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Concurrent tracking of strain and noise bursts at ferroelastic phase fronts

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Many technological applications are based on functional materials that exhibit reversible first-order ferroelastic transitions, including elastocaloric refrigeration, energy harvesting, and sensing and actuation. During these phase changes inhomogeneous microstructures are formed which fit together different crystalline phases, and evolve abruptly through strain bursts related to domain nucleation and the propagation of phase fronts, accompanied by acoustic emission. Mechanical performance is strongly affected by such microstructure formation and evolution, yet visualisation of these processes remains challenging. Here we report a detailed study of the bursty dynamics during a reversible stress-induced martensitic transformation in a CuZnAl shape-memory alloy. We combine full-field strain-burst detection, performed by means of an optical grid method, with the acoustic tracking of martensitic strain avalanches using two transducers, which allows for the location of the acoustic-emission events to be determined and the measurement of their energies. The matching of these two techniques reveals interface formation, advancement, jamming and arrest at pinning points within the transforming crystal.

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Martensitic transformations are first-order diffusionless phase transitions observed in a variety of crystalline materials, including metals, ceramics and proteins^{1–3}. They occur via cooperative atomic motions producing rapid changes of lattice structure, and typically form inhomogeneous microstructures involving different coexisting crystalline phases and variants. Many technological applications, such as environmentally-friendly elastocaloric refrigeration,^{4–6} waste-energy harvesting^{7,8}, smart sensing and actuating^{1,3}, are based on functional ferroelastic² materials, like shape-memory alloys, exhibiting highly reversible martensites^{7,9–11}. The intermittent progress of the structural transformations is inherent to the first-order character of these solid-state phase transitions². The microstructure responds to changes in environmental conditions through strain avalanching^{12,13}, with associated bursts of acoustic emission (AE)^{13–20}, related to the nucleation of phase domains and to phase-front advancements^{12–14}. The functional properties and stability of the material are strongly affected^{16,7,10,11} by these events marking microstructural evolution and reorganization, and their visualisation and thorough understanding is currently a big challenge^{12,13,17,21–24}.

To shed light on the details of these phenomena, we have studied the strain-avalanching in the stress-induced martensitic transformation in a CuZnAl shape-memory alloy^{12,14}. For this purpose we combined two different techniques: on the one hand, AE detection using two transducers²¹, which has unbeatable time resolution¹⁶ and allows for avalanche localisation and energy measurement; and, on the other hand, strain measurement via the grid method, allowing for full-field strain imaging^{25–29}. These approaches, used separately so far, have much contributed to our understanding of structural transformations in crystalline solids. They are used concurrently here for the first time.

Results

Elongation test. We have used a Cu_{68.13}Zn_{15.74}Al_{16.13} (at.%) single-crystal grown by the Bridgman method. The specimen is a thin elongated parallelepiped with cylindrical heads for gripping. The vertical *y*-axis is oriented along the sample length, and close to the [001] crystallographic direction in the bcc austenitic lattice (see refs. ^{14,21} and Fig. 1a, b for dimensions and details). The elongated shape of this specimen is particularly suitable for our study, which concentrates on lengthwise phase-front propagation treated in a one-dimensional (1D) setting along the *y* direction (see below). In the absence of applied external force, this alloy exhibits a reversible symmetry-breaking martensitic transformation at $M_s = 234$ K from a cubic L2₁ high-temperature parent phase (austenite) to a lower-temperature monoclinic 18R product phase (martensite). The transition can also be induced at room temperature by applying a uniaxial loading. Prior to the present test, an appropriate heat treatment was performed so that the alloy was in an ordered state, free from internal stresses, and with a minimum vacancy concentration. The specimen was then submitted to a series of more than 20 loading-unloading cycles to reach a stationary transition path between the parent and product phases.

Figure 1a, b also show the bidimensional grid (with pitch 0.2 mm) transferred onto the specimen²⁵ to follow the strain evolution through the GM (see Methods). The parallel 1D study of AE along the *y* direction (see Methods) involved the recording of acoustic activity by means of two transducers suitably placed on the grips of the loading apparatus, as in Fig. 1c. The latter is an in-house designed gravity-based device¹² producing a strictly monotonic uniaxial load, which can be applied at a very low rate. During the elongation test, with time *t* running in seconds, we monitored the stress-induced martensitic transformation under

