

## Bioelectromagnetism

### Basic Concepts

- 1- True or False: The magnitude of the force exerted on one charge by another charge is inversely proportional to the square of the distance between the two charges.
- 2- True or False: By definition, the *electric field strength* at point P is given by  $\mathbf{E} = \mathbf{F}/Q_{\text{test}}$ .
- 3- True or False: The units of  $\mathbf{E}$  are volts (V).
- 4- True or False: Because  $\mathbf{E}$  fields exert forces on charges, work is required to move a charge from one point in space to another in the presence of an  $\mathbf{E}$  field. The work done per unit charge is called *electric potential difference*.
- 5- True or False: When  $\mathbf{E}$  does not vary with time, or when it varies slowly with time the frequency is low.
- 6- True or False: When charges are moving, they exert another kind of force on each other that is not along a line between the charges. Magnetic fields are used to account for this other kind of force.
- 7- True or False: Moving charges produce an electric current. This current  $\mathbf{I}$  produces a magnetic field  $\mathbf{B}$ .
- 8- True or False: Maxwell's equations, which are a fundamental set of equations that form the framework of all of classical electromagnetic field theory.
- 9- The shape of the wave as a function of time is called the *waveform*.
- 10- True or False: The simplest type of electrical waveform is constant with time. This is called *direct current* or *DC* (also called *static* fields).
- 11- True or False: Many applications in electromagnetics use waves that are single-frequency sine waves. These waves are often called *alternating current* or *AC* waves, because the current alternates from positive to negative and back again. A major characteristic of AC waves is that the electric and magnetic fields can

generate each other and are therefore coupled and cannot be analyzed separately.

- 12- Electromagnetic radiation of frequency  $f$ , when waves propagate in free space or in the human body wavelength is maintained. The wavelength does not depend on the medium where spreads.
- 13- Consider a signal of frequency  $f=2.45$  GHz. Calculate its  $\lambda$  in free space. Place it in the spectrum.
- 14- Consider a signal of frequency  $f=433$  MHz. Calculate its  $\lambda$  in free space. Place it in the spectrum.
- 15- What are ISM frequency bands?

## EM Propagation in Biological Media

1. A plane wave travels from semi-infinite medium 1 to semi-infinite medium 2 and propagates normal to the boundary between the two media.



Show that the reflection coefficient of a plane wave with normal incidence on a flat boundary is given as:

$$\Gamma = \frac{\sqrt{\epsilon_{r1}} - \sqrt{\epsilon_{r2}}}{\sqrt{\epsilon_{r1}} + \sqrt{\epsilon_{r2}}}$$

2. A plane wave travels from semi-infinite air medium to semi-infinite skin medium. Find the reflection and transmission coefficients assuming an incident signal of  $f=1.8$  GHz. Take into consideration permittivity and conductivity values from Table I.

TABLE I  
 RELATIVE PERMITTIVITY  $\epsilon_r$ , CONDUCTIVITY  $\sigma$  (S/M) OF THE BODY TISSUES

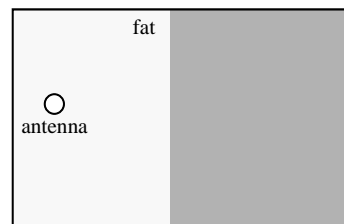
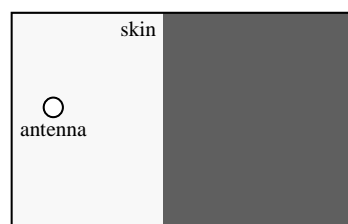
Frequency		skin	fat	muscle	bone
10 MHz	$\epsilon_r$	361.66	13.77	170.73	36.77
	$\sigma$	0.19	0.03	0.62	0.04
433 MHz	$\epsilon_r$	46.08	5.57	56.87	13.07
	$\sigma$	0.70	0.04	0.80	0.09
0.9 GHz	$\epsilon_r$	41.4	5.46	55.03	12.45
	$\sigma$	0.86	0.05	0.94	0.14
1.8 GHz	$\epsilon_r$	38.87	5.35	53.55	11.78
	$\sigma$	1.18	0.08	1.34	0.27
2.45 GHz	$\epsilon_r$	38.01	5.28	52.73	11.38
	$\sigma$	1.46	0.10	1.74	0.39
5 GHz	$\epsilon_r$	35.77	5.03	49.54	10.04
	$\sigma$	3.06	0.24	4.04	0.96
10 GHz	$\epsilon_r$	31.29	4.60	42.76	8.12
	$\sigma$	8.01	0.58	10.63	2.14
17 GHz	$\epsilon_r$	24.54	4.15	34.06	6.49
	$\sigma$	16.09	1.07	20.71	3.48

