasi-OWAGE operators.

The study provides a simple example to review the function of two simple aggregations operators of average green-house gases emission. During this example we review weighted average gases emission (WAGE) and ordered weighted average gases emission (OWAGE) to represent the difference between the result of the calculation based on these operators.

Table 6 European average GHG emission according to different scenario-aggregated results 1

Country	WAGE	OWAGE	OWAWAGE	IOWAGE	IOWAWAGE	POWAWAGE	IPOWAWAGE
Albania	0.274	0.268	0.267	0.267	0.267	0.269	0.269
Andorra	0.320	0.310	0.304	0.300	0.301	0.303	0.301
Austria	0.282	0.317	0.291	0.279	0.280	0.285	0.277
Belarus	0.317	0.333	0.308	0.307	0.300	0.306	0.301
Belgium	0.319	0.276	0.328	0.308	0.337	0.329	0.335
Bosnia and Herzegovina	0.330	0.339	0.328	0.330	0.325	0.329	0.327
Bulgaria	0.298	0.334	0.304	0.316	0.299	0.304	0.300
Cyprus	0.288	0.288	0.294	0.276	0.291	0.292	0.289
Czech R	0.322	0.280	0.292	0.310	0.301	0.300	0.306
Denmark	0.278	0.307	0.287	0.293	0.282	0.292	0.289
Estonia	0.302	0.304	0.307	0.284	0.301	0.304	0.300
Finland	0.331	0.320	0.320	0.339	0.326	0.328	0.332
France	0.286	0.315	0.306	0.294	0.299	0.304	0.300
Germany	0.303	0.287	0.285	0.286	0.285	0.291	0.290
Greece	0.318	0.270	0.295	0.304	0.305	0.297	0.304
Hungary	0.343	0.333	0.327	0.342	0.330	0.327	0.329
Iceland	0.303	0.281	0.280	0.284	0.281	0.280	0.280
Ireland	0.316	0.312	0.314	0.321	0.316	0.312	0.314
Italy	0.303	0.316	0.318	0.324	0.320	0.318	0.319
Kosovo	0.305	0.301	0.314	0.313	0.318	0.319	0.321
Latvia	0.284	0.337	0.300	0.293	0.287	0.291	0.282
Liechtenstein	0.289	0.286	0.300	0.284	0.299	0.297	0.296
Lithuania	0.303	0.317	0.318	0.307	0.315	0.322	0.320
Luxembourg	0.297	0.265	0.277	0.281	0.281	0.278	0.281
Macedonia	0.328	0.349	0.340	0.349	0.340	0.342	0.342
Malta	0.320	0.296	0.319	0.326	0.328	0.322	0.328
Moldova	0.344	0.304	0.323	0.344	0.335	0.323	0.330
Monaco	0.320	0.319	0.318	0.318	0.318	0.313	0.313
Montenegro	0.263	0.323	0.296	0.258	0.277	0.293	0.280
Netherlands	0.288	0.297	0.301	0.310	0.305	0.304	0.307
Norway	0.282	0.283	0.280	0.300	0.286	0.284	0.288
Poland	0.288	0.286	0.291	0.297	0.294	0.288	0.290
Portugal	0.324	0.325	0.337	0.329	0.338	0.336	0.337
Romania	0.289	0.289	0.280	0.269	0.274	0.274	0.270
Russia	0.304	0.301	0.300	0.294	0.298	0.302	0.300
San Marino	0.348	0.320	0.324	0.336	0.329	0.326	0.330
Serbia	0.293	0.292	0.304	0.289	0.303	0.303	0.302
Slovakia	0.321	0.290	0.320	0.322	0.330	0.329	0.335
Slovenia	0.335	0.364	0.342	0.337	0.334	0.341	0.336
Spain	0.285	0.294	0.291	0.290	0.290	0.295	0.294
Sweden	0.356	0.359	0.364	0.360	0.365	0.365	0.365
Switzerland	0.361	0.336	0.345	0.350	0.350	0.347	0.349
Ukraine	0.330	0.281	0.312	0.306	0.319	0.311	0.316
United Kingdom	0.342	0.354	0.353	0.333	0.347	0.351	0.347
Vatican city	0.264	0.283	0.251	0.265	0.246	0.252	0.249
European average	0.310	0.321	0.314	0.309	0.310	0.313	0.310

We also analyzed the applicability of these approaches for the process of decision-making problem in GHG emission. To achieve to this aim, we implement an illustrative example regarding the calculation of the average of green-house gases emission among European countries. To this end we collect the opinions of the four experts in this area in seven various scenarios in a multi-person analysis. Based on this example, and through five steps we obtain the final table that demonstrate comprehensively the situation of the European countries in a descending trend based on the results of different aggregation operators that

can occur according to different scenarios between the minimum and maximum results.