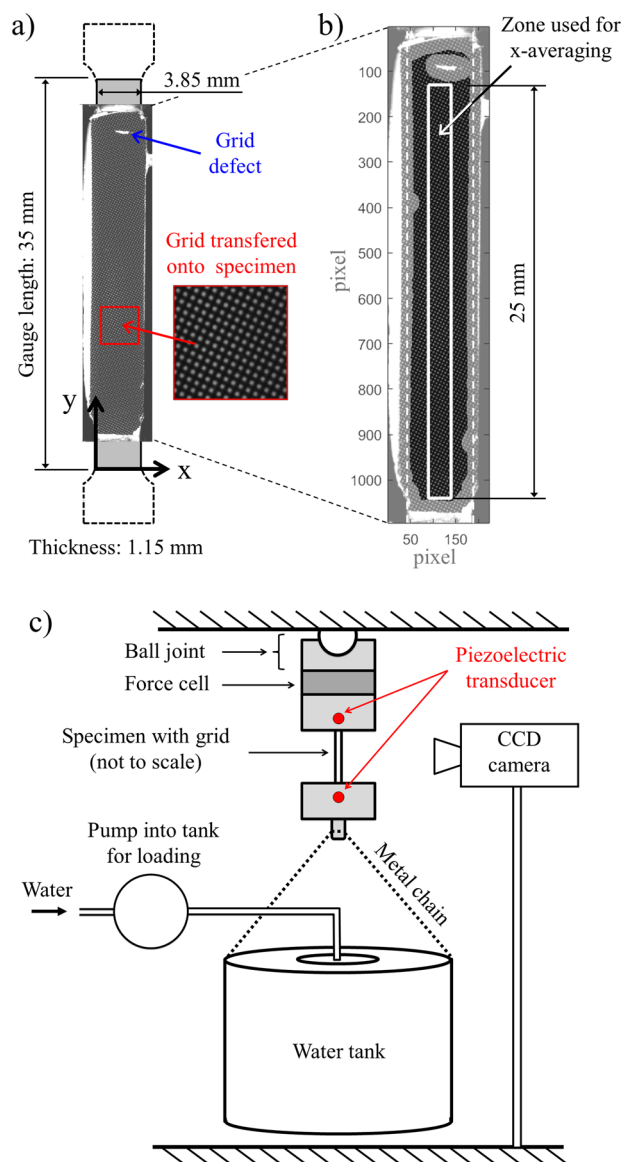


Fig. 1 Experimental setup. **a** Sketch of the CuZnAl single-crystal specimen (3.85 × 35 × 1.12 mm), with photograph of the grid transferred onto it. **b** Detail showing the rectangular strip (outlined in white) used to extract the 1D strain profiles along the vertical *y*-axis, by means of *x*-averaging of the 2D strain maps produced by the grid method. The white-dashed lines mark the specimen sides. The dark-shaded domain on the grid was used for 2D strain mapping to avoid side effects. **c** Schematic view of the loading device, showing the position of the piezoelectric transducers used for the 1D localisation, along the *y*-axis, of the acoustic events.

the following conditions: (a) preloading of 81.92 MPa; (b) constant loading rate 109.7 Pa/s, up to 88.97 MPa, with a total duration of about 64,200 s (i.e. ~8 h; room temperature: 25.7 ± 0.5 °C). After the application of the preload the force was increased very slowly so as to approach the transformation plateau in almost adiabatic conditions, and to obtain the phase transition with a minimum of precursors or spurious disturbances, and a minimal dependence on the loading history. The observed plateau (duration ~27 min) indeed resulted to be nearly horizontal, shown in black on the macroscopic stress-strain curve of Fig. 2a, with the elastic load-up portions shown in red. To ensure specimen integrity, the loading was stopped shortly after the elastic response resumed at the end of the plateau, although