- Assume that a plane wave with  $E_0=200\text{V/m}$  and  $f=1.8\text{ GHz}$  is propagating in the  $z$  direction though the air and arrives to our body. How much field will be transmitted?
- Repeat problem 2 for frequencies of 10 MHz, 433 MHz, 900 MHz, 2.45 GHz, 5 GHz and 17 GHz. Discuss the results.
- Find the penetration depth for the media of problem 2 at the specified frequency.
- Repeat problem 5 for frequencies of 10 MHz, 433 MHz, 900 MHz, 1,8 GHz, 2.45 GHz, 5 GHz, 10 GHz and 17 GHz. Discuss the results.
- The complex permittivity of skin, fat, and muscle at 915 MHz, 2.45 GHz and 10 GHz, respectively, is given in the following table:

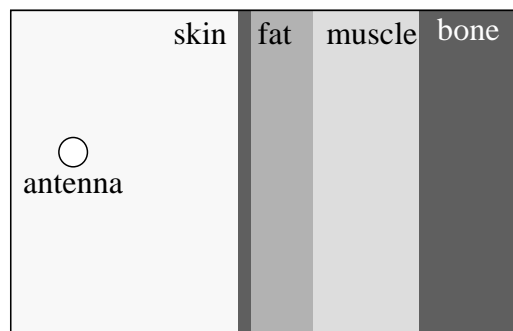
	915 MHz		2.45 MHz		10 GHz	
	$\epsilon'$	$\epsilon''$	$\epsilon'$	$\epsilon''$	$\epsilon'$	$\epsilon''$
skin	41.5	17	38	11	31	14.5
fat	11.3	2.2	10.9	2	8.8	3.1
muscle	55	19	53	12.5	43	19

Calculate the loss tangent at the specified frequencies.

- Find the reflection coefficients of the skin-fat and fat-muscle interfaces at the specified frequencies of problem 7.
- Assume that a plane wave with frequency of 1.8 GHz is propagating in the  $z$  direction through the air and arrives to a skin or fat tissue. Which tissue will absorb more energy? Take into consideration permittivity and conductivity values from Table I.



10. Assume that a plane wave with  $E_0=200\text{V/m}$  and  $f=1.8\text{ GHz}$  is propagating in the  $z$  direction through the air and arrives to the skin tissue of problem 9. Calculate the electric field strength 1 cm below the air-skin interface. Take into consideration permittivity and conductivity values from Table I. Repeat the calculation for a signal of 17 GHz.
11. Assume that a plane wave with frequency of 1.8 GHz is propagating in the  $z$  direction through the air and arrives to the following tissue sequence:



Which tissue will now absorb more energy? Take into consideration permittivity and conductivity values from Table I.

12. Consider now a plane wave with  $E_0=50\text{V/m}$  and  $f=1.8\text{ GHz}$  is propagating in the  $z$  direction through the air and arrives to the tissue sequence of problem 11. If we assume a skin and fat thicknesses of 3 mm and 5 mm respectively, calculate the electric field maximum amplitude that could reach the muscle tissue. Ignore the influence of standing waves.

## Dosimetry

1. A plane wave with  $E_0=100$  V/m travels from semi-infinite air medium to semi-infinite skin medium. Find the maximum local SAR in the skin assuming an incident signal of  $f=1.8$  GHz. Take into consideration constant values from Tables I and II.

TABLE I  
RELATIVE PERMITIVITY  $\epsilon_r$ , CONDUCTIVITY  $\sigma$  (S/M) OF THE BODY TISSUES

Frequency		skin	fat	muscle	bone
10 MHz	$\epsilon_r$	361.66	13.77	170.73	36.77
	$\sigma$	0.19	0.03	0.62	0.04
433 MHz	$\epsilon_r$	46.08	5.57	56.87	13.07
	$\sigma$	0.70	0.04	0.80	0.09
0.9 GHz	$\epsilon_r$	41.4	5.46	55.03	12.45
	$\sigma$	0.86	0.05	0.94	0.14
1.8 GHz	$\epsilon_r$	38.87	5.35	53.55	11.78
	$\sigma$	1.18	0.08	1.34	0.27
2.45 GHz	$\epsilon_r$	38.01	5.28	52.73	11.38
	$\sigma$	1.46	0.10	1.74	0.39
5 GHz	$\epsilon_r$	35.77	5.03	49.54	10.04
	$\sigma$	3.06	0.24	4.04	0.96
10 GHz	$\epsilon_r$	31.29	4.60	42.76	8.12
	$\sigma$	8.01	0.58	10.63	2.14
17 GHz	$\epsilon_r$	24.54	4.15	34.06	6.49
	$\sigma$	16.09	1.07	20.71	3.48

TABLE II  
DENSITY OF THE BODY TISSUES ( $\text{kg/m}^3$ )

skin	fat	muscle	bone
1100	916	1041	1990

2. A plane wave with  $E_0=100$  V/m travels from semi-infinite air medium to semi-infinite skin medium. Find the maximum local SAR in the skin assuming incident signals of frequencies 10 MHz and 5 GHz. Take into consideration constant values from Tables I and II.

3. A plane wave with  $E_0=100$  V/m travels from semi-infinite air medium to semi-infinite skin medium. Find the 1 g average SAR in the skin assuming an incident signal of  $f=1.8$  GHz. Take into consideration constant values from Tables I and II. Repeat the calculation for with  $E_0=100$ V/m an incident signal of  $f=5$  GHz.