In the future research, by using the different aggregation operators such as logarithmic [1], heavy [19,20], Bonferroni [5] and prioritized [2], we calculate the average GHG emission in a wide range of scenarios among the countries also among different continents.

Table 7 European average GHG emission according to different scenario-aggregated results 2

Rank	WAGE	OWAGE	OWAWAGE	IOWAGE	IOWAWAGE	POWAWAGE	IPOWAWAGE
1	MNE	LUX	VAT	MNE	VAT	VAT	VAT
2	VAT	ALB	ALB	VAT	ALB	ALB	ALB
3	ALB	GRC	LUX	ALB	ROU	ROU	ROU
4	DNK	BEL	ROU	ROU	MNE	LUX	AUT
5	AUT	CZE	NOR	CYP	AUT	ISL	MNE
6	NOR	UKR	ISL	AUT	ISL	NOR	ISL
7	LVA	ISL	DEU	LUX	LUX	AUT	LUX
8	ESP	NOR	DNK	LIE	DNK	POL	LVA
9	FRA	VAT	POL	EST	DEU	DEU	NOR
10	NLD	POL	ESP	ISL	NOR	LVA	DNK
11	POL	LIE	AUT	DEU	LVA	CYP	CYP
12	CYP	DEU	CZE	SRB	ESP	DNK	POL
13	ROU	CYP	CYP	ESP	CYP	MNE	DEU
14	LIE	ROU	GRC	DNK	POL	ESP	ESP
15	SRB	SVK	MNE	LVA	RUS	LIE	LIE
16	LUX	SRB	LIE	FRA	BGR	GRC	FRA
17	BGR	ESP	LVA	RUS	LIE	CZE	RUS
18	EST	MLT	RUS	POL	FRA	RUS	BGR
19	ITA	NLD	NLD	AND	BLR	AND	EST
20	LTU	RUS	AND	NOR	AND	SRB	AND
21	ISL	RKS	SRB	GRC	EST	BGR	BLR
22	DEU	EST	BGR	UKR	CZE	NLD	SRB
23	RUS	MDA	FRA	LTU	SRB	FRA	GRC
24	RKS	DNK	EST	BLR	NLD	EST	CZE
25	IRL	AND	BLR	BEL	GRC	BLR	NLD
26	BLR	IRL	UKR	NLD	LTU	UKR	MCO
27	GRC	FRA	IRL	CZE	IRL	IRL	IRL
28	BEL	ITA	RKS	RKS	RKS	MCO	UKR
29	AND	AUT	ITA	BGR	MCO	ITA	ITA
30	MCO	LTU	LTU	MCO	UKR	RKS	LTU
31	MLT	MCO	MCO	IRL	ITA	LTU	RKS
32	SVK	FIN	MLT	SVK	BIH	MLT	BIH
33	CZE	SMR	FIN	ITA	FIN	MDA	MLT
34	PRT	MNE	SVK	MLT	MLT	SMR	HUN
35	MKD	PRT	MDA	PRT	SMR	HUN	SMR
36	BIH	BLR	SMR	BIH	SVK	FIN	MDA
37	UKR	HUN	HUN	GBR	HUN	SVK	FIN
38	FIN	BGR	BIH	SMR	SVN	BEL	SVK
39	SVN	CHE	BEL	SVN	MDA	BIH	BEL
40	GBR	LVA	PRT	FIN	BEL	PRT	SVN
41	HUN	BIH	MKD	HUN	PRT	SVN	PRT
42	MDA	MKD	SVN	MDA	MKD	MKD	MKD
43	SMR	GBR	CHE	MKD	GBR	CHE	GBR
44	SWE	SWE	GBR	CHE	CHE	GBR	CHE
45	CHE	SVN	SWE	SWE	SWE	SWE	SWE

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