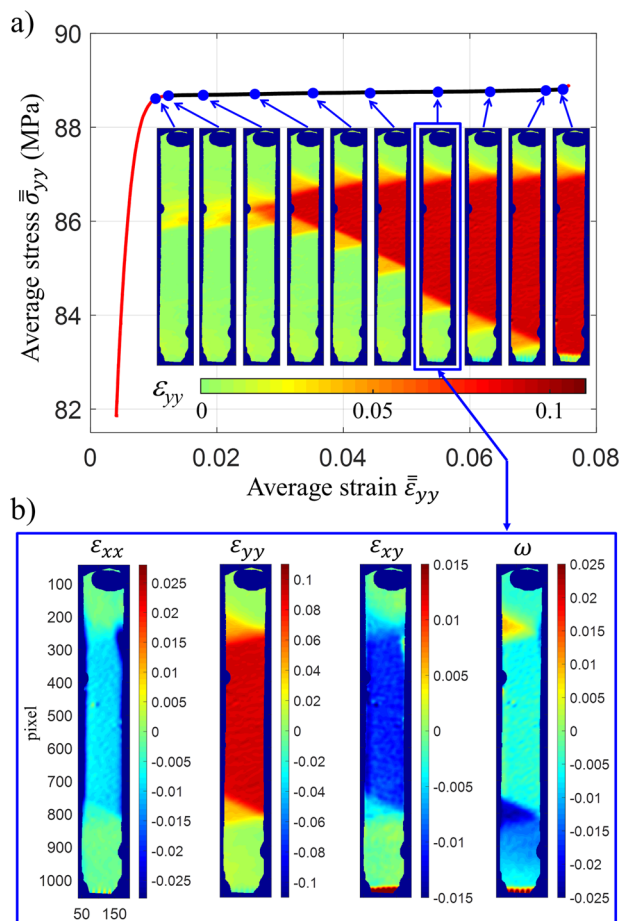


Fig. 2 Stress-strain curve and evolution of the strain field. **a** The elastic part of the stress-strain curve is indicated in red and the transformation plateau in black. Snapshots of the map for the strain component ϵ_{yy} are shown at various loading stages, marked by blue dots on the plateau. **b** Maps of all the in-plane strain components ϵ_{xx} , ϵ_{xy} , ϵ_{yy} , and of the local rotation angle ω , corresponding to the average-strain value $\bar{\epsilon}_{yy} = 0.052$. See also Supplementary Movie 1.

the residual austenite might have further transformed at higher loads. The monitoring of AE during the test, done concurrently to strain detection, recorded $\sim 110,000$ [$\sim 60,000$] AE hits at the upper [lower] transducer, with the corresponding amplitudes and energies (see Methods).

Strain field evolution. By suitably processing^{25–28} the captured images of the deforming grid, we obtained a sequence of (x, y) -maps during the entire elongation test, giving the spatial distribution on the sample's face of the linear in-plane strain components ϵ_{xx} , ϵ_{xy} , ϵ_{yy} , and of the local rotation angle ω around the z -axis. Figure 2 displays a number of such maps describing the strain evolution along the transformation plateau.

Because of the 1D character of our analysis of AE activity along the y -axis on this elongated specimen, we focus hereafter on the behaviour of the ϵ_{yy} strain component, whose signal-to-noise ratio is also the highest compared to ϵ_{xx} and ϵ_{xy} . The strain data animation in Supplementary Movie 1 shows the temporal evolution of the ϵ_{yy} -map on the sample (green austenite; red martensite). This evidences the progress of the structural phase change during the test (total duration on the plateau: about 27 min, clocked by the time counter in s, with the blue dot indicating current conditions on the stress-strain curve). We see from Fig. 2a and Supplementary Movie 1 that the austenite-to-martensite

transformation mainly proceeded here through the creation and propagation of two triangular fronts (in yellow-orange on the strain maps) lying between pure austenite (in red) and pure martensite (in green). Martensite nucleated at a point with higher stress fluctuations within the bulk or on the surface of the sample. The triangular shape of the observed fronts is explained by the formation of martensitic twinned micro-layers, whose average strains are kinematically compatible with austenite and pure martensite across suitable non-parallel transversal planes in the sample, see for instance the X-microstructures analyzed in Ref. 30. Supplementary Movie 1 also shows the temporal evolution of the associated strain-rate $\dot{\epsilon}_{yy}$ maps on the sample (see Methods), which clearly highlight the bursty propagation of the triangle-shaped fronts. Strain-rate values are here limited to $2.5 \times 10^{-3} \text{ s}^{-1}$ for better visualisation of the transformation intermittency investigated in detail below. While the advancing phase front carried most of the strain avalanching during the elongation, small transformation-strain bursts occurred nonetheless throughout the specimen, with small precursor events taking place also before entering the transformation plateau³¹, producing the slight non-linearity in the red elastic part of the stress-strain curve in Fig. 2a.

Analysis of global strain- and AE-intermittency. We first assess the global stress-strain behaviour of the specimen during the elongation test. We consider the average of the ϵ_{yy} strain [σ_{yy} stress] over the entire sample, denoted by $\bar{\epsilon}_{yy}$ [$\bar{\sigma}_{yy}$]. These quantities undergo a quite continuous evolution at the time scale of the plateau duration, as shown by the black curves in Figs. 2a and 3a. The corresponding strain rate $\dot{\bar{\epsilon}}_{yy}$ was then computed by taking the differences in consecutive strain maps separated by a time interval of 3.8 s. The resulting values of $\dot{\bar{\epsilon}}_{yy}$ exhibit the spiky time evolution shown in red in Fig. 3a. This clearly highlights the jerky progress of the martensitic transformation despite the very small and constant loading rate and the apparent continuity of $\bar{\epsilon}_{yy}$. The time evolution of the number of AE hits, recorded within the same 3.8-s bins, is also plotted in blue in Fig. 3a. The high correlation of this intermittent AE signal with the strain-rate spiking can be noticed, giving a scatter plot tightly clustered near the graph bisector in Fig. 3b. The off-diagonal crosses near the bottom of Fig. 3b correspond to the decoupling of the AE and the strain-rate signals at the end of the transformation plateau (shaded area of Fig. 3a). This is due to the lower phase front moving progressively out of the grid zone near the end of the loading test, so that AE recording continued while strain events could no longer be detected (see the lower orange triangle exiting through the bottom end of the strain maps in the last snapshots of Fig. 2a, and the end of Supplementary Movie 1).

Analysis of local strain- and AE-events. The intermittent evolution of the global quantities in Fig. 3 results from the local intermittency in the underlying structural transformation within the specimen. We studied this first through the localisation of the acoustic emission in the sample. From the total $\sim 70,000$ AE hits recorded during the test, it was possible to determine the y -location of $\sim 38,000$ AE events (see Methods). Their (t, y) -chart with energies is given in Fig. 4a, with Fig. 4b displaying the corresponding AE number density. We studied at the same time the associated local space-time strain intermittency by first considering the differences between consecutive 2D ϵ_{yy} -strain maps, with the same 3.8-s time step as in Fig. 3a (see also Supplementary Movie 1). Through x -averaging, these maps give the y -profiles of the 1D strain rate $\dot{\epsilon}_{yy}$ vs. time t , where $\bar{\epsilon}_{yy}$ is the

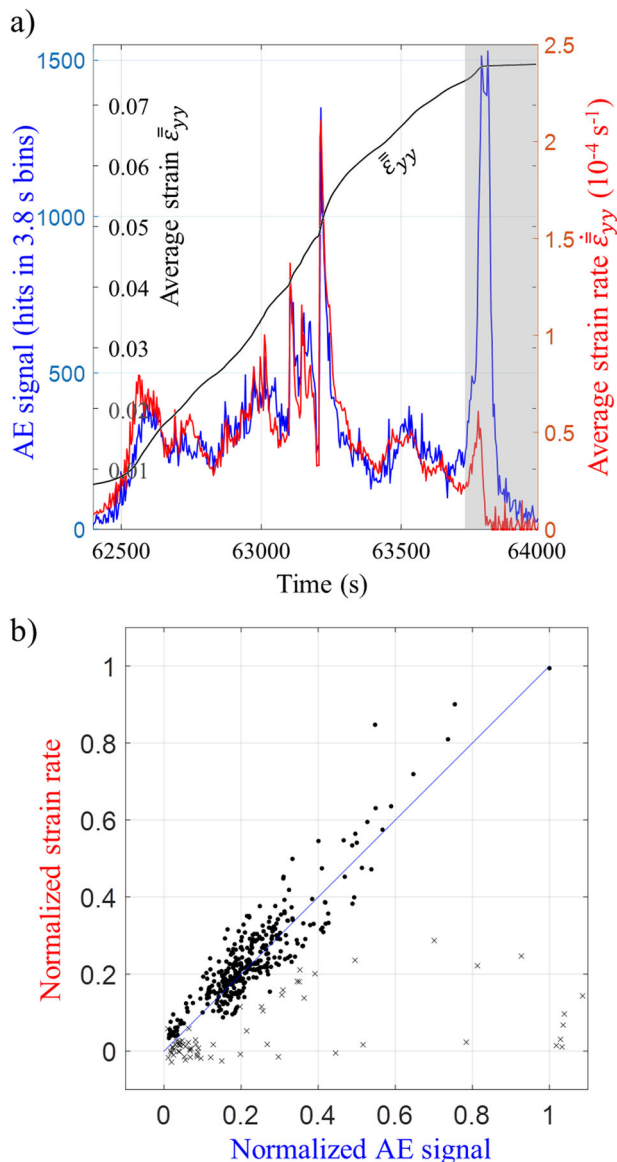


Fig. 3 Concurrent tracking of average-strain and overall AE intermittency during the phase transformation. **a** Time evolution of the average-strain rate $\dot{\bar{\epsilon}}_{yy}$ (red) and of the time-density of AE hits (blue) along the transformation plateau, where $\bar{\epsilon}_{yy}$ is the value of ϵ_{yy} averaged over the sample. The corresponding time evolution of $\bar{\epsilon}_{yy}$ is also shown (black). The time step is 3.8 s for both signals. The shaded area indicates the phase-front exiting the grid at the end of the test, with continuing AE recording but no strain detection. **b** Correlation between strain-rate and AE signal (dots), normalised by peak values near $t = 63,200$ s. Crosses correspond to data from the shaded zone of panel **a** where AE and strain-rate signals are decoupled. (The figure contains 352 dots and 68 crosses.) Pearson [Spearman] correlation value for dots -0.90 [-0.85].

x -average of ϵ_{yy} across the central strip in Fig. 1b. This produced the ~ 420 colour-coded 1D strain-rate y -profiles along the plateau which are represented on the same (t, y) -plane in Fig. 4c. We observe in Fig. 4a, b the nucleation of martensite marked by high-energy AE hits and high strain-rate activity near $t = 62,500$ s, with the ensuing separation of the two phase fronts moving towards the ends of the sample as the transformation progresses. Due to the x -averaging on the thin strip in Fig. 1b, the propagation of the triangular fronts of Fig. 1a is described here by the advancement with t of two small nearby high strain-rate intervals, forming two

parallel high-activity bands in the (t, y) -plane. This is especially evident for the lower phase front in the white-dashed inset of Fig. 4c. We notice that small transformation events, detected by both strain and acoustic emission, are present also away from the phase fronts, especially in the martensitic region of the sample.

In the present 1D framework, the distinct transformation-strain avalanches on the sample are then tracked by considering, on each y -profile of $\dot{\bar{\epsilon}}_{yy}$ in 4c, the set of y -coordinates whereon the value of the strain rate $\dot{\bar{\epsilon}}_{yy}$ exceeds the noise threshold $3 \times 10^{-4} \text{ s}^{-1}$ (see Methods). At any given t , a 1D strain event is thus defined by each separate y -interval on which $\dot{\bar{\epsilon}}_{yy}$ reaches above the threshold. This assures that localised strain-rate surges emerging from the noise floor while monitoring the phase-change reliably reflect the occurrence of a transformation burst. In this way ~ 1100 strain avalanches were identified on the plateau, see Fig. 4d. Besides its interval size, each 1D strain event is also characterised by its epicenter, i.e. the value of y on which $\dot{\bar{\epsilon}}_{yy}$ is maximal, as well as its magnitude, defined by the sum of the squared values of $\dot{\bar{\epsilon}}_{yy}$ over the interval. The results shown in the four panels of Fig. 4 clearly highlight various different aspects of the strong spatial and temporal heterogeneity in the phase-transformation activity under the slow, steady forcing. This is also underscored by the heavy-tailed distributions in Fig. 5, pointing to the emergence of scale-free behaviour in the material during the transition process, as reported earlier separately for strain^{12,13} and AE^{14–16} avalanching. In Fig. 5 the dashed blue line indicates a power-law distribution with exponent ~ 1.8 , which is in the range of the AE exponents previously found in these SMAs^{14–16}.

The 3.8-s time step considered above for the strain maps is orders of magnitude larger than the typical time scales of AE avalanche durations¹⁶. Each strain event evidenced in Fig. 4d thus originates from the merging of a large and variable number of microscale transition bursts. Such wide separation of scales is partially obviated by considering the density of localised AE events in suitable time bins, as done in Fig. 4b. To the latter we can thus superpose the strain-burst data of Fig. 4d. The result can be seen in Fig. 6a, where we notice the remarkably good agreement between the results of the two measurement techniques utilised to track the transformation intermittency in space and time. The inset to Fig. 6a shows the good correlation between the AE and strain data even at the present scale of local transition events, and not solely at the scale of the overall sample as in Fig. 3b. Some specific features of this concordance are seen in the close-up Fig. 6b. Here the different experimental techniques concurrently detect successive changes in the phase transformation intensity levels as they occur in the sample. We notice a low activity interval at $t = 63,050$ – $63,100$ s, followed by strong activity from about $t = 63,100$ s to an almost complete pause near $t = 63,200$ s, possibly due to a strong pinning site. There ensues a rapid sequence of large transformation bursts at $t = 63,210$ – $63,230$ s. Such details greatly enhance and very usefully complement the spatially opaque description of the global sample behaviour obtained via the averaged quantities in Fig. 3a.

Discussion

We have performed a detailed investigation of the stress-induced reversible martensitic transformation in a CuZnAl shape-memory alloy, considering a simplest case wherein the phase change largely occurs through the development and advancement of two diverging austenite-martensite triangle-shaped strain fronts. We have studied the intermittent progress of these complex interfaces by combining the full-field strain-burst detection via the optical grid method, concurrently with acoustic detection allowing for

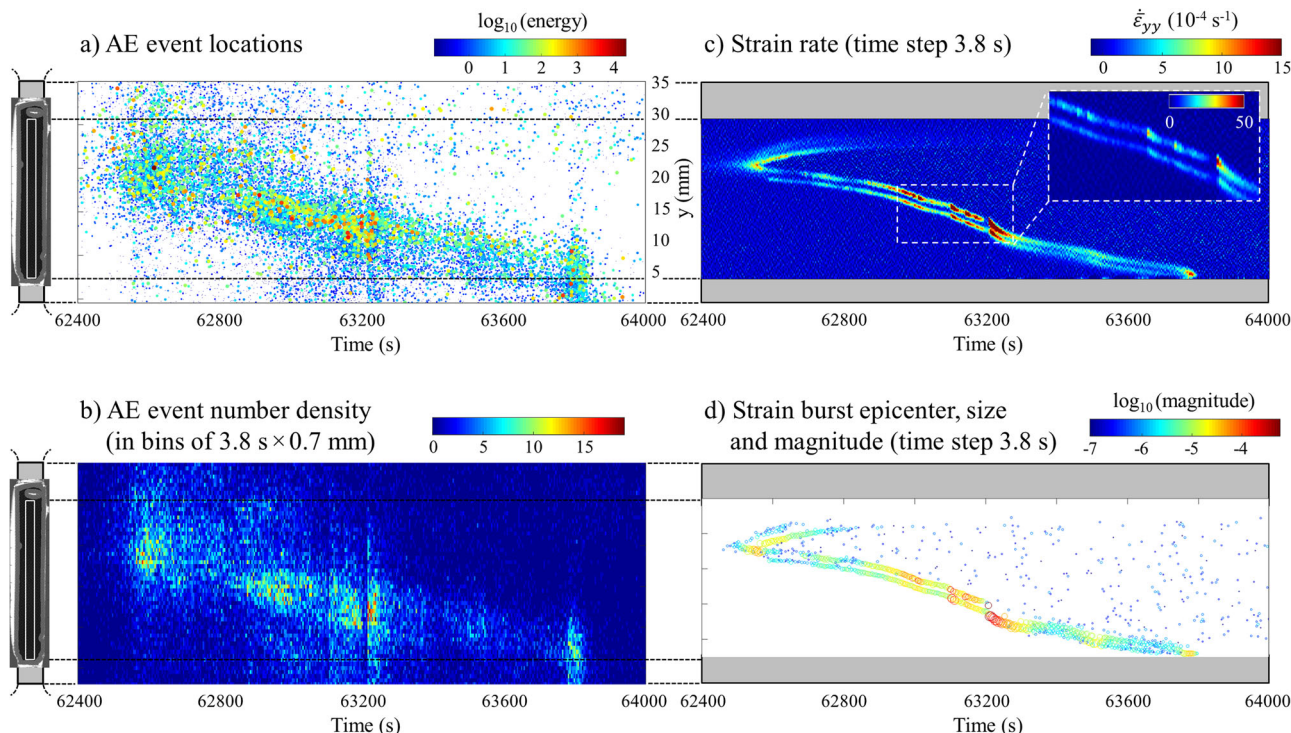


Fig. 4 Strain-rate data and AE data on the sample and along the transformation plateau, plotted on the (t, y) -plane. **a** AE event locations and energies. **b** Number density of localised AE events derived from the map in panel **a**, in bins of dimensions $0.7 \text{ mm} \times 3.8 \text{ s}$. **c** Profiles in y of the x -averaged strain-rate $\dot{\epsilon}_{yy}$ for each time t . Inset: detail of the austenite/martensite front propagation. **d** Epicenters of 1D strain-bursts, with associated size and magnitude (size represented by circle radius).

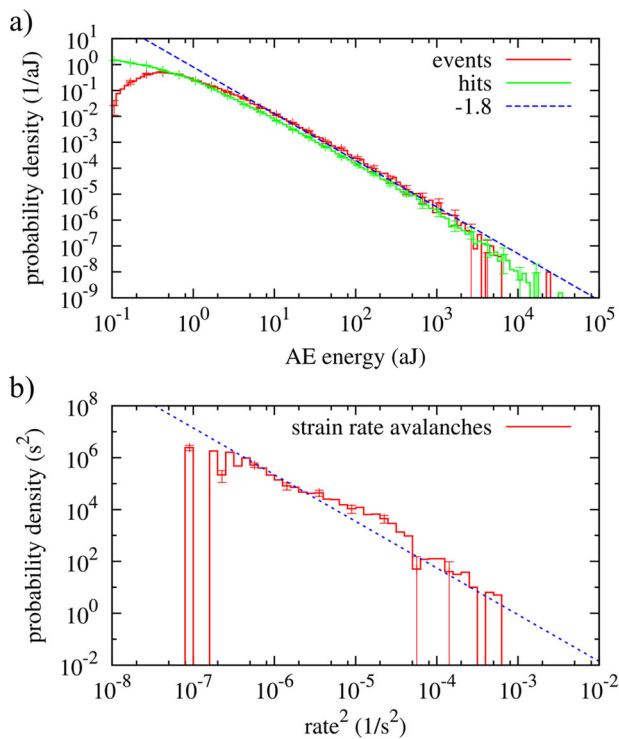


Fig. 5 Statistical properties of the phase-transformation avalanches on the plateau (log-log plots). **a** Probability density of AE avalanche energies. **b** Probability density of strain-avalanche magnitudes. In both panels the dashed blue line, drawn to guide the eye, indicates the behaviour of a power-law distribution with exponent -1.8 .

the 1D localisation of AE avalanches and the measurement of their energies. The matching of these two microseismological techniques revealed the great correlation of the independently collected data for strain and acoustic events in space and time, a property which could so far only be hitherto true, due to the expected common transformational origin of these phenomena. Our results highlight with unprecedented detail interface formation, advancement, jamming, and arrest at pinning points, within the crystal undergoing the phase transformation.

The experimental approach explored here for solid-state phase transitions can be readily adapted to more general and diverse shapes of the transforming sample, and under more complex loading conditions, as might be suggested by particular applications of reversible martensitic materials. Furthermore, it can be applied to the study of analogous bursty phenomena in the plasticity³² and fracture³³ of crystalline solids, as well as metallic glasses³⁴ and porous media³⁵, where the investigation and modeling of materials' behavior can greatly benefit from the detailed visualization and analysis made possible by the presently described techniques.

Methods

Strain and strain-rate mapping. The strain maps were obtained via the grid method²⁵⁻²⁹. A bidimensional grid with pitch 0.2 mm was first printed with a $50,800 \text{ dpi}$ photoplotter on a polymeric sheet and then transferred onto the sample surface by using a white E504 Epotecny adhesive.²⁵ The grid was slightly rotated with respect to pixel lines to avoid aliasing and the associated parasitic fringes²⁸. Grid images during the test were captured by a Sencicam QE camera featuring a 12-bit/ 1040×1376 pixel sensor and a 105 mm Tokina lens, with 10-ms shutter time and about 17 Hz acquisition frequency. Magnification was adjusted so that one grid pitch was encoded with about seven pixels, leading to a pixel size of 0.0274 mm on the sample. A direct-current LED system was used for lighting to avoid flickering. The grid images were processed by using the Localised Spectrum Analysis²⁷, with a Gaussian window characterized by a 7-pixel standard deviation. The movement of the physical points between reference and current grids was compensated²⁷, leading to the disappearance of the small local grid defects when subtracting the current and

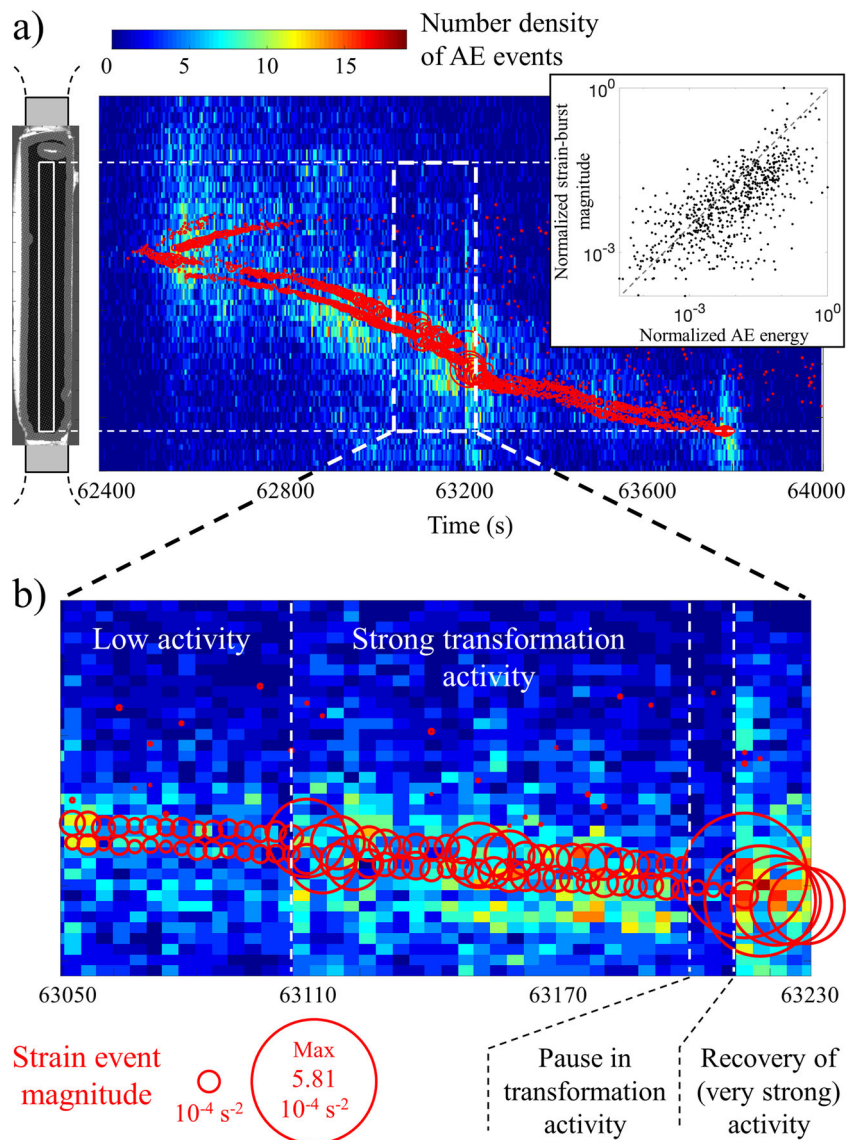


Fig. 6 Concurrent tracking of strain and AE avalanches in the sample during the phase transformation. **a** Superimposition of the strain avalanches in Fig. 4d onto the AE density map in Fig. 4b. Inset: correlation of strain-event magnitudes with pooled AE-event energies (normalised), when AE locations and strain avalanches are paired along the y -direction for each value of t . Pearson [Spearman] correlation is -0.42 [-0.79]. **b** Temporal zoom highlighting details of the bursty phase transformation progress in the sample during the elongation test.

reference distributions of the phases' modulation of the regular grid pattern caused by deformation. With the present data, the spatial resolution for strain measurements is conservatively estimated^{26,29} to be ~ 42 pixels, i.e. ~ 1.15 mm on the sample. The strain increments were first computed between two consecutive strain maps set apart by 64 grid images (i.e. ~ 3.8 s), and then divided by the corresponding 3.8 s time separation, to obtain strain rates in s^{-1} . This choice of time step gives a convenient trade-off between the measurement and temporal resolutions for strain-rates, and for AE data processing, and produces ~ 420 strain-increment maps on the transformation plateau, conventionally defined from $t = 62,400$ s to $t = 64,000$ s, with duration 1600 s. The noise threshold to reliably detect strain-rate bursts was experimentally estimated by analysing the fluctuations directly in the 1D strain-rate distributions. For this purpose, a stack of 15 consecutive y -profiles was considered, obtained during about 1 min at the beginning of the test after preloading, with the specimen being still while taking the images. Due to the noise reduction because of x -averaging across $N = 50$ pixels (Fig. 1b), this gave a noise standard deviation of $6.70 \times 10^{-5} \text{ s}^{-1}$. The final threshold for the 1D strain-rate profiles was conservatively taken to be 4.5 times this quantity, giving a value of $\sim 3 \times 10^{-4} \text{ s}^{-1}$. This allowed to identify 1058 1D strain bursts on the plateau.

AE detection and location. AE from the sample was detected by means of two micro-80 piezoelectric transducers from Europhysical Acoustics, working with a relatively flat response in the range 0.2–1 MHz. They were acoustically coupled to the upper and lower grips on the opposite face with respect to the camera. Electric

signals were preamplified (60 dB) and input into a two-channel PCI2 acquisition system from Europhysical Acoustics, working at 40 MHz with an A/D conversion of 18 bits. Individual AE hits were defined in both channels in the following way: a hit starts at time t_{ini} when the absolute value of the preamplified signal $|V(t)|$ from any channel crosses a noise threshold (21 dB, equivalent to 11.22 mV), and ends at t_{final} when $|V(t)|$ remains below the threshold until $t_{final} + 100 \mu\text{s}$. The amplitude of the hit is defined from the maximum value $|V_{max}|$ of the preamplified signal in the first $100 \mu\text{s}$, converted to dB according to $A(\text{dB}) = 20 \log(V_{max}/1 \mu\text{V}) - 60$. Then an $A = 60$ dB signal corresponds to a 1V peak in the preamplified signal and 1mV peak in the signal from the transducer. The energy of the hit is given by $E = \frac{1}{10k\Omega} \int_{t_{ini}}^{t_{final}} (V(t))^2 dt$. $N_1 = 108,471$ and $N_2 = 60,357$ hits were recorded in channels 1 (upper grip) and 2 (lower grip), respectively, the asymmetry being due to the differences in the acoustic coupling of the two transducers. The hit list so acquired was analyzed for the 1D-location of the AE events, defined from any pair of consecutive hits detected in opposite channels within less than $t_{max} = 0.038$ ms, with event location given by $y = 0.5L \left(1 - \frac{\Delta t}{t_{max}}\right)$, for $L = 35$ mm the length of the central part of the sample, and Δt the delay between the two hits. In this way 37,540 acoustic events were located along the y -axis of the specimen in Fig. 1a, of which 26,266 belong to the 25-mm interval in the averaging zone of Fig. 1b. The source energy of a located event is estimated by $E = \sqrt{E_1 E_2}$, where E_1 and E_2 are the energies measured in channel 1 and 2, respectively. This formula approximately corrects for the effects of attenuation in the sample, assuming a constant

exponential damping factor. Similarly, given its logarithmic character, the source amplitude is defined as $A = (A_1 + A_2)/2$.

Data availability

The data that support the findings of this study are available from the corresponding authors on reasonable request.

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Author contributions

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Competing interests

The authors declare no competing interests.


Additional information